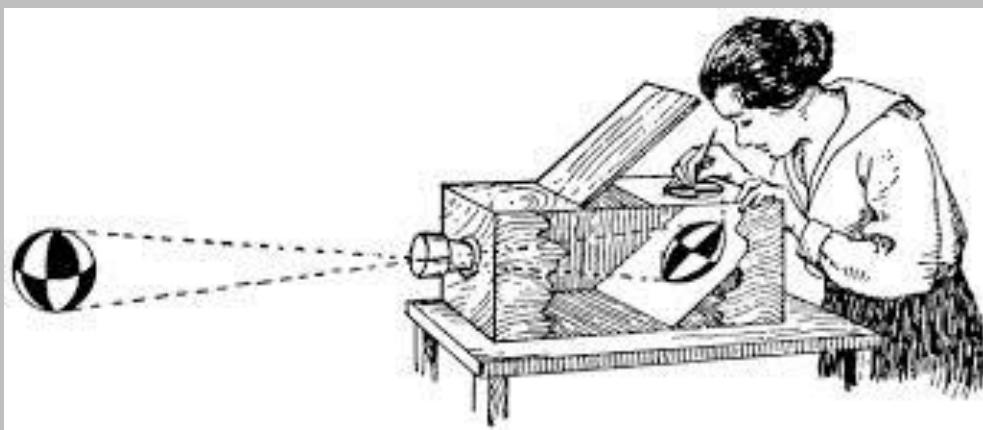
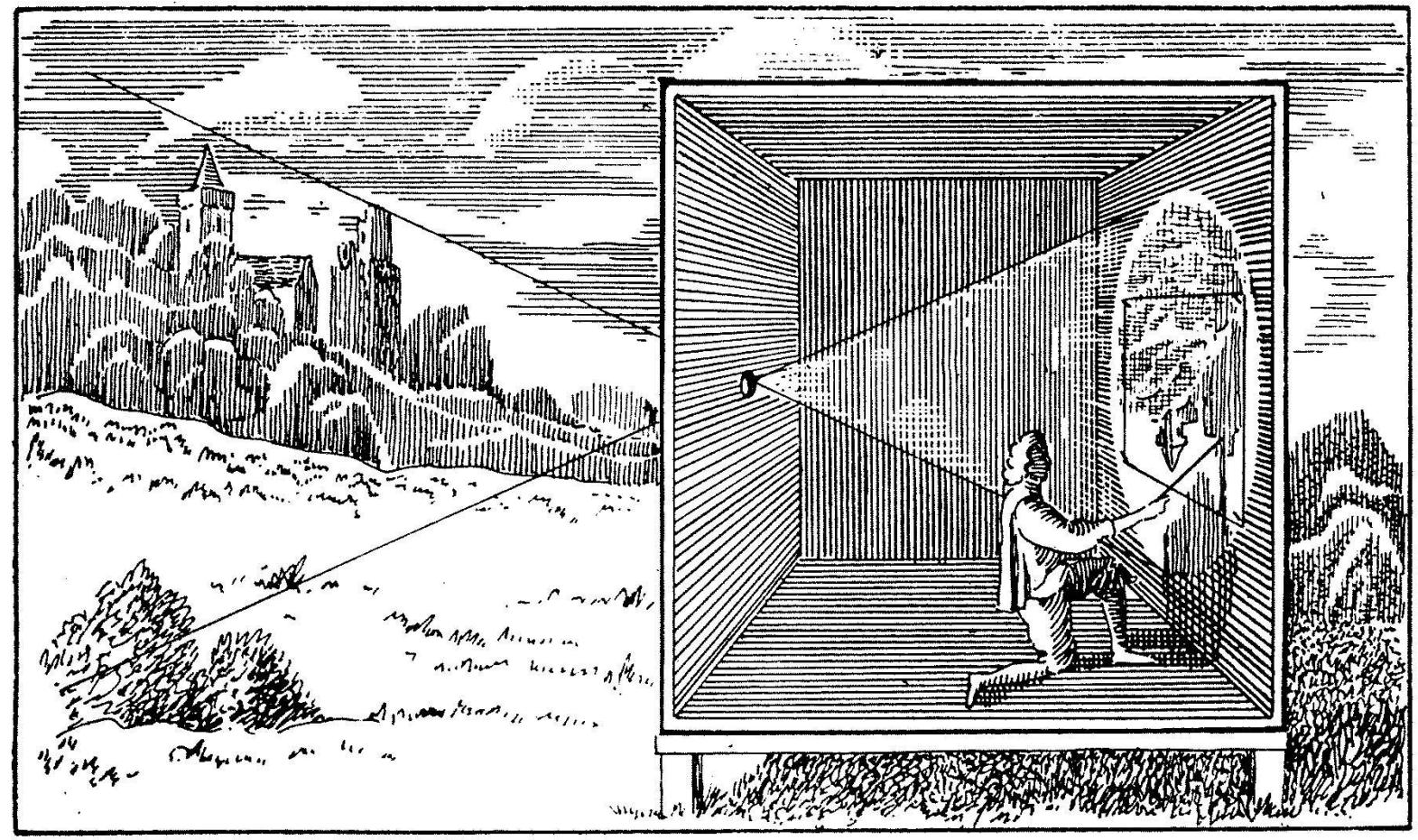
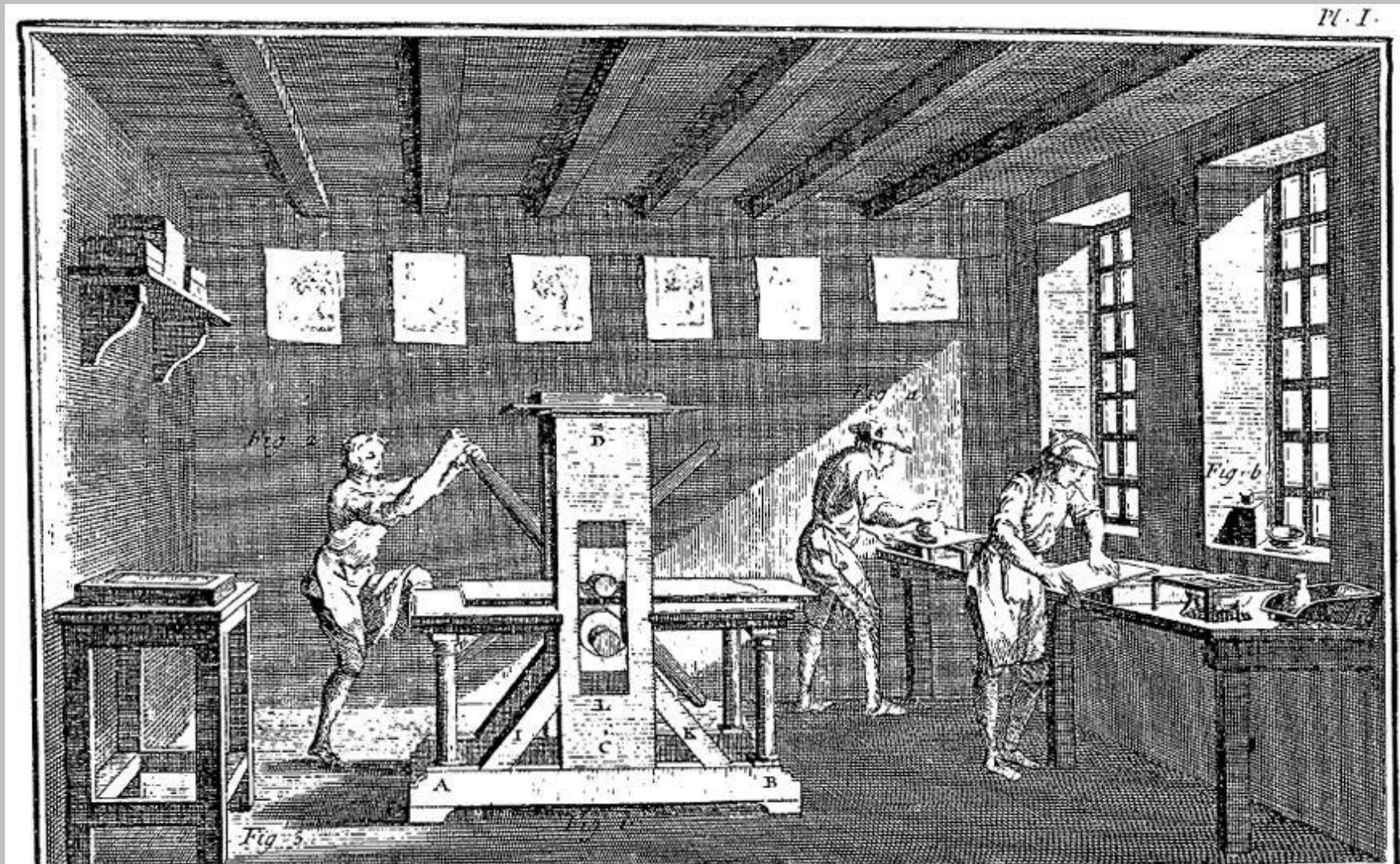


# Informatique Graphique 3D

Introduction

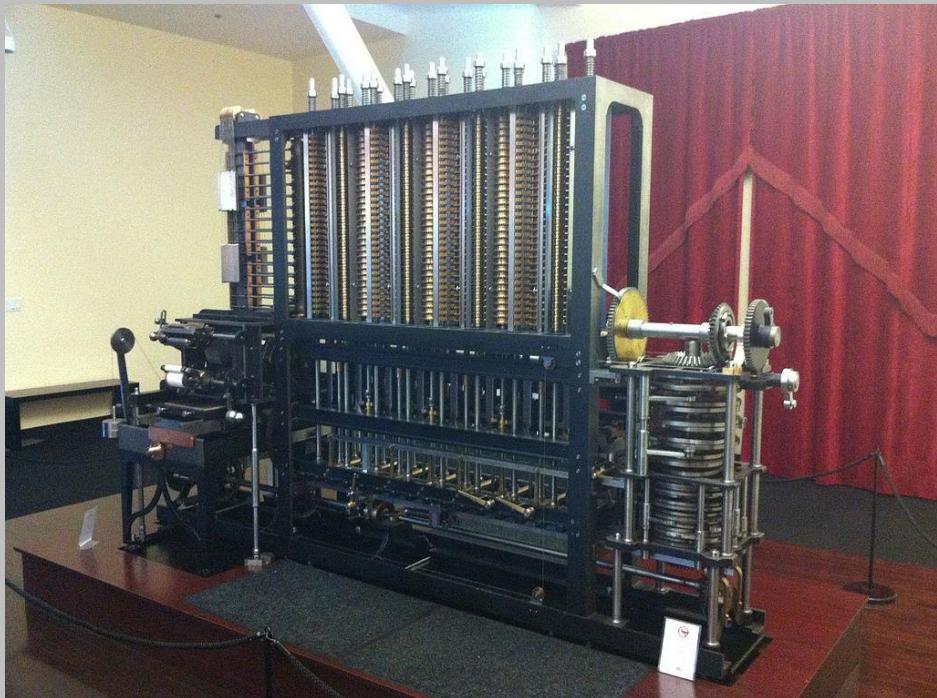
# Histoire de l'imagerie 3D



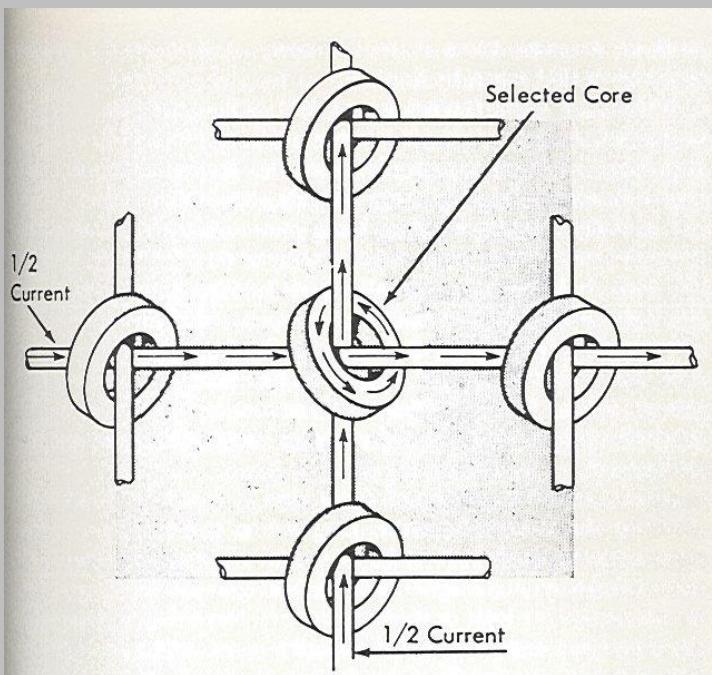
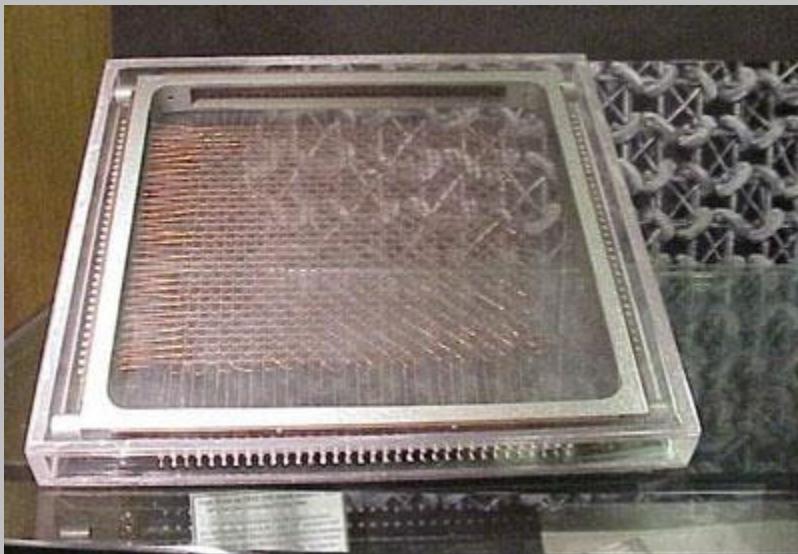
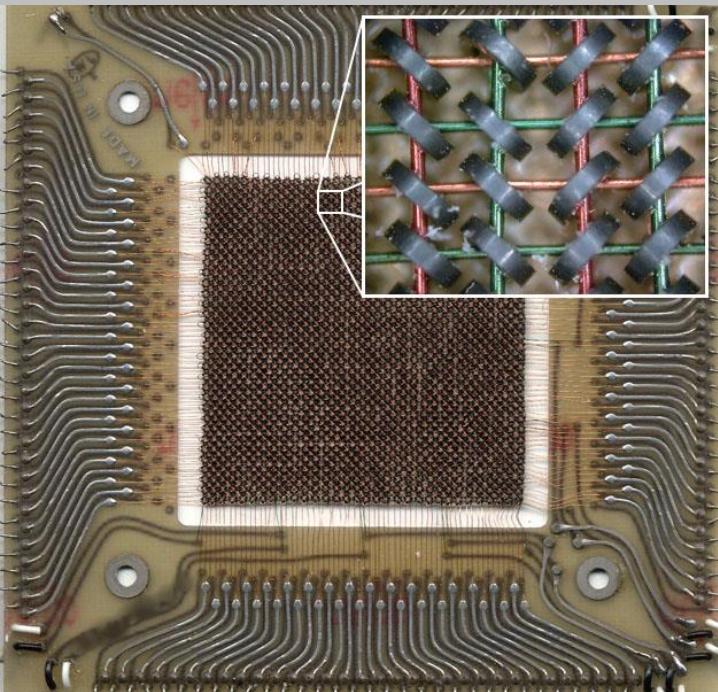


*Fig. 5.*









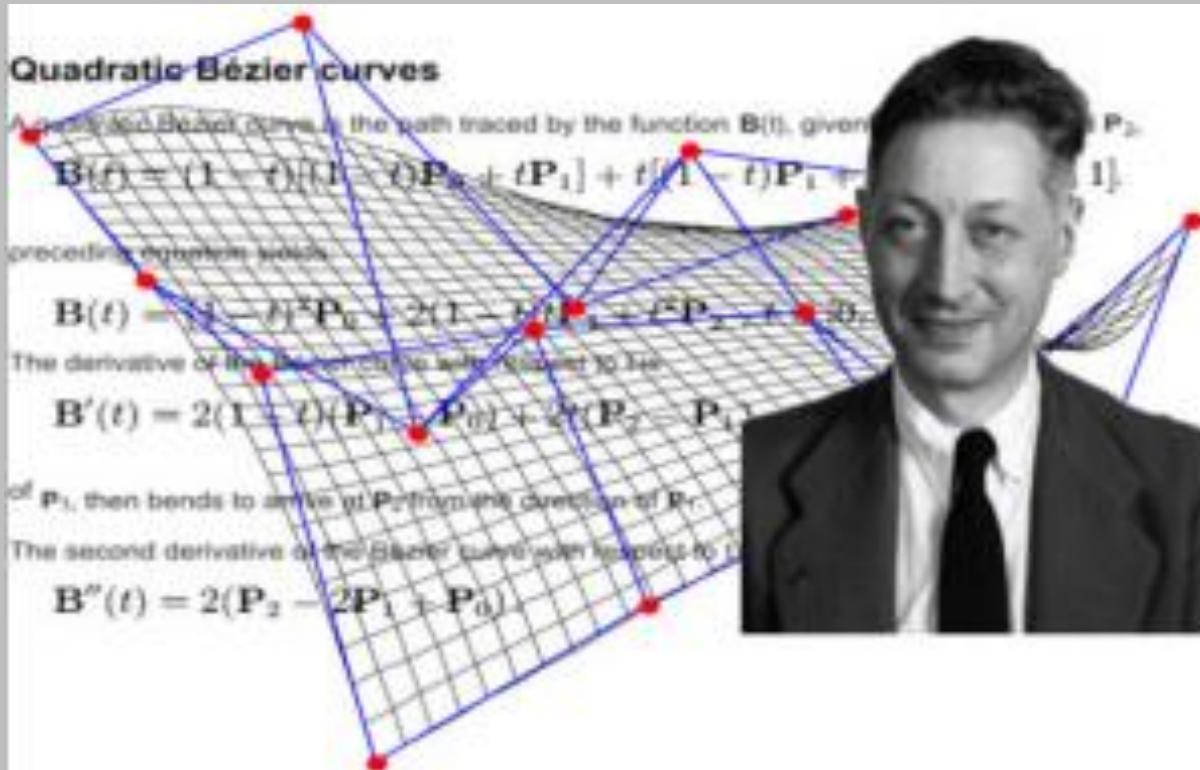
- 1948 - ENIAC



- 1961 – Spacewar! Premier jeu vidéo



- 1962 – Courbe de Bézier



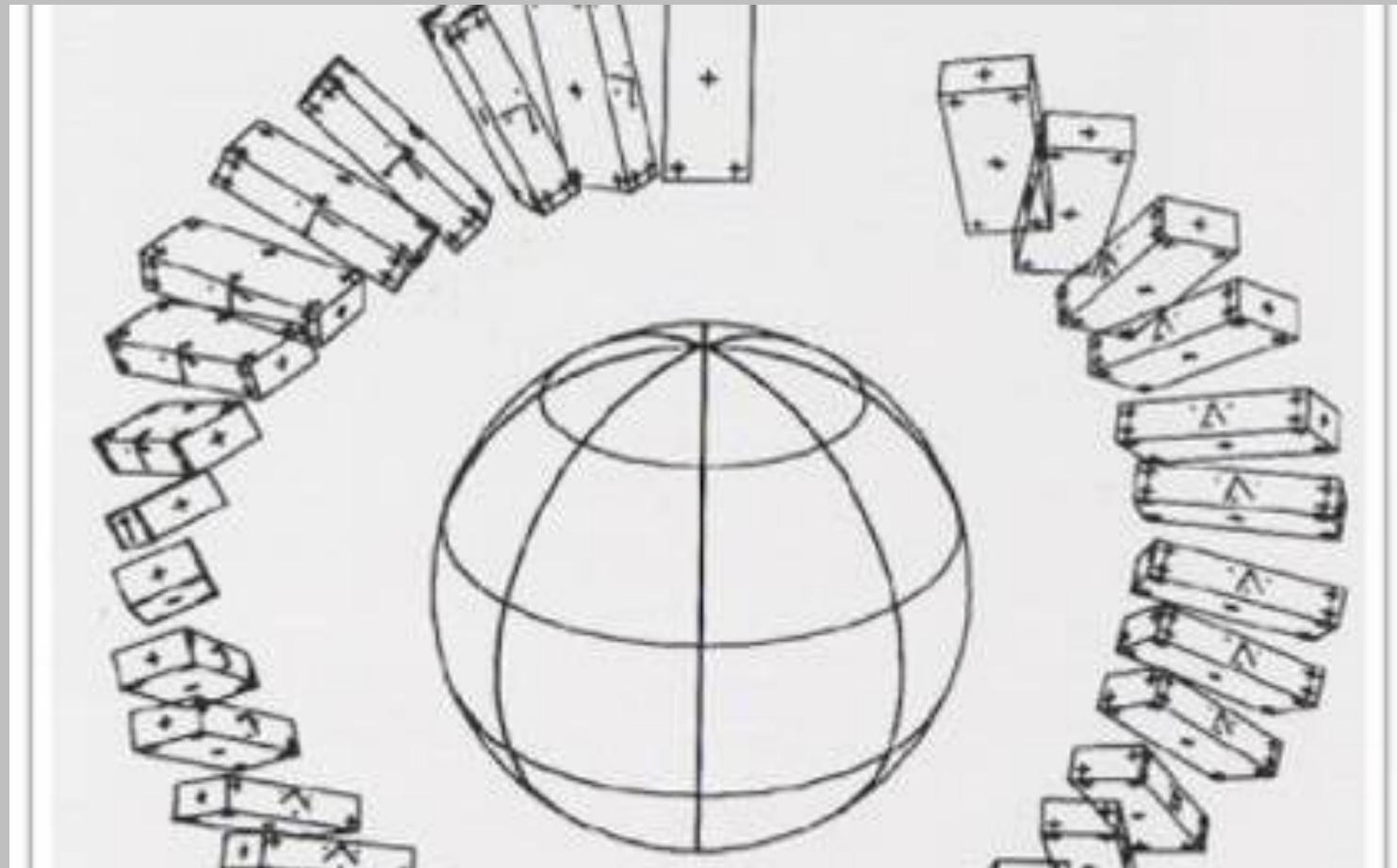
- 1963 – La souris



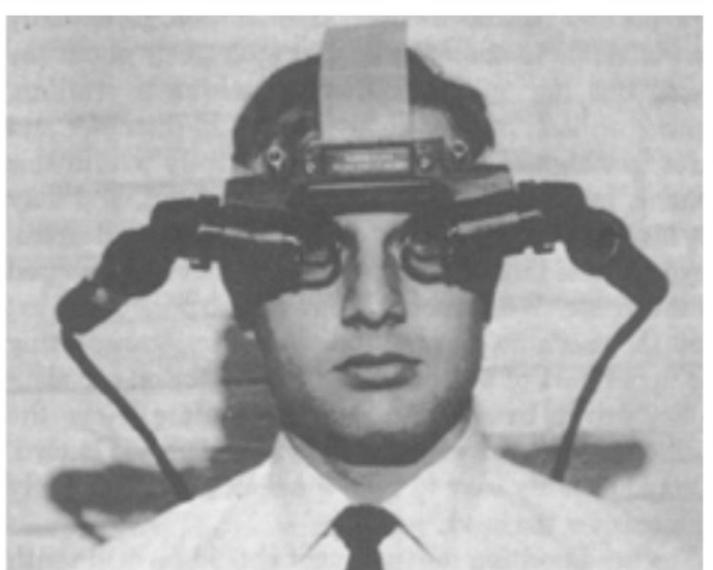
- 1963 - Sketchpad: premier logiciel de CAO



- 1963 – premier film généré par ordinateur



- 1968 – HMD par Sutherland



- 1971 – Ombrage de Gouraud



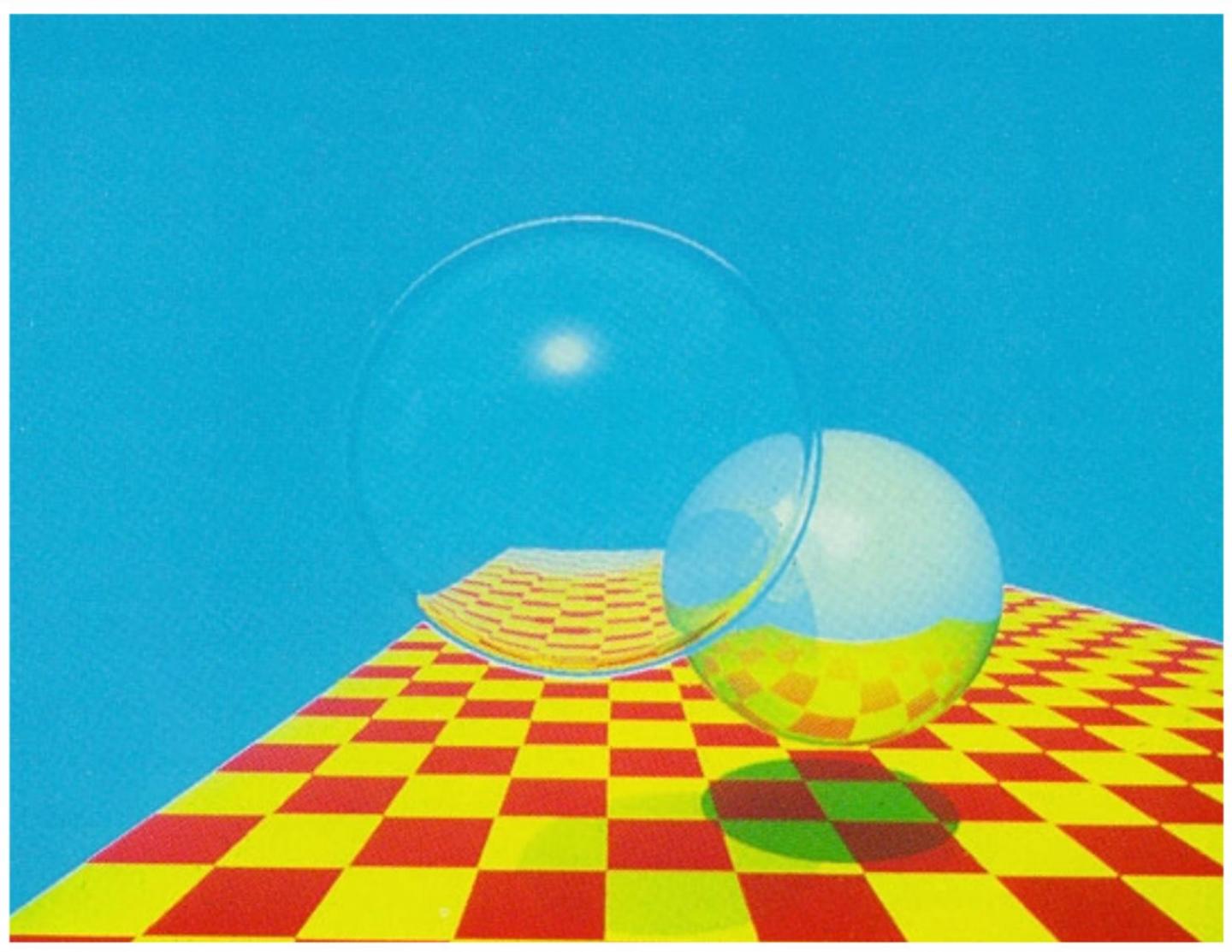
- 1972 – premier film avec rendu ombré par Ed Catmull



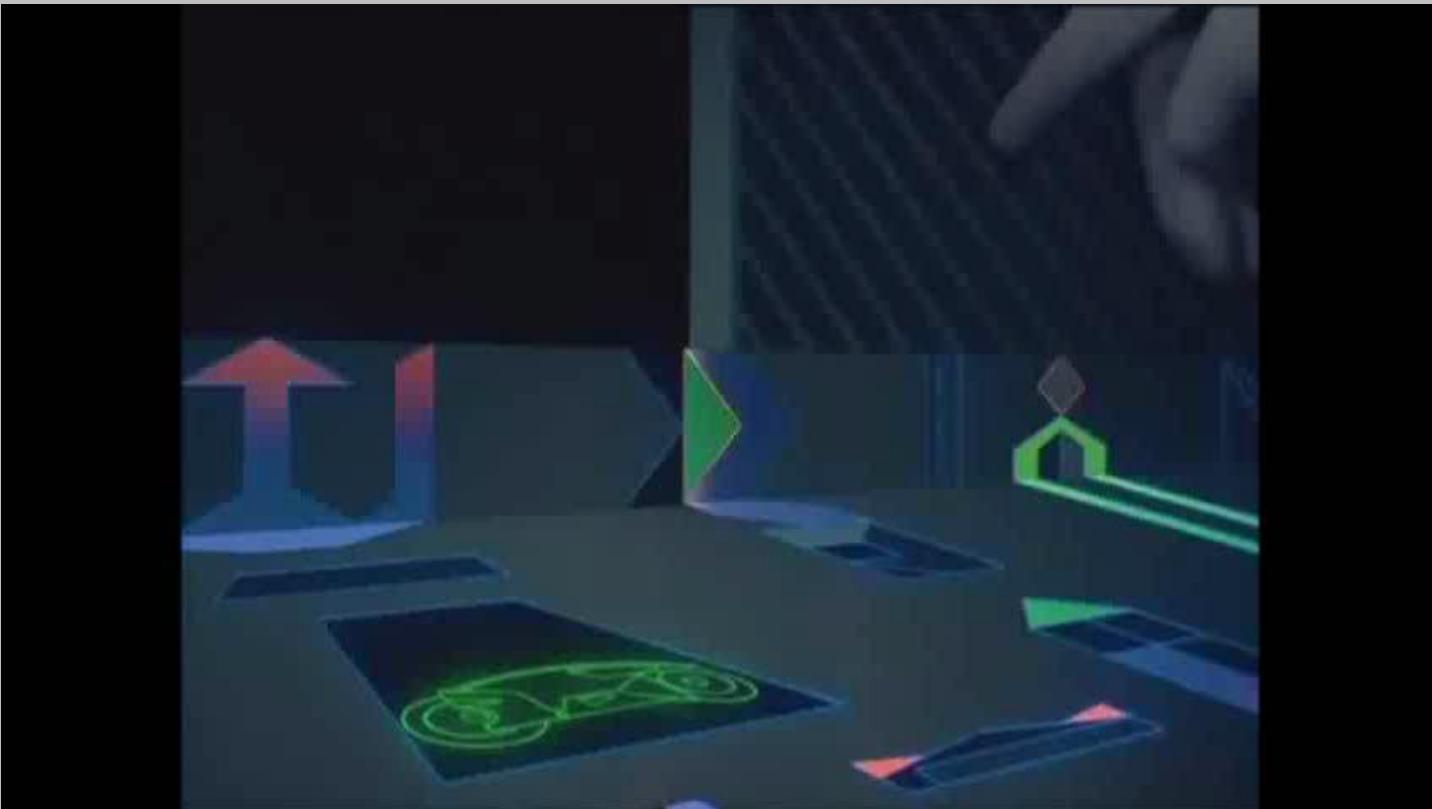
- 1976 – Environment mapping par J. Blinn



- 1980 – Lancer de rayon - Turner Whitted



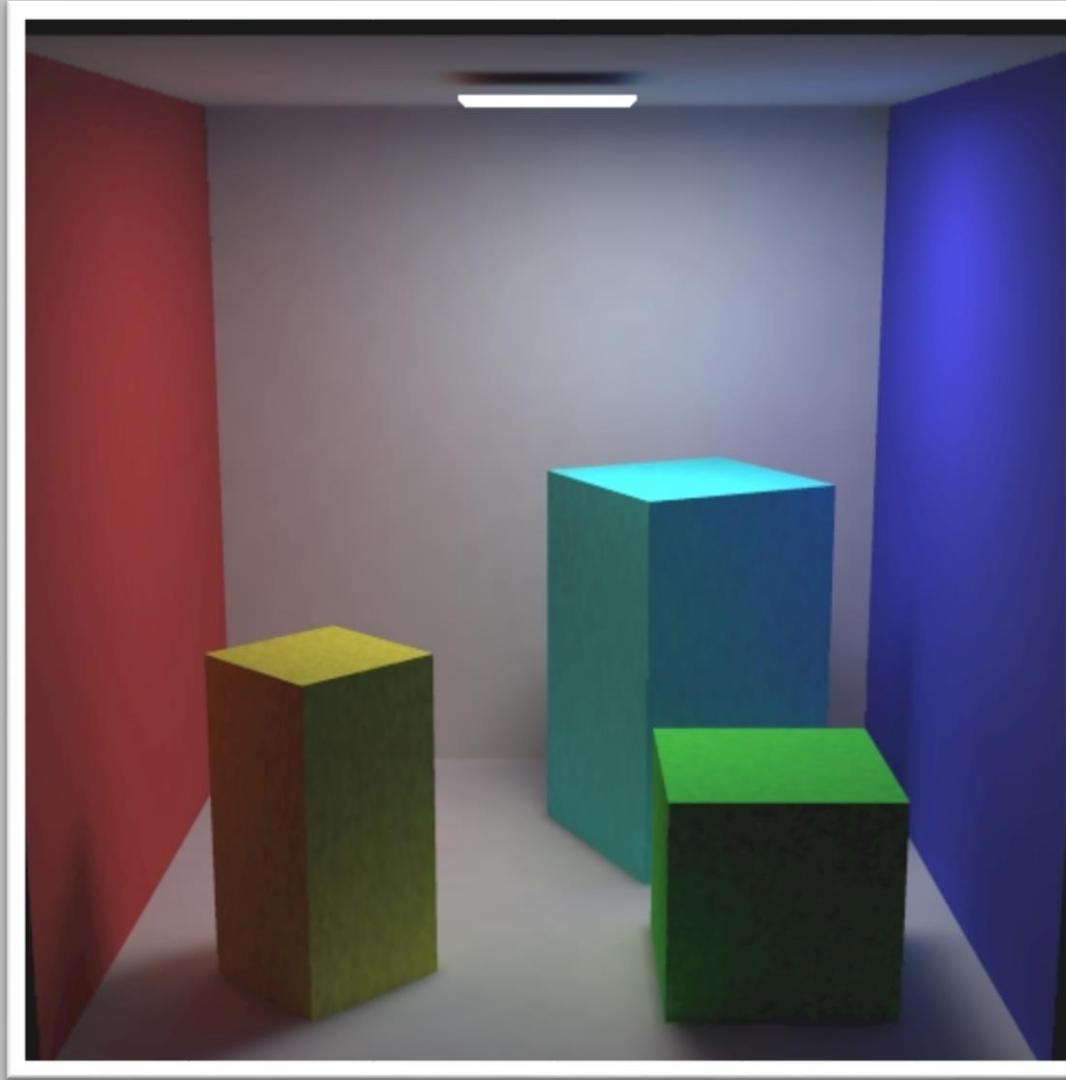
- 1980 – Film Tron



- 1982 – Première intégration réel/virtuel utilisant l'environnement mapping - Gene Miller



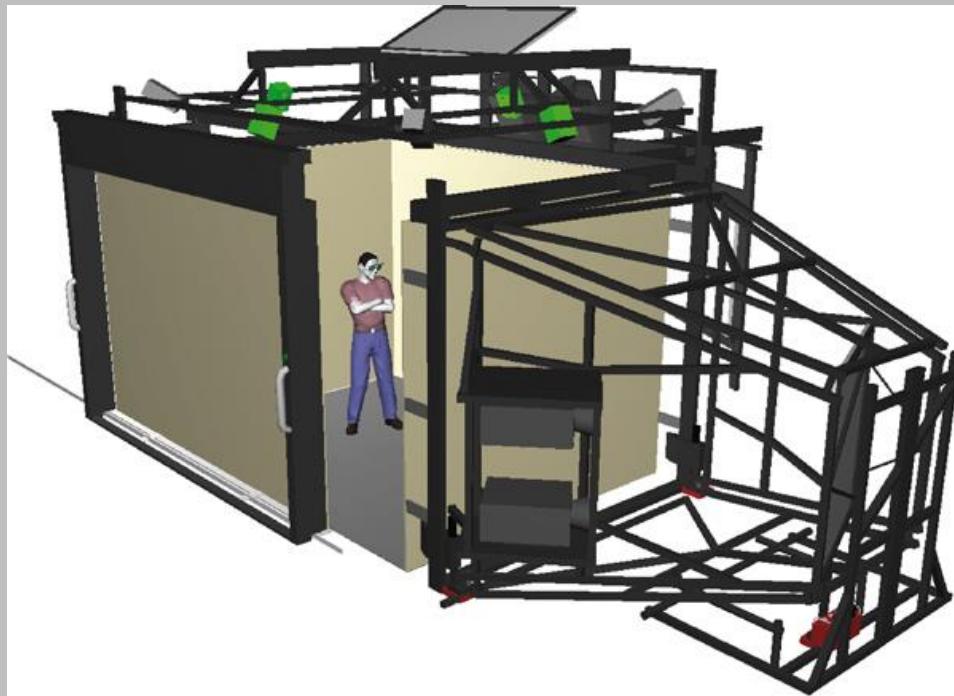
- 1984 – Radiosité - Goral



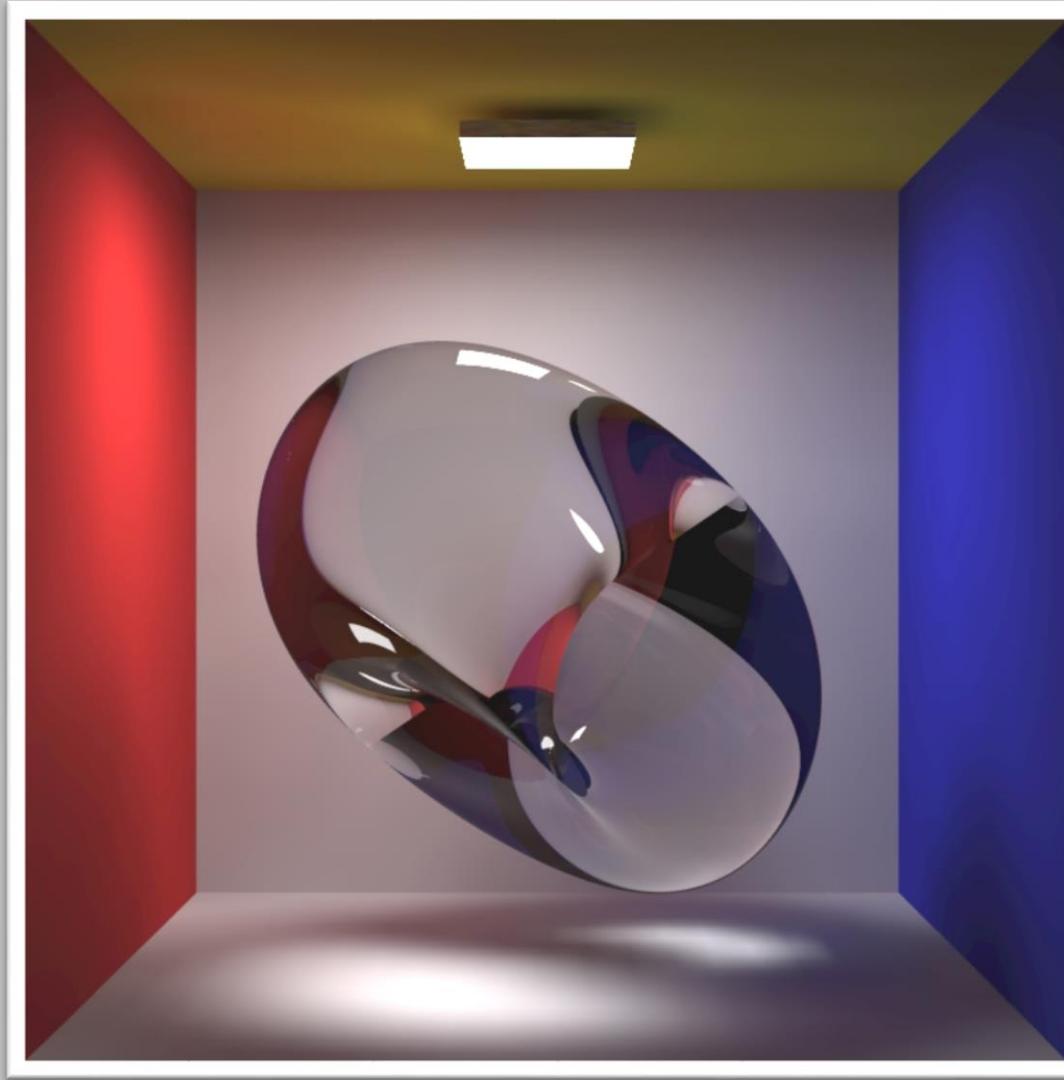
- 1984 – Motion blur



- 1992 – CAVE



- 1996 – Photon mapping – E.W. Jensen

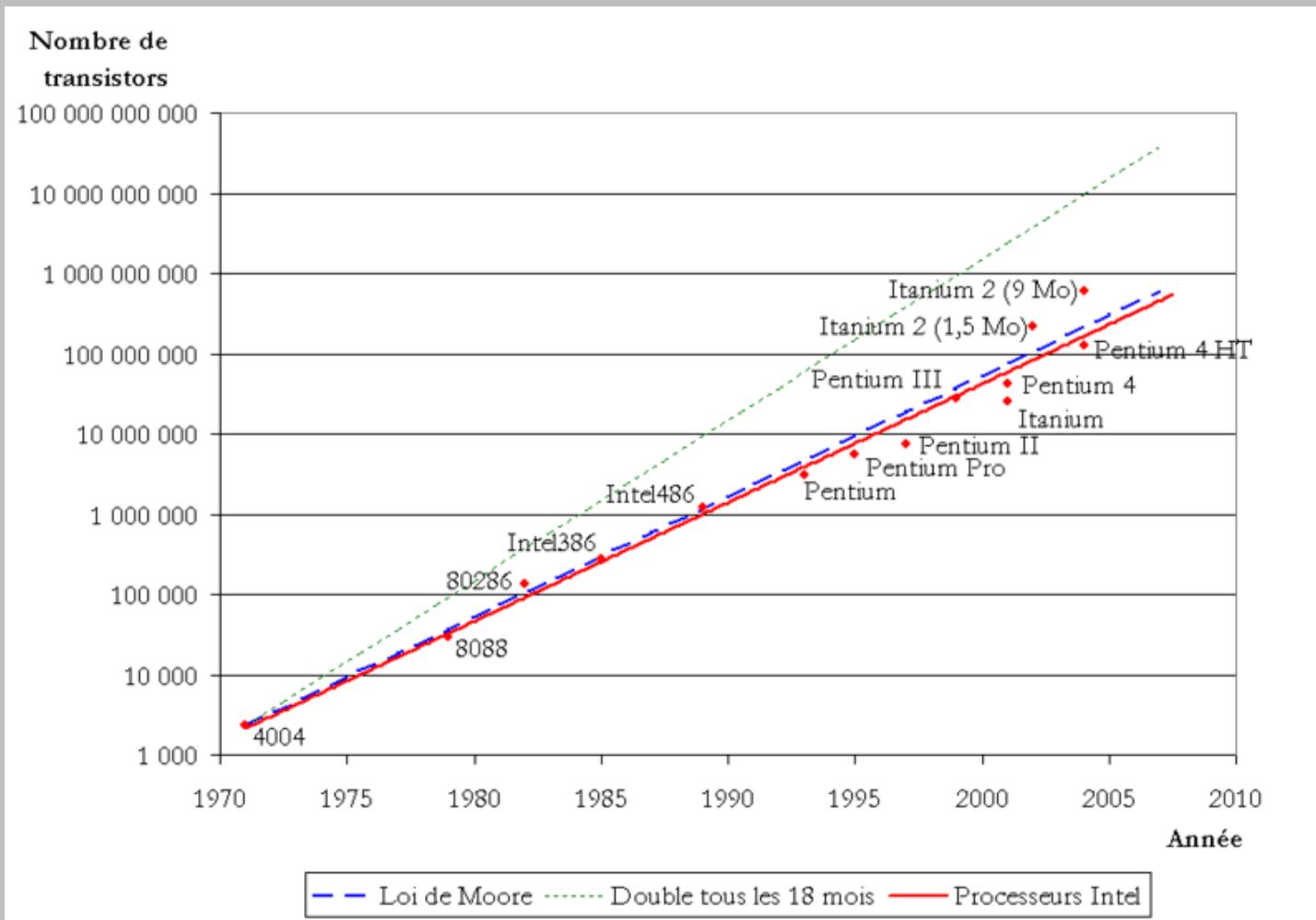


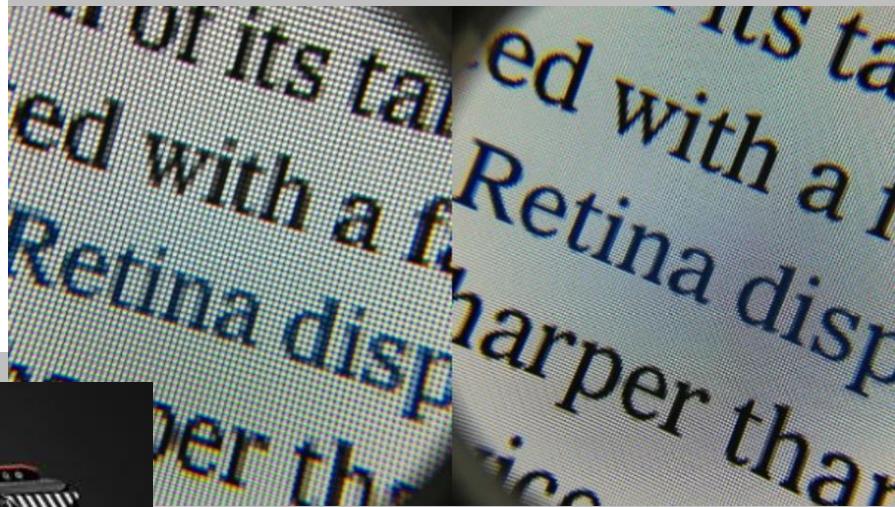
- 2001 – Subsurface Scattering – E.W. Jensen



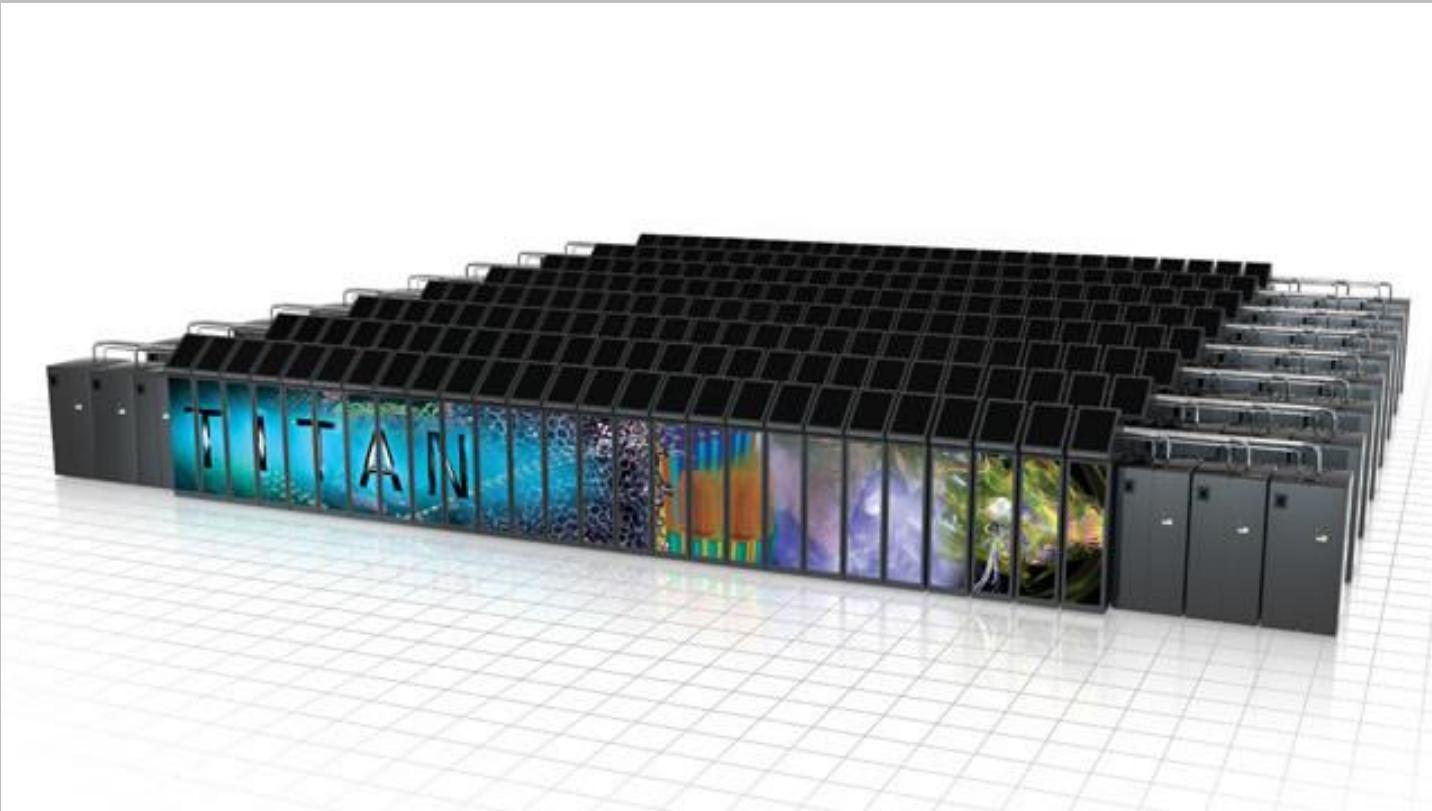
# Materiel

# • Loie de Moore



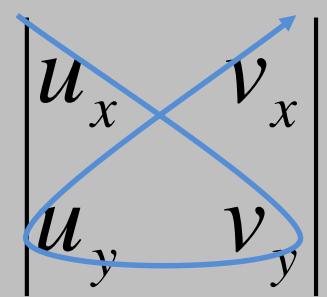


- Super calculateurs



# Mathématiques

- Déterminants 2x2

$$\det(\vec{u}, \vec{v}) = \begin{vmatrix} u_x & v_x \\ u_y & v_y \end{vmatrix} = u_x v_y - u_y v_x$$
A diagram showing two vectors, u and v, originating from the same point. Vector u has components u\_x and u\_y, and vector v has components v\_x and v\_y. A parallelogram is formed by these vectors. The area of this parallelogram is shaded in light blue. The formula for the determinant of the vectors is shown as the area of this parallelogram.

- Déterminants 3x3

$$\det(\vec{u}, \vec{v}, \vec{w}) = \begin{vmatrix} u_x & v_x & w_x \\ u_y & v_y & w_y \\ u_z & v_z & w_z \end{vmatrix} = \begin{bmatrix} u_x & v_x & w_x \\ u_y & v_y & w_y \\ u_z & v_z & w_z \end{bmatrix} \begin{array}{c} u_x \\ u_y \\ u_z \end{array} \begin{array}{c} v_x \\ v_y \\ v_z \end{array} \begin{array}{c} w_x \\ w_y \\ w_z \end{array}$$

$$= u_x v_y w_z + v_x w_y u_z + w_x u_y v_z - w_x v_y u_z - u_x w_y v_z - v_x u_y w_z$$

- Produit Scalaire

$$\vec{u} \cdot \vec{v} = |\vec{u}| |\vec{v}| \cos(\theta)$$

$$\vec{u} \cdot \vec{v} = u_x v_x + u_y v_y + u_z v_z$$

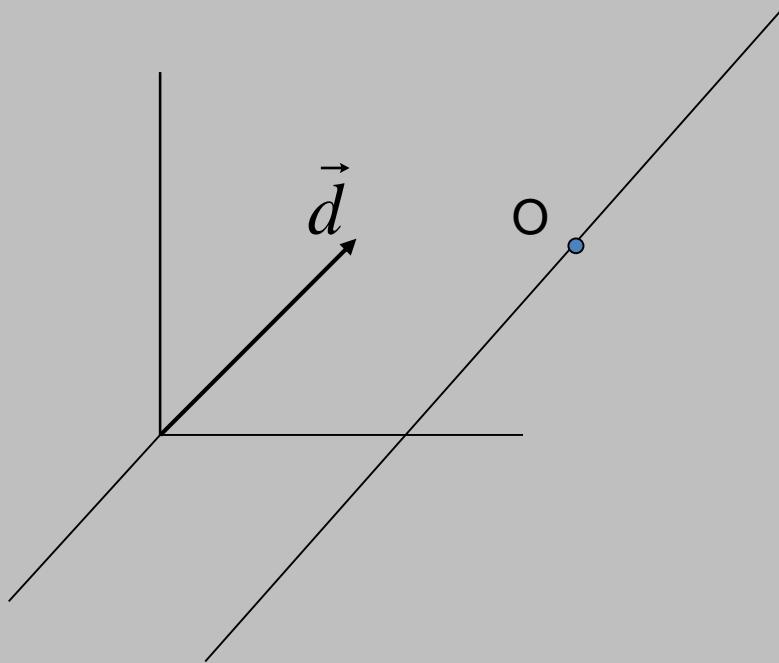
- Produit Vectoriel

$$|\vec{u} \wedge \vec{v}| = |\vec{u}| |\vec{v}| \sin(\theta)$$

$$\vec{u} \wedge \vec{v} = \left( \begin{vmatrix} u_y & v_y \\ u_z & v_z \end{vmatrix}, \begin{vmatrix} u_z & v_z \\ u_x & v_x \end{vmatrix}, \begin{vmatrix} u_x & v_x \\ u_y & v_y \end{vmatrix} \right)$$

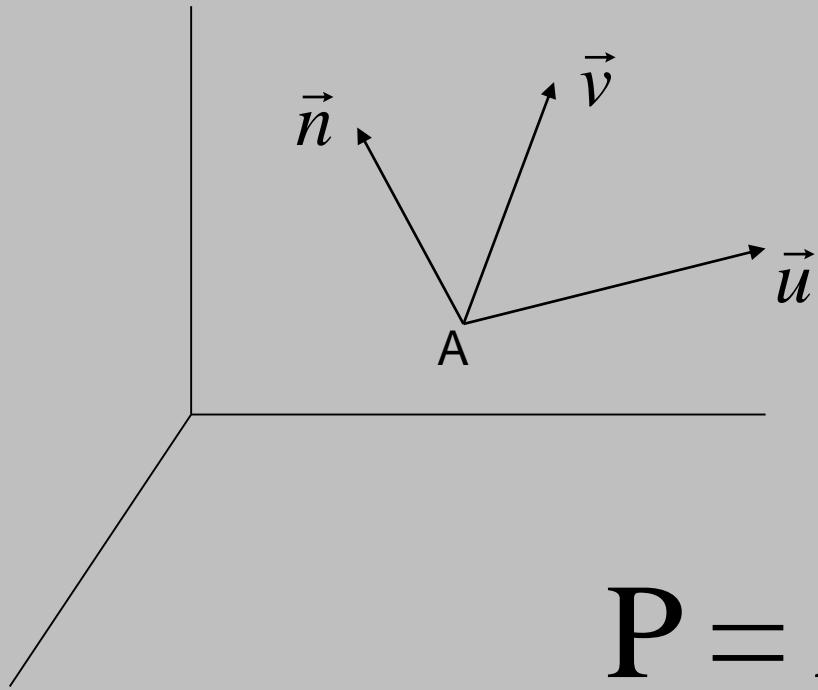
$$\vec{u} \wedge \vec{v} = (u_y v_z - u_z v_y, u_z v_x - u_x v_z, u_x v_y - u_y v_x)$$

- Droite et Plan



$$P = O + t\vec{d}$$

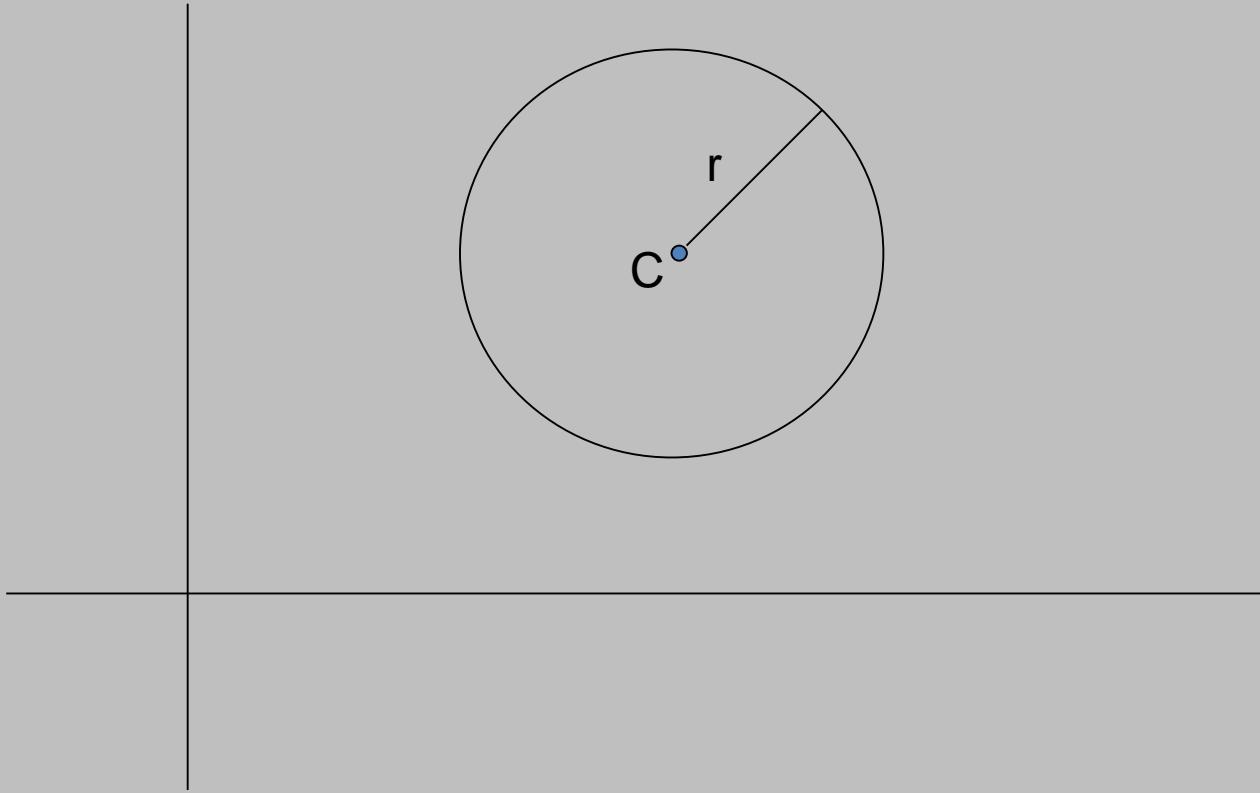
- Droite et Plan



$$P = A + \alpha \vec{u} + \beta \vec{v}$$

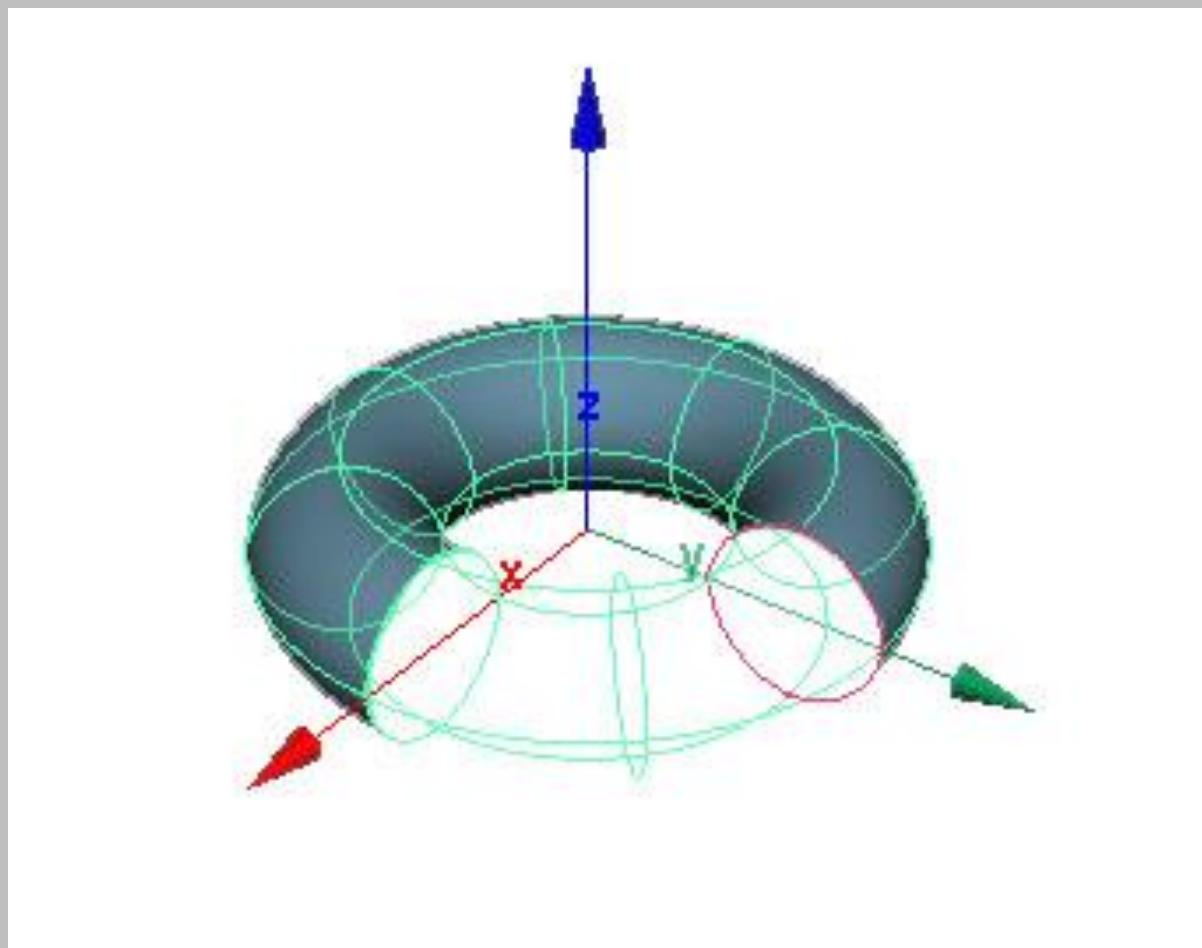
$$(P - A) \cdot \vec{n} = 0$$

- Sphère

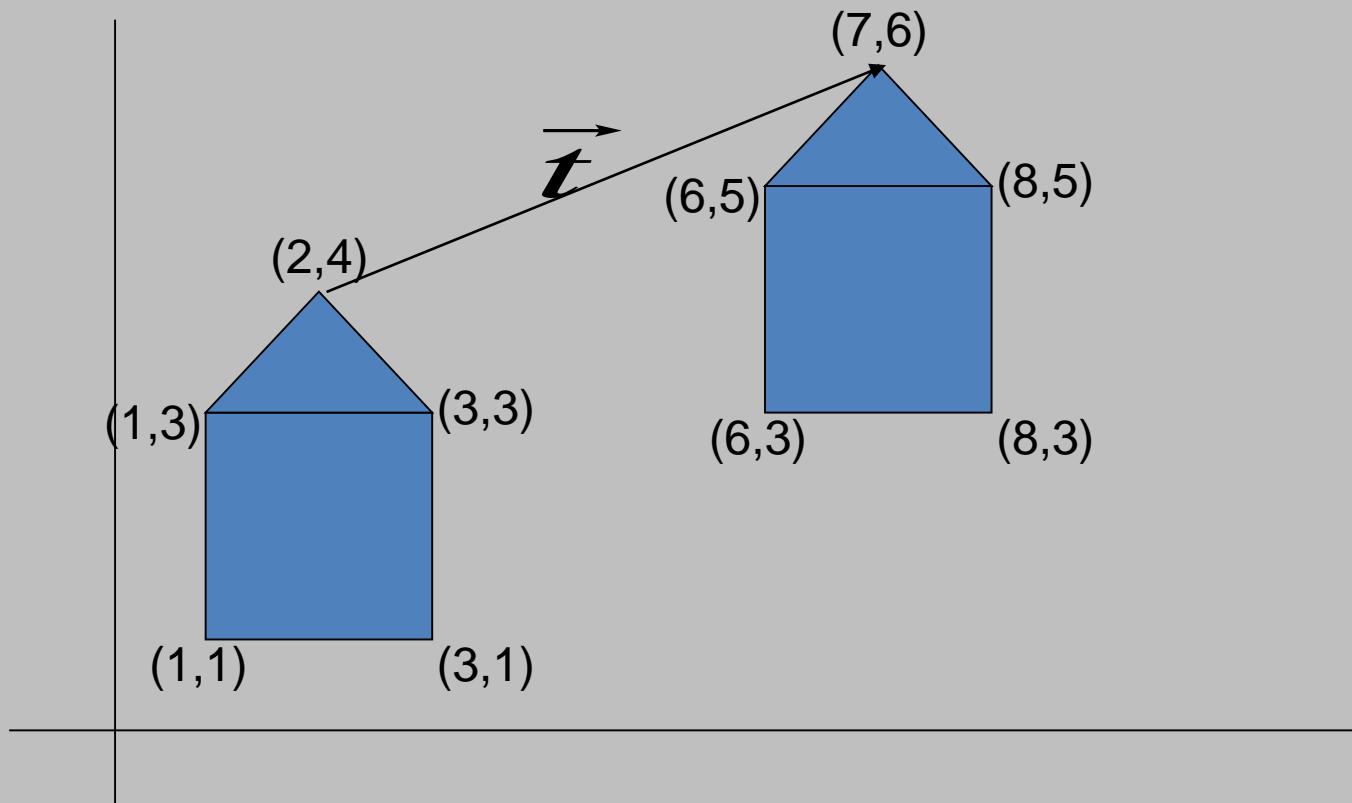


$$(P - C)^2 - r^2 = 0$$

- Tore



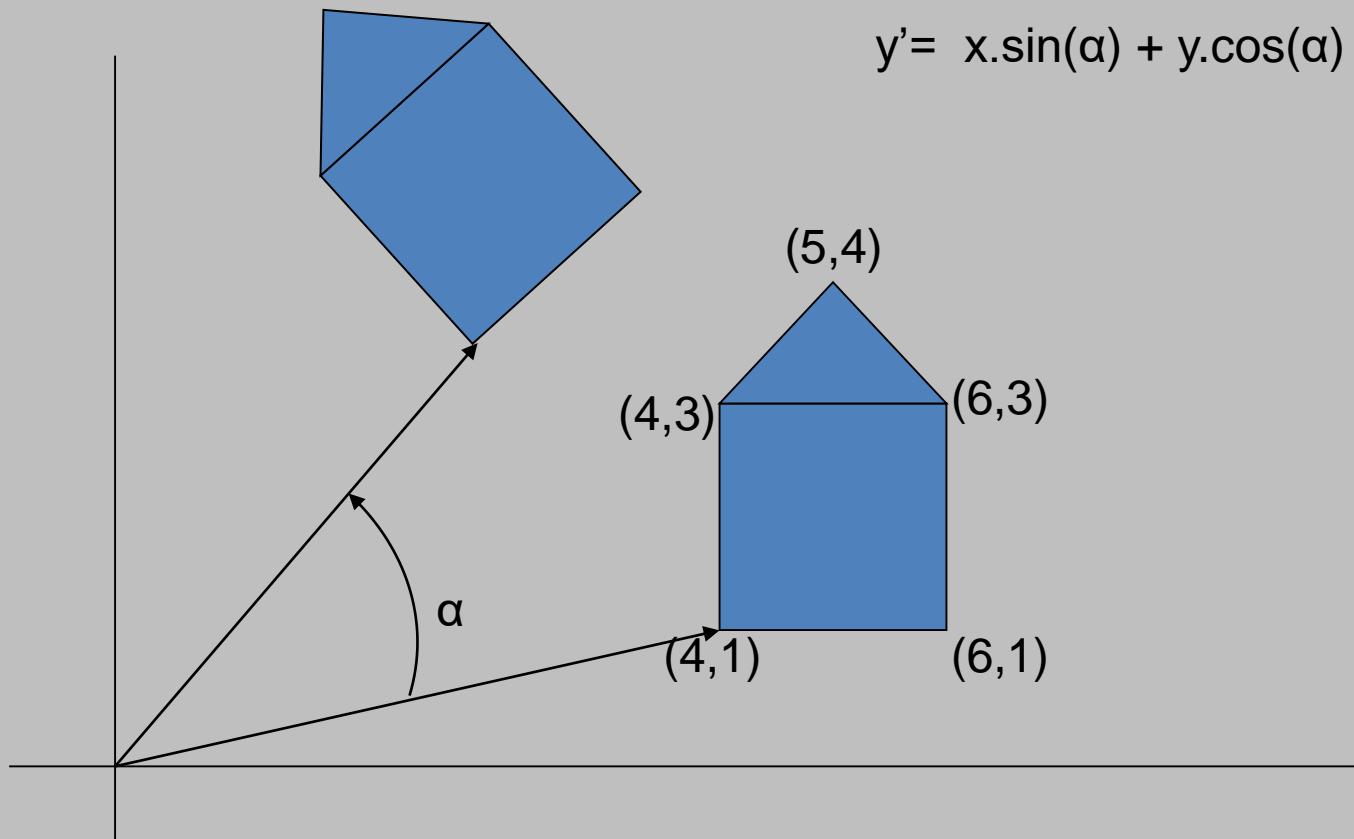
- Translation



- Rotation

$$x' = x \cdot \cos(\alpha) - y \cdot \sin(\alpha)$$

$$y' = x \cdot \sin(\alpha) + y \cdot \cos(\alpha)$$



- N équations à N inconnues

$$\left\{ \begin{array}{l} a_{1,1}x_1 + a_{1,2}x_2 + \dots + a_{1,n}x_n = \lambda_1 \\ a_{2,1}x_1 + a_{2,2}x_2 + \dots + a_{2,n}x_n = \lambda_2 \\ \vdots \\ a_{n,1}x_1 + a_{n,2}x_2 + \dots + a_{n,n}x_n = \lambda_n \end{array} \right.$$

$$\begin{pmatrix} a_{1,1} & a_{1,2} & \cdots & a_{1,n} \\ a_{2,1} & a_{2,2} & \cdots & a_{2,n} \\ \vdots & \vdots & \ddots & \vdots \\ a_{n,1} & a_{n,2} & \cdots & a_{n,n} \end{pmatrix} \times \begin{pmatrix} x_1 \\ x_2 \\ \vdots \\ x_n \end{pmatrix} = \begin{pmatrix} \lambda_1 \\ \lambda_2 \\ \vdots \\ \lambda_n \end{pmatrix} \Leftrightarrow A \cdot X = \Lambda$$

$$x_k = \frac{\det(A_k)}{\det(A)}$$

Lumière



Gamma
Rayons X
UV
IR
Micro-ondes
Télévision
Radio
Radar

Spectre complet

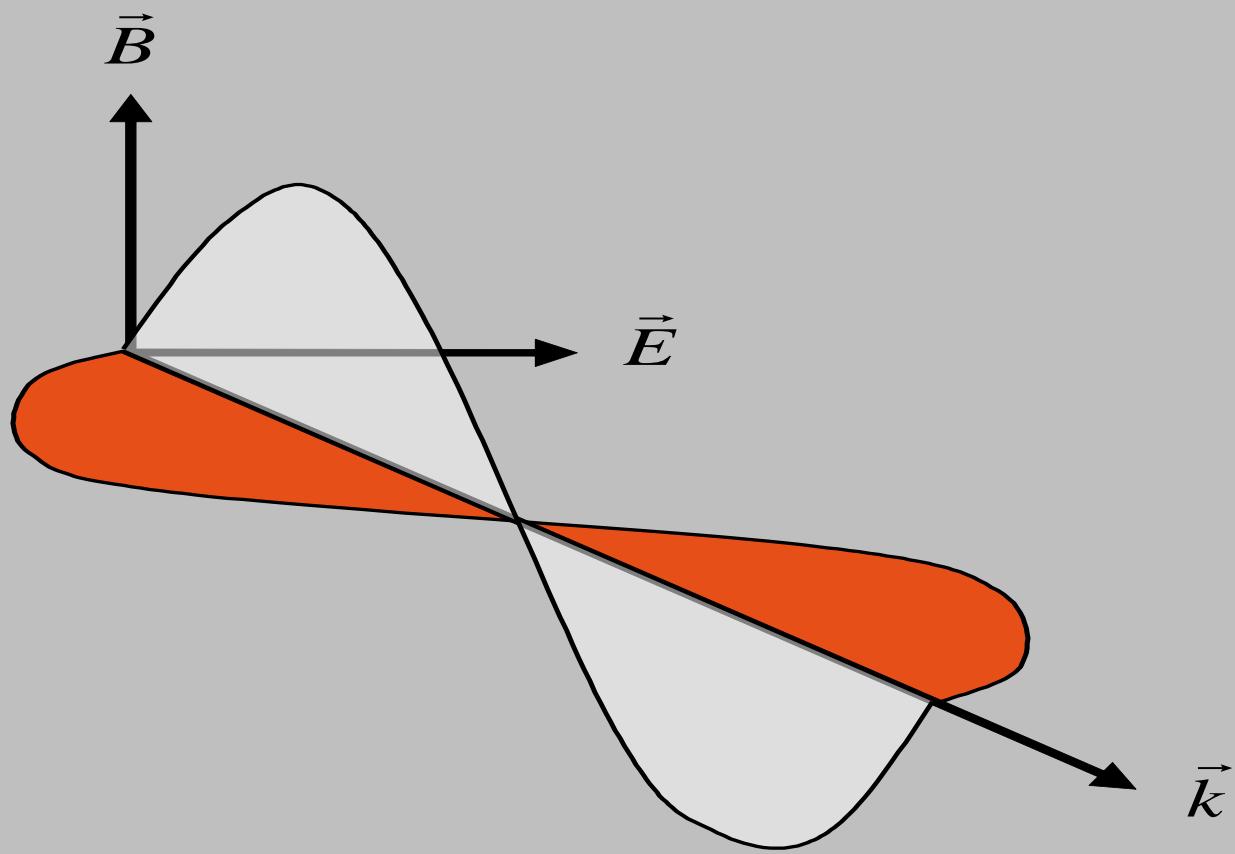


380 nm



780 nm

Spectre visible



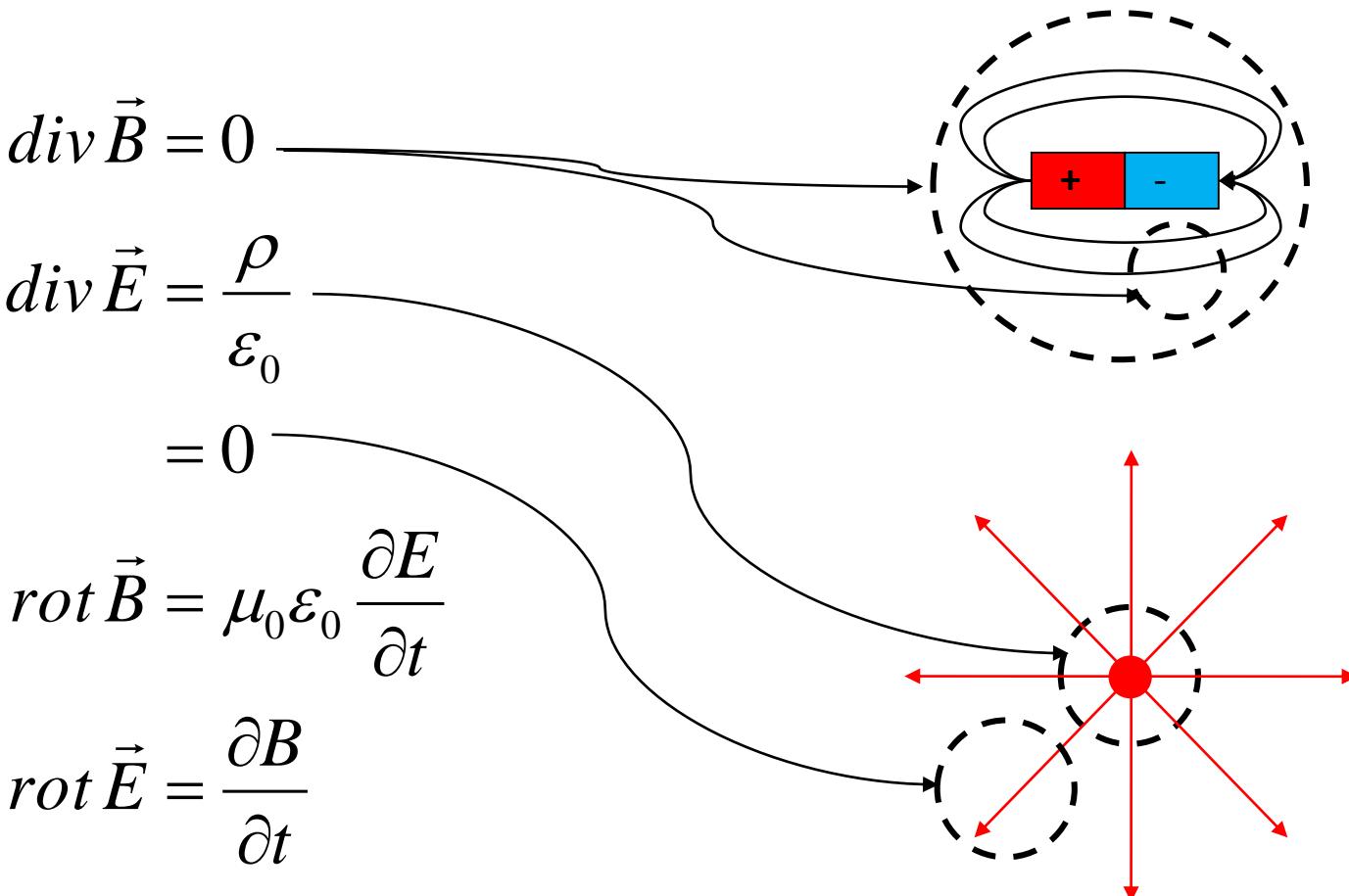
$$\operatorname{div} \vec{B} = 0$$

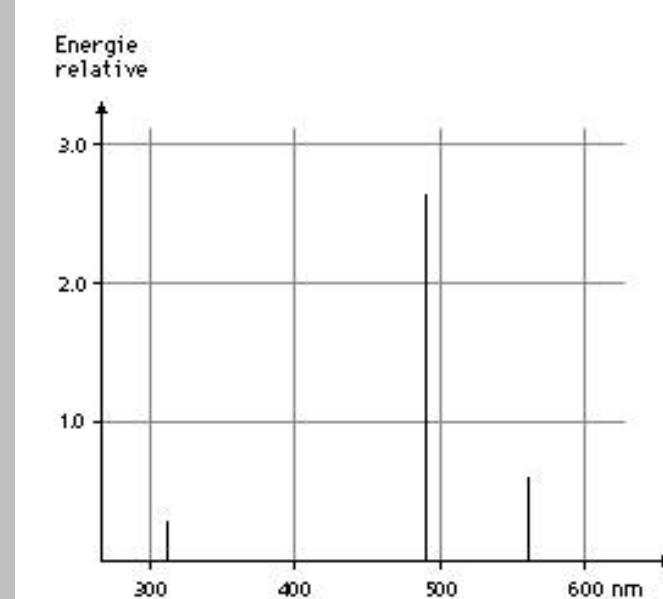
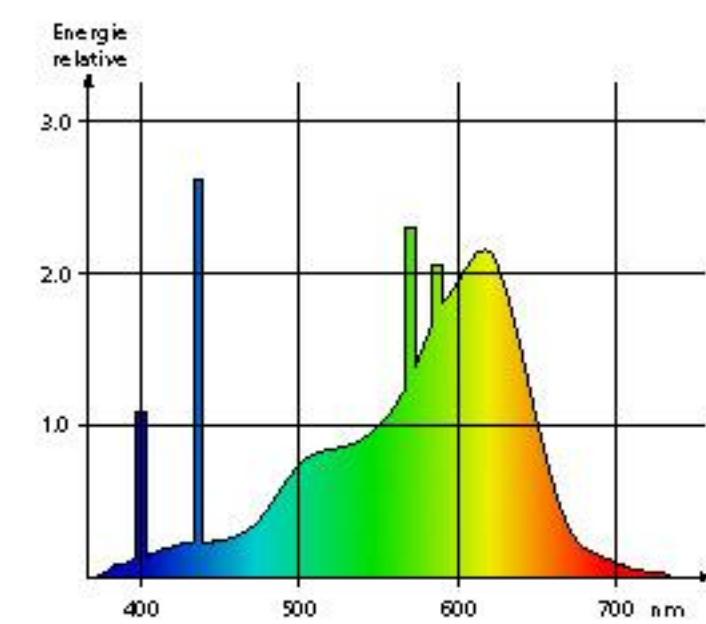
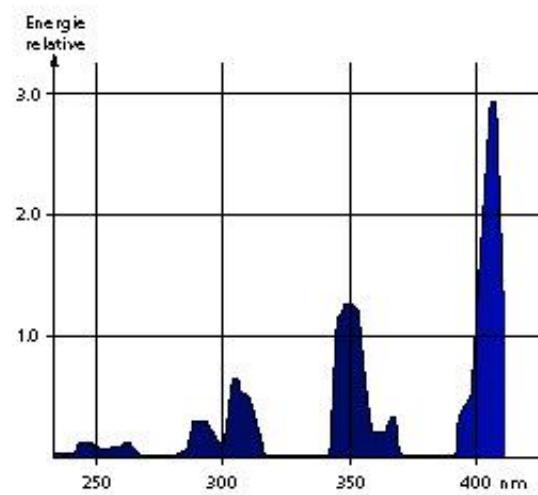
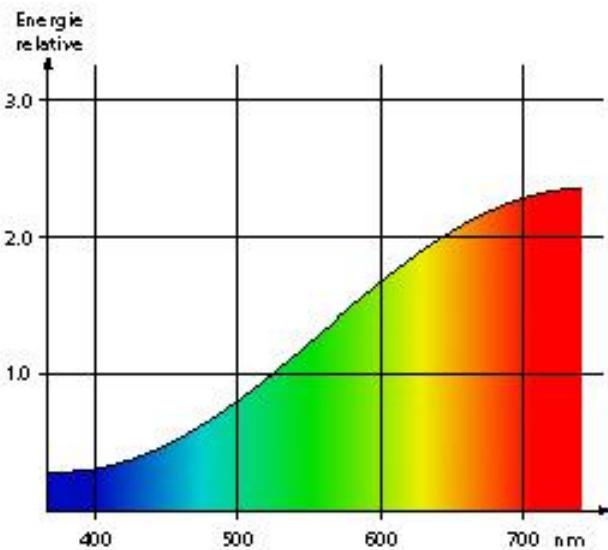
$$\operatorname{div} \vec{E} = \frac{\rho}{\epsilon_0}$$

$$= 0$$

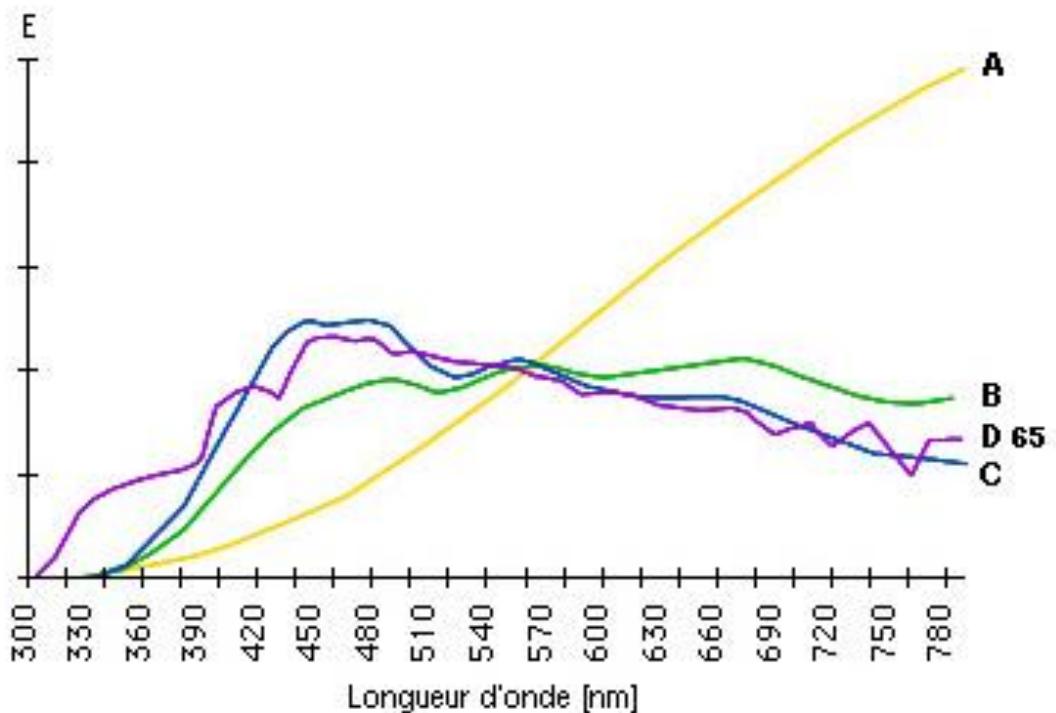
$$\operatorname{rot} \vec{B} = \mu_0 \epsilon_0 \frac{\partial E}{\partial t}$$

$$\operatorname{rot} \vec{E} = \frac{\partial B}{\partial t}$$





## Illuminants normalisés



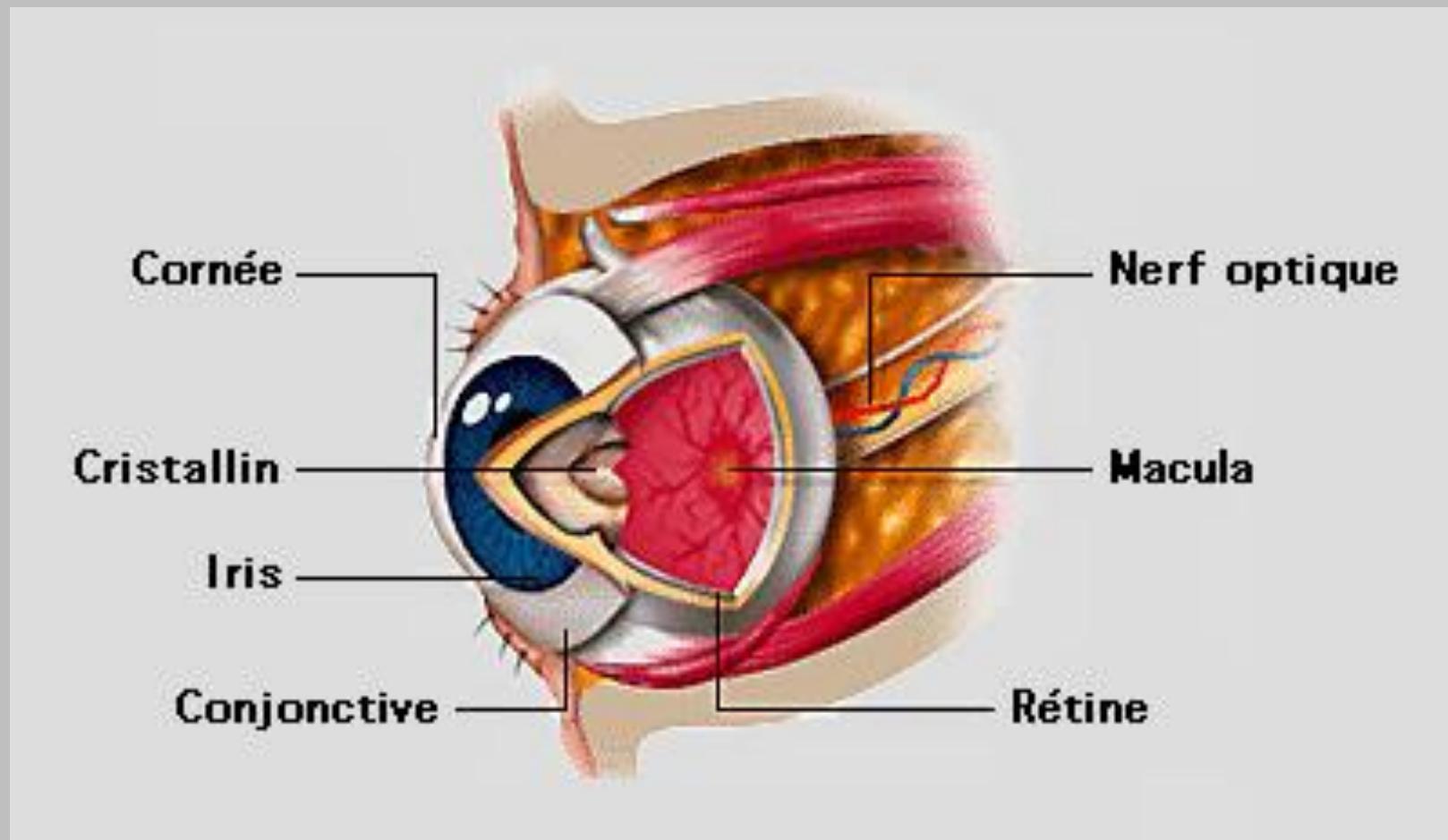
Incandescence (2856 K)

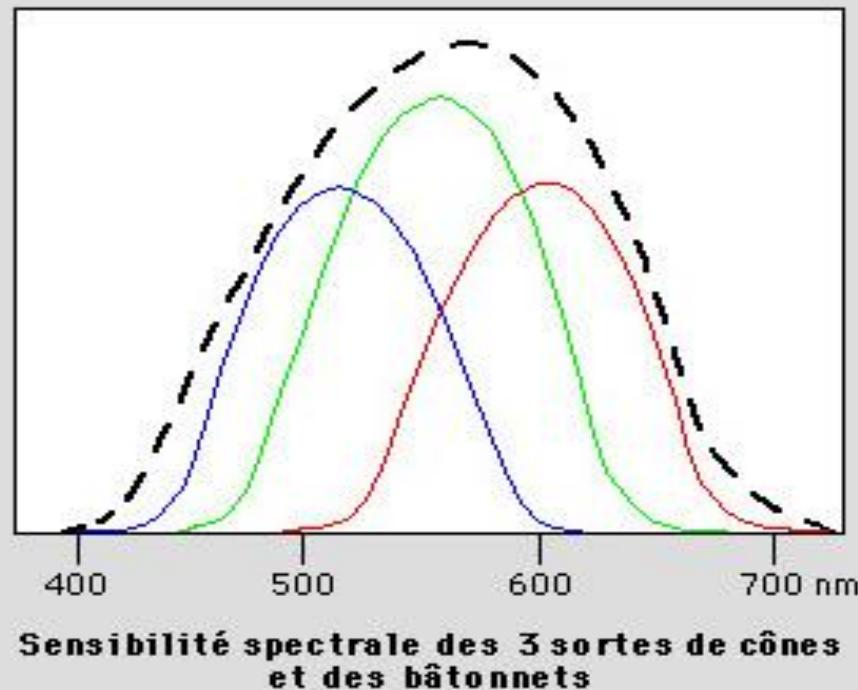
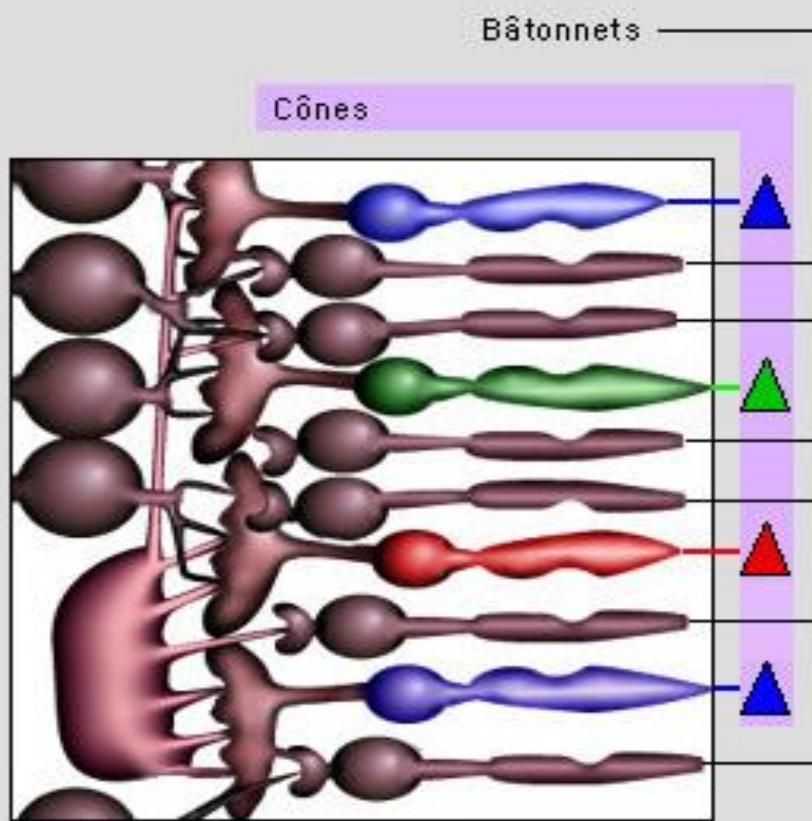
Soleil direct (4874 K)

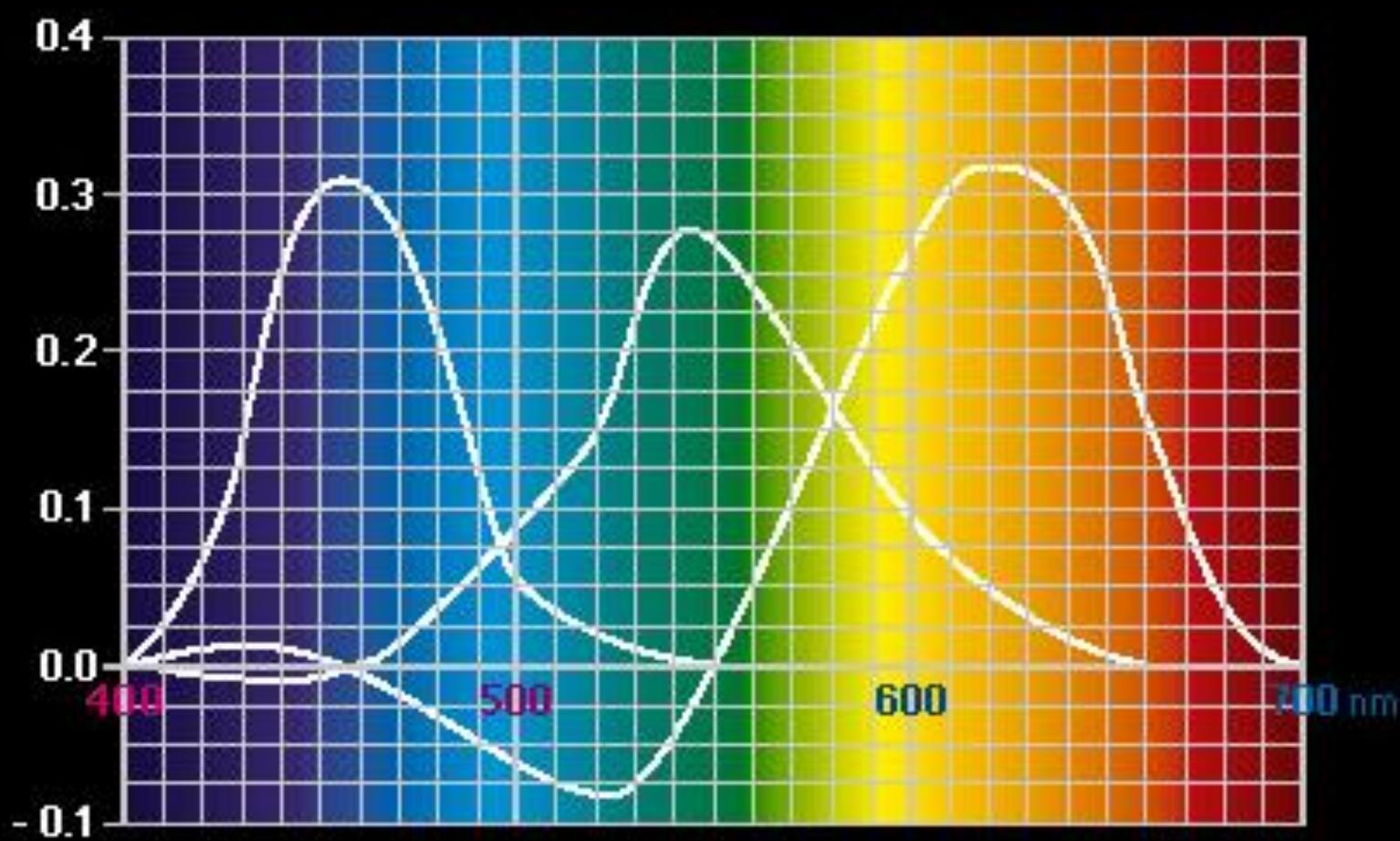
Jour moyen, sans UV (6774 K)

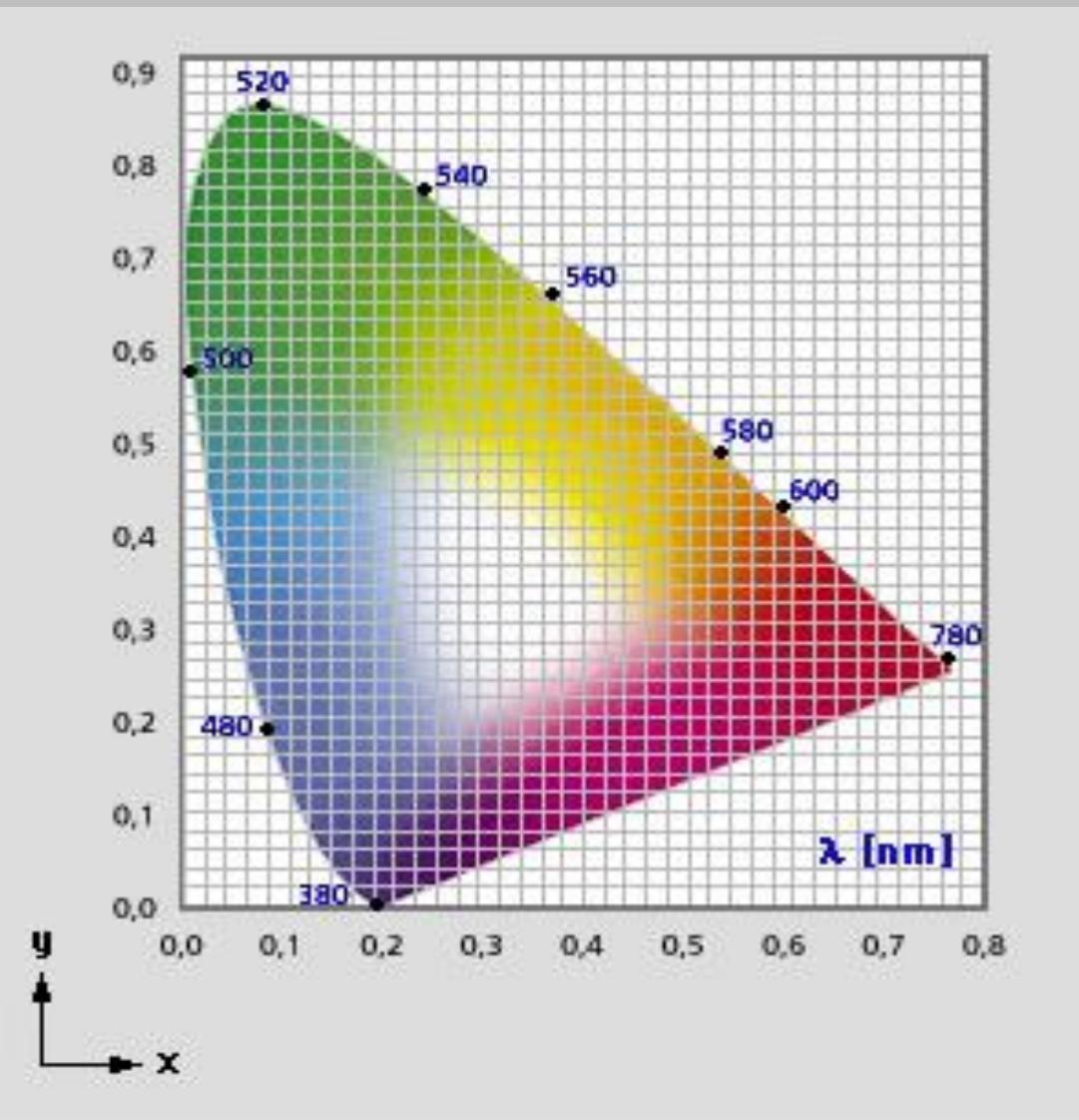
Jour moyen, avec UV (6504 K)

# Couleur

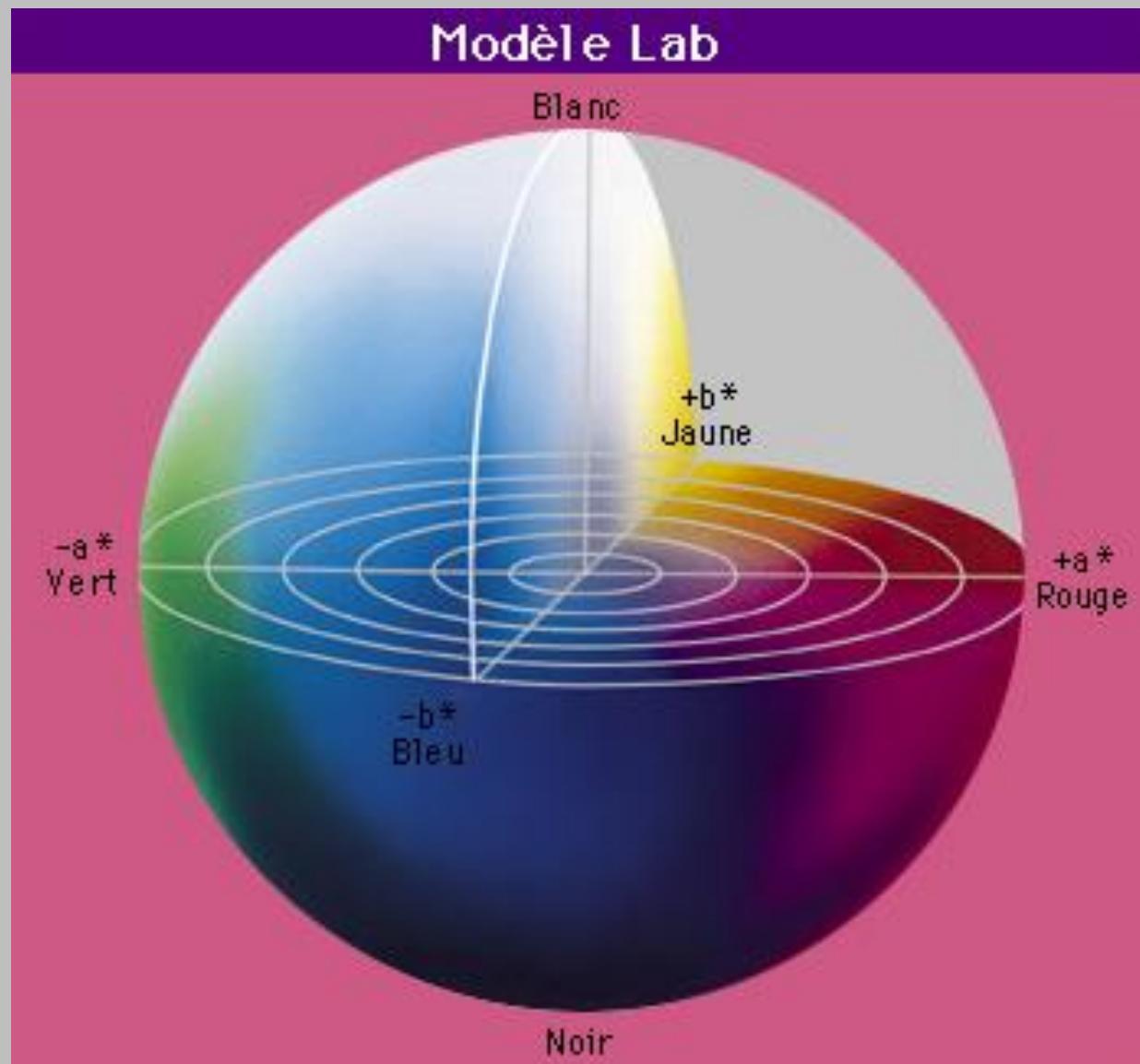


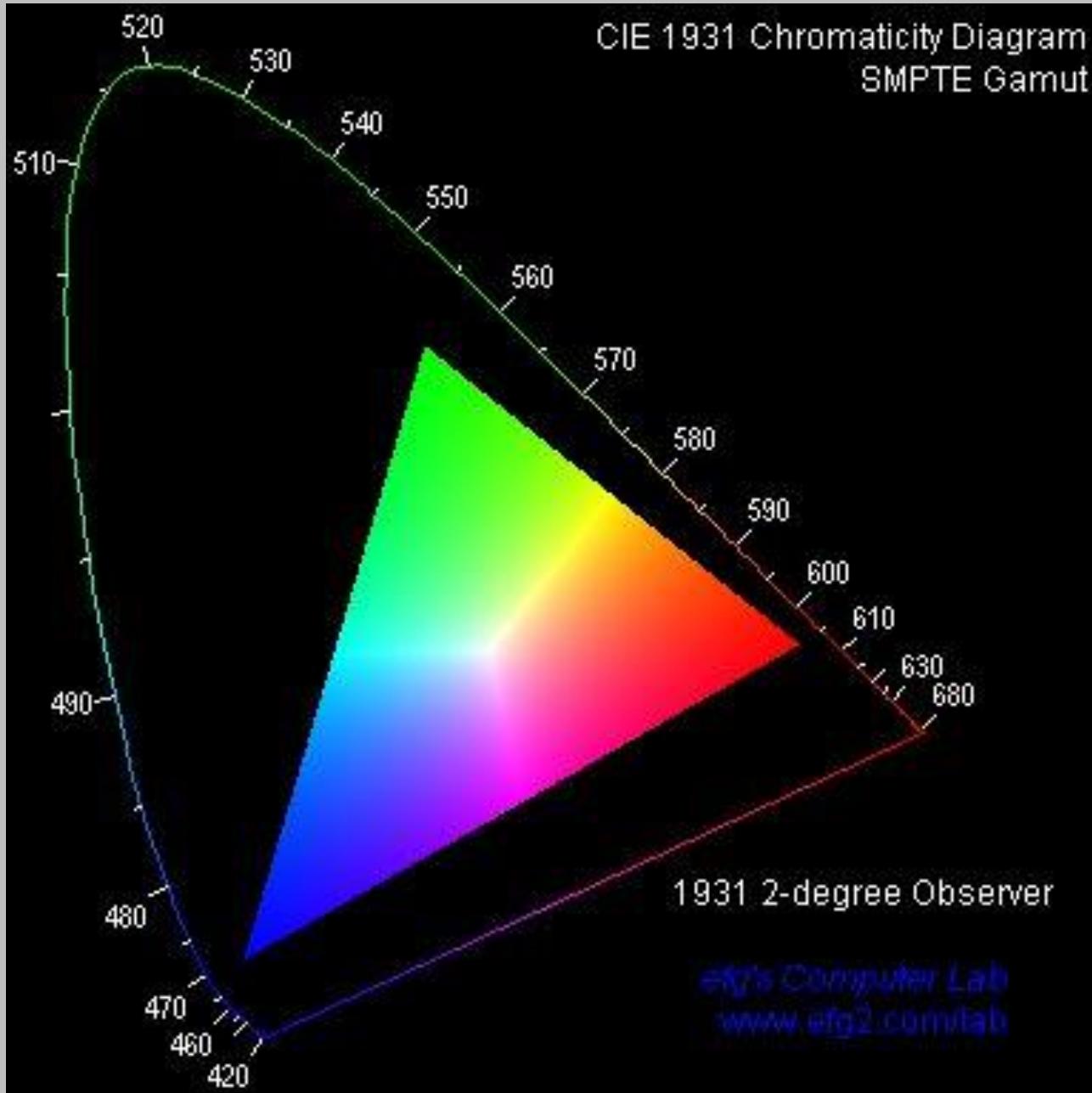






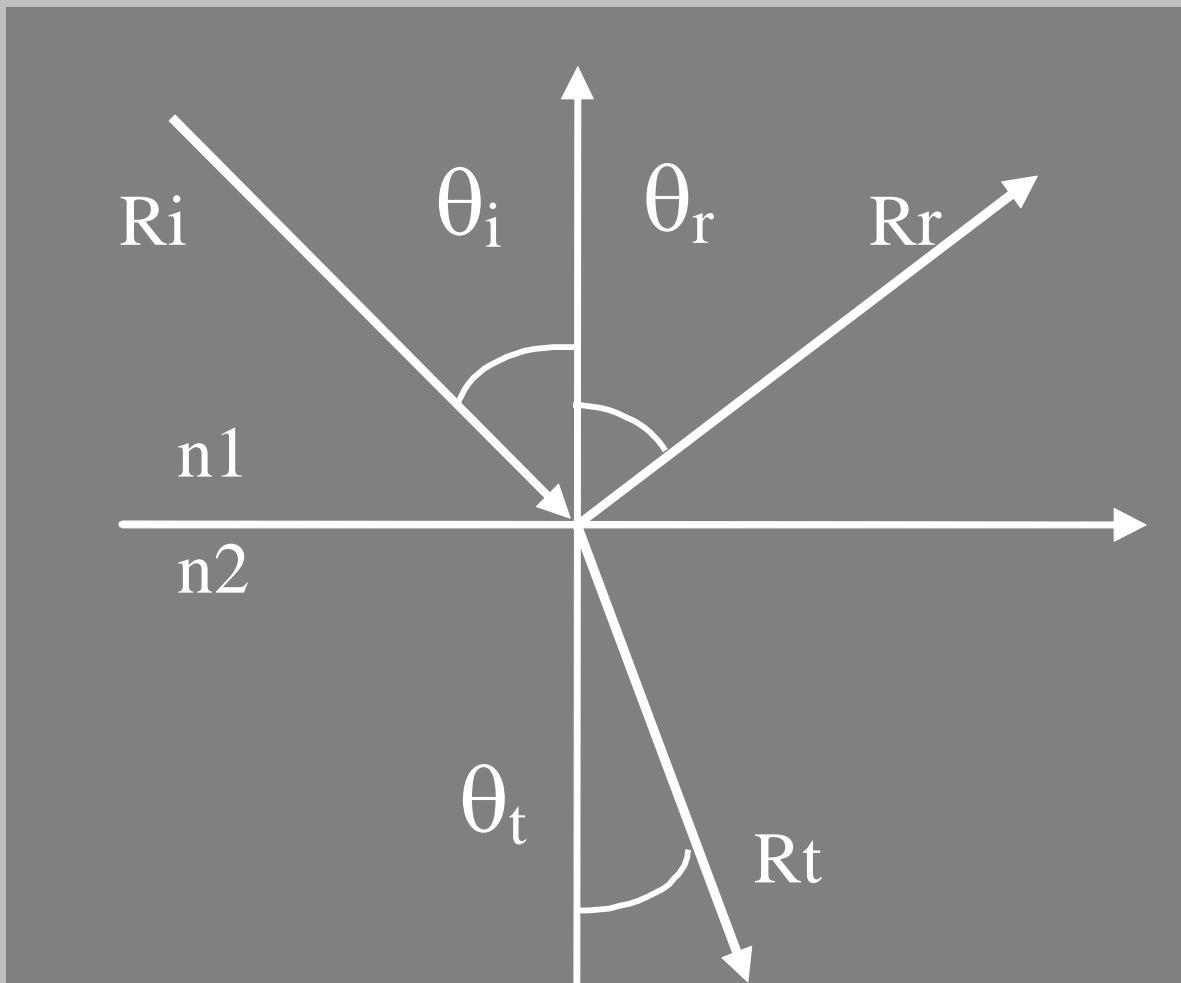
## Modèle Lab

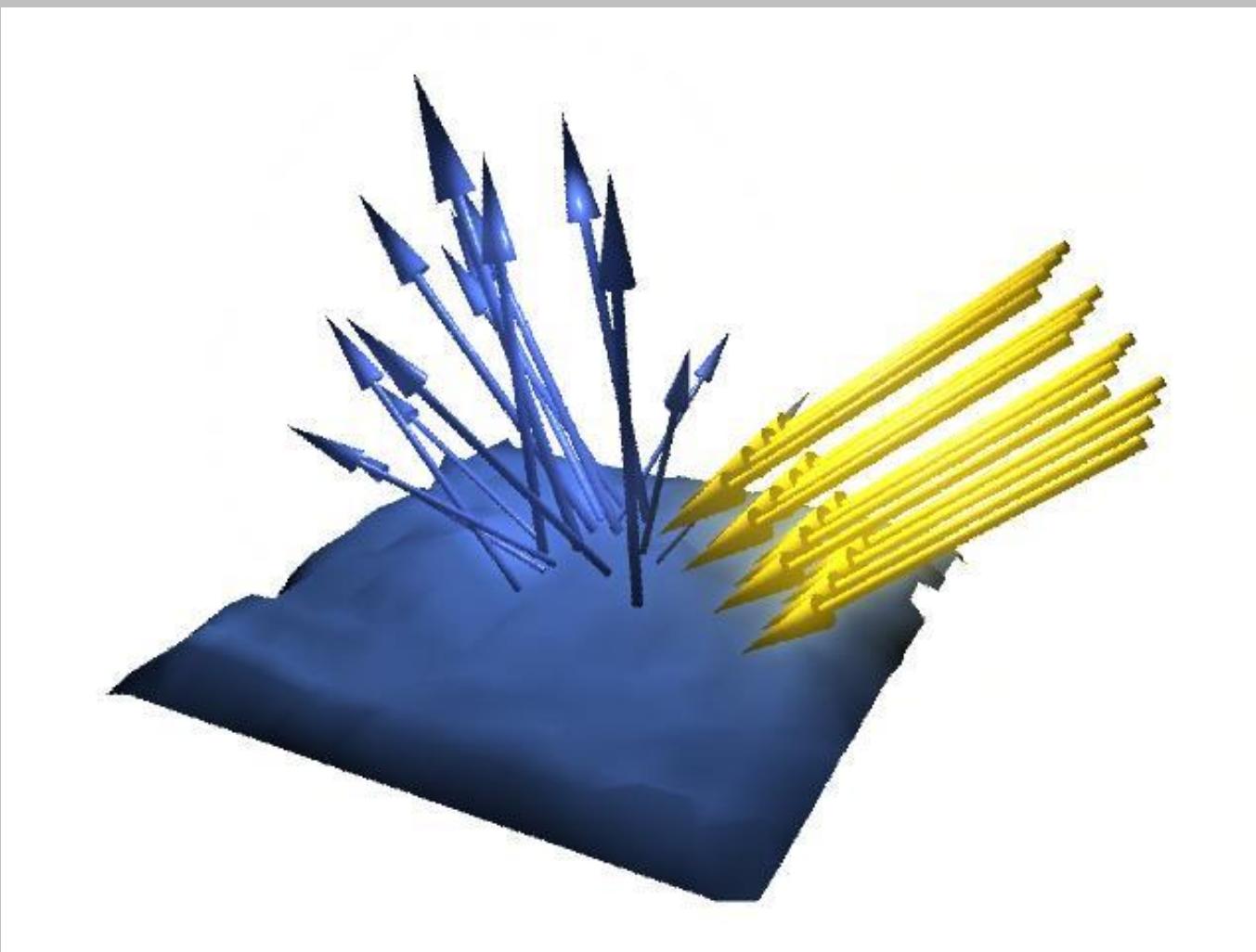


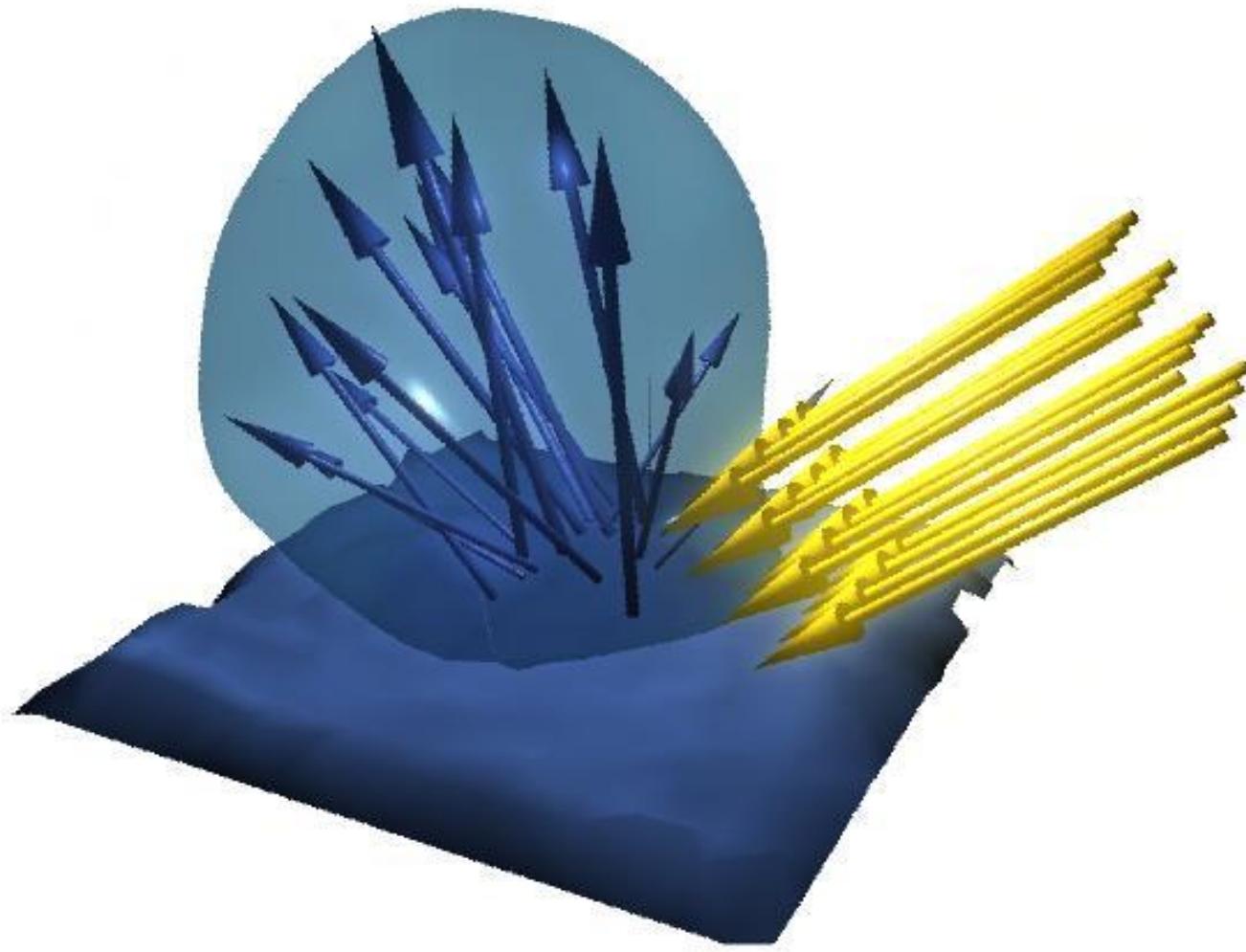


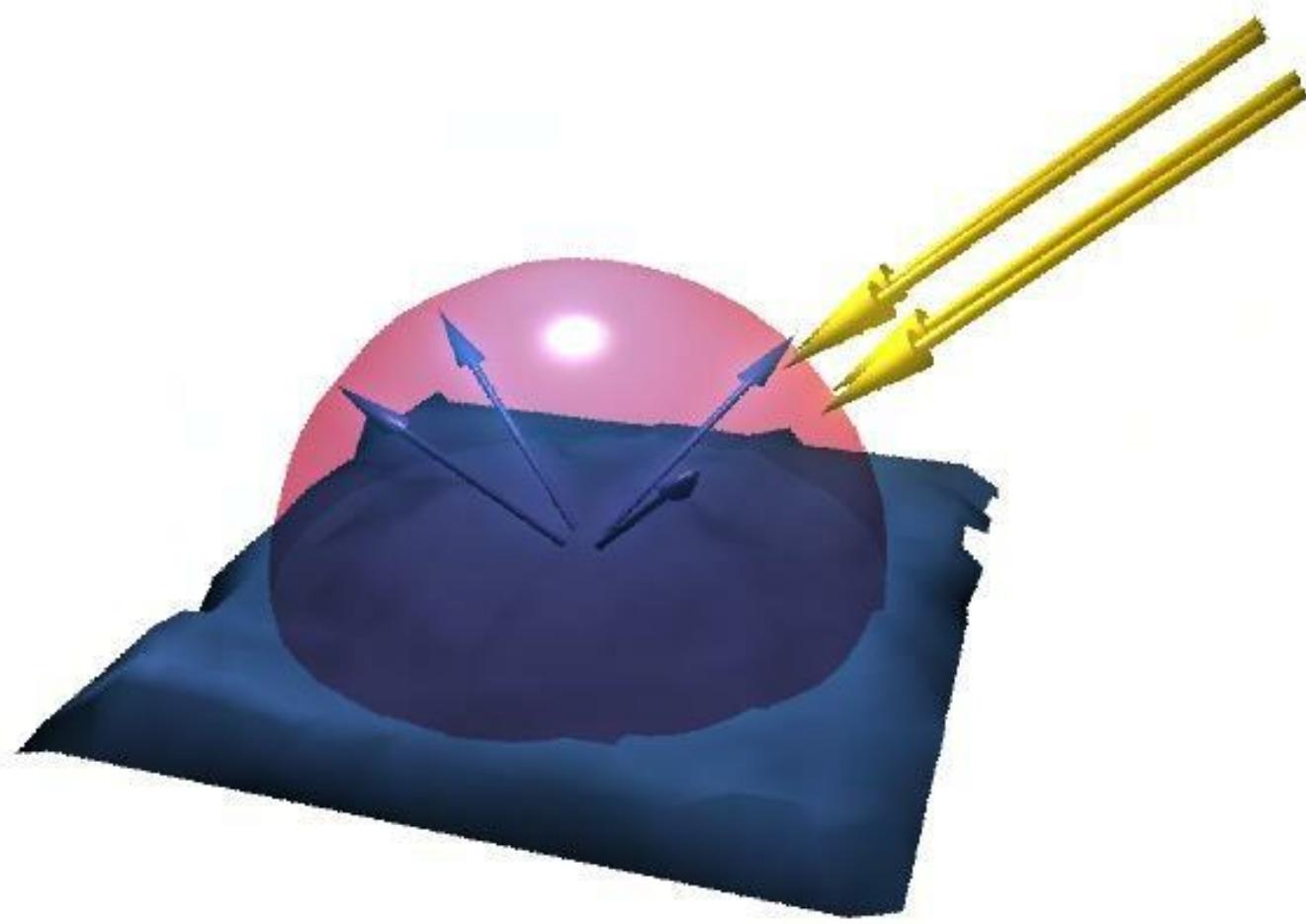
# Matière

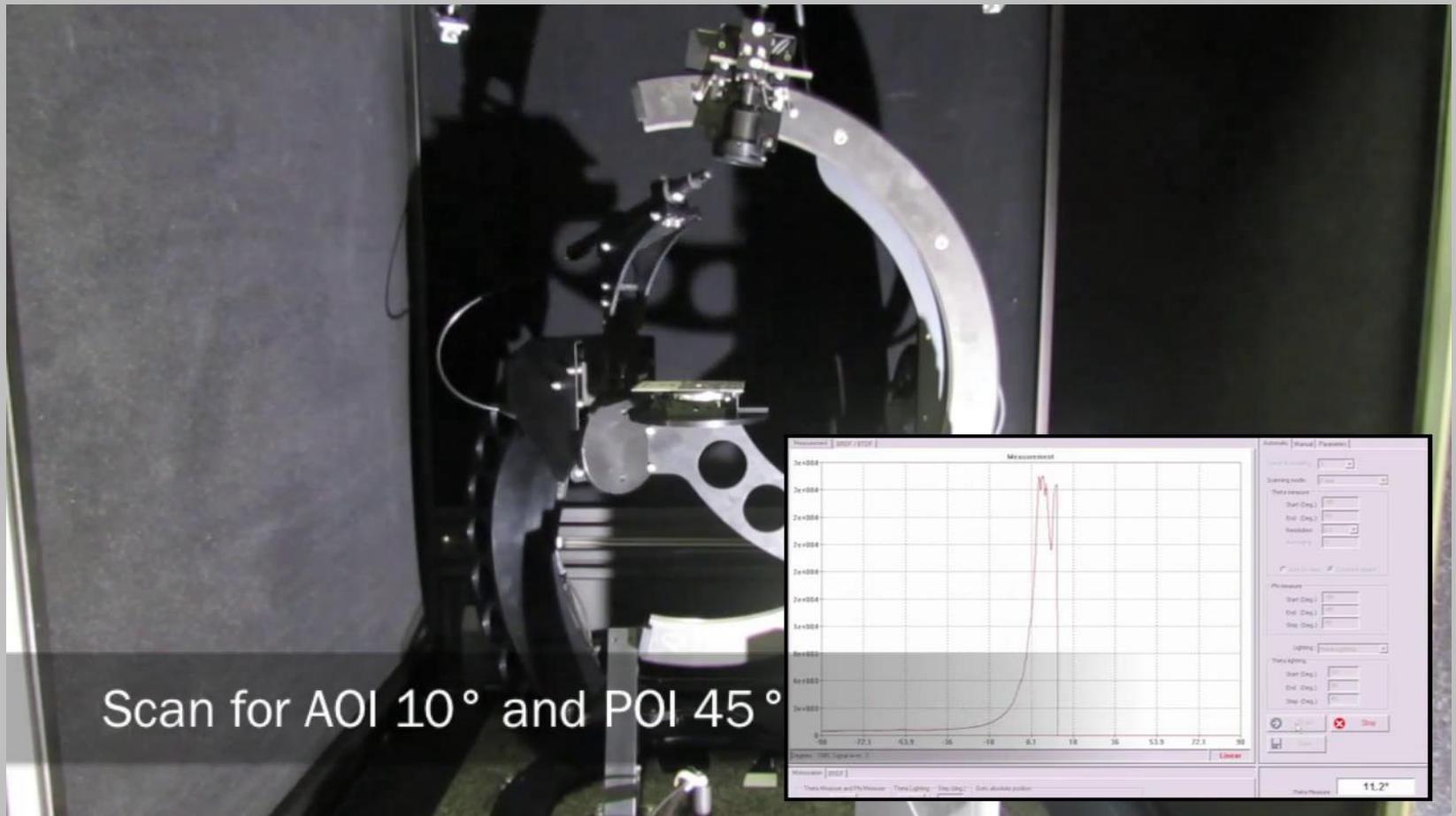
- Lois de Descartes pour la réflexion / transmission de la lumière





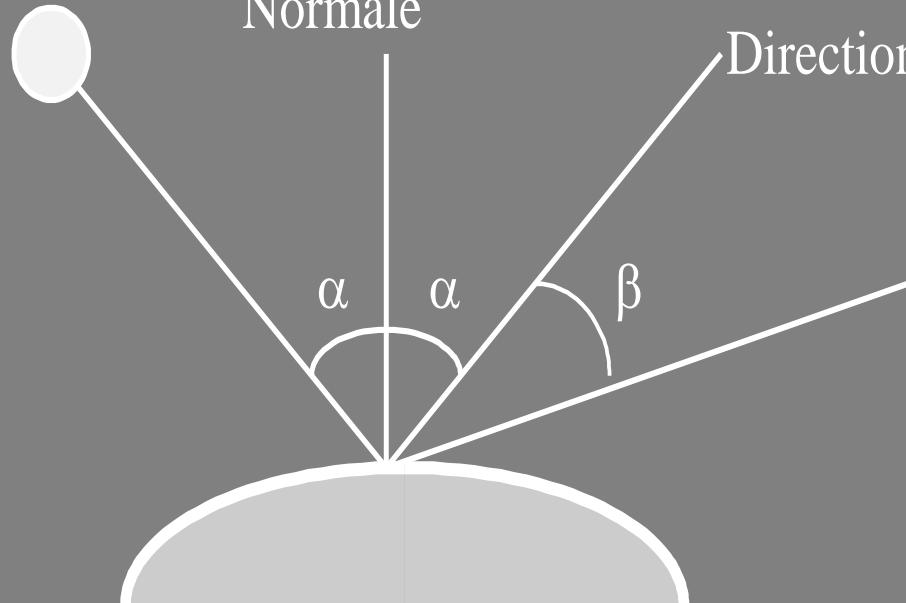






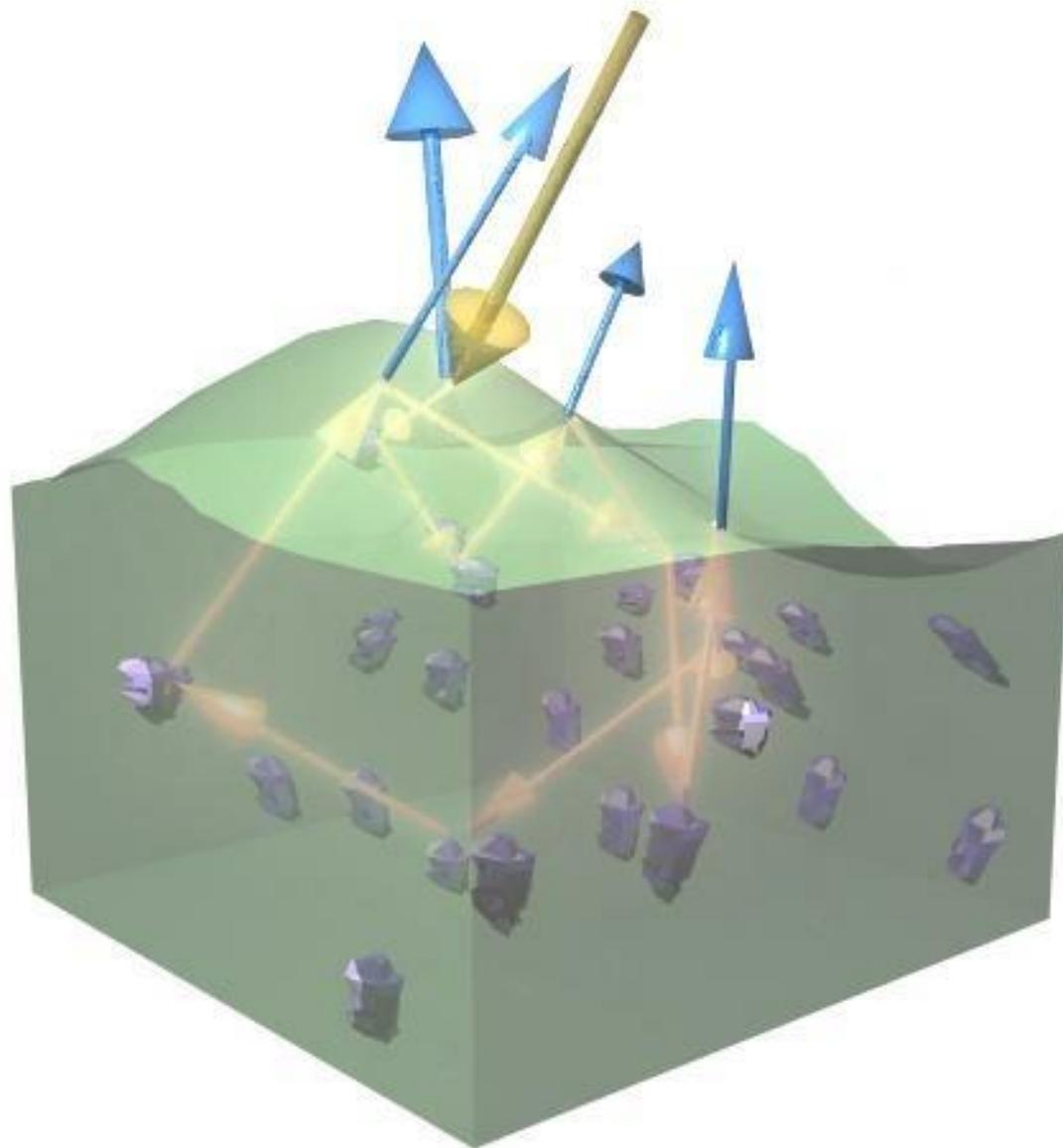
Source  
lumineuse

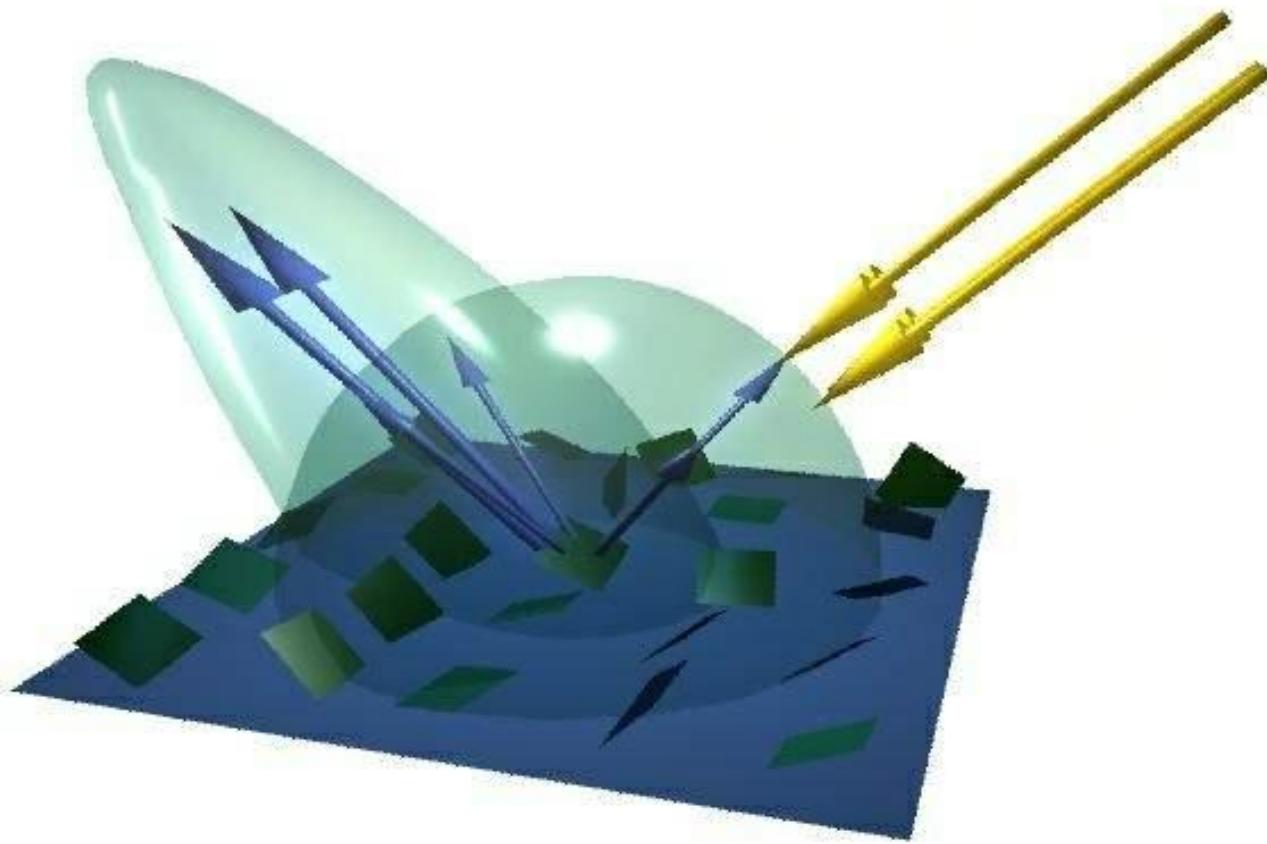
Normale



Objet illuminé

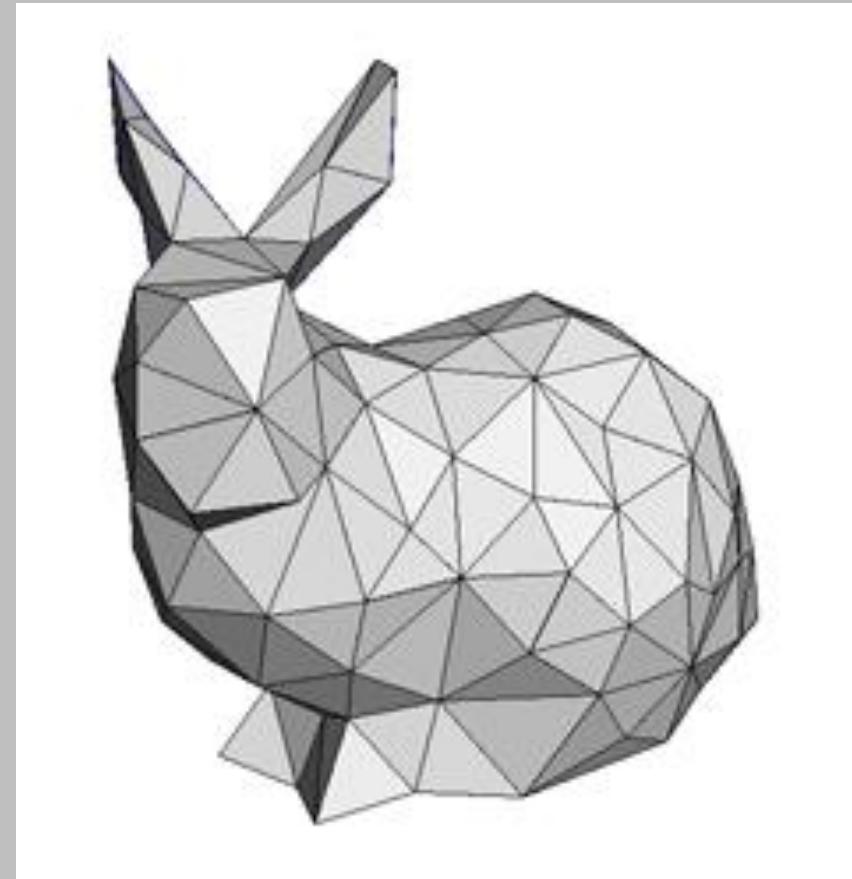
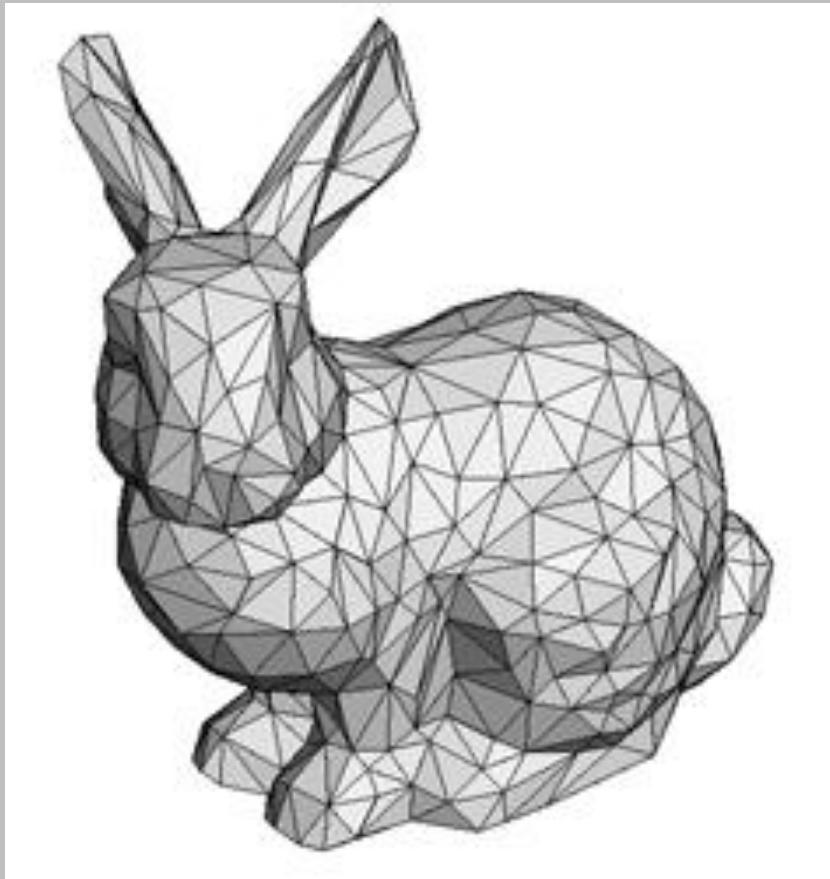
$$I(P) = k_d I_{ambiant} + \sum_{i \leq N} k_d \cdot \cos \alpha_i \cdot I_i + \sum_{i \leq N} k_s(\alpha) \cdot \cos^n \beta_i \cdot I_i$$



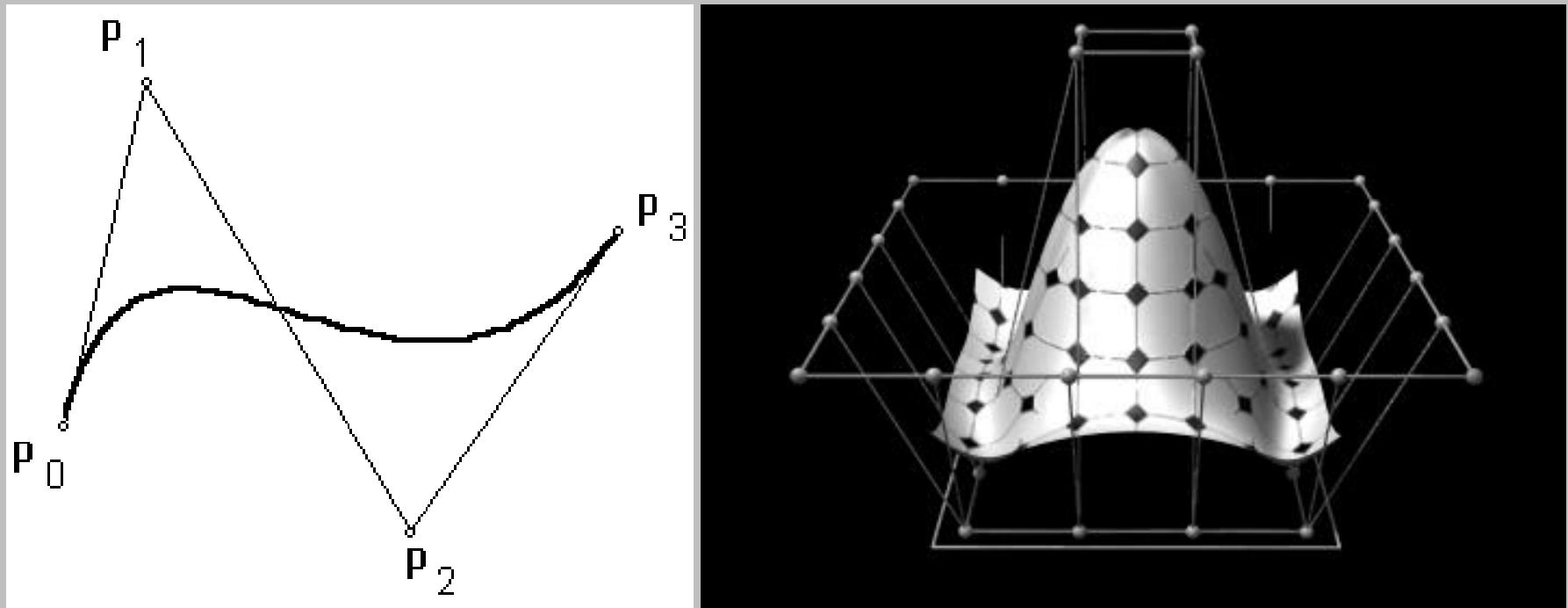


# Modélisation

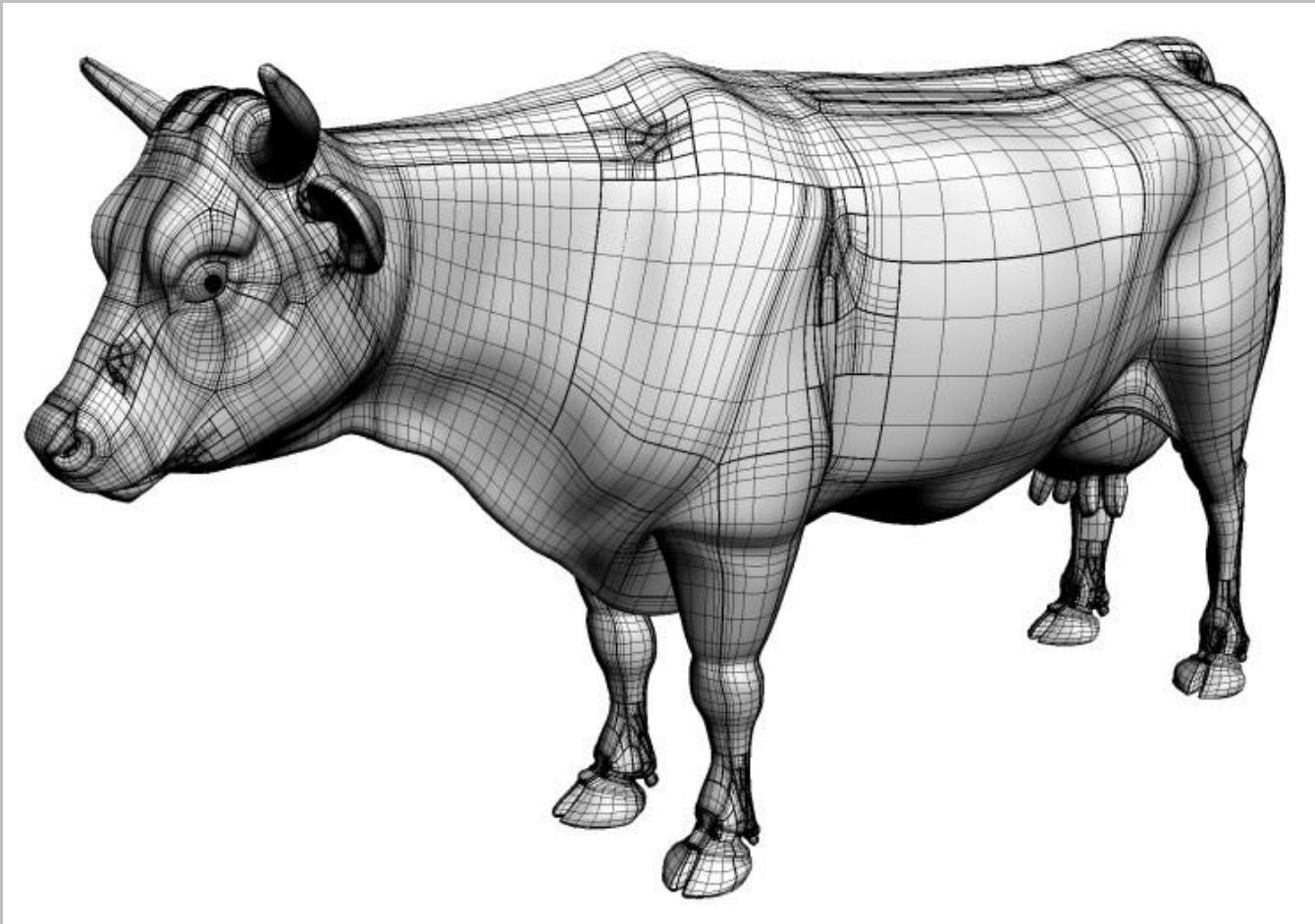
- Modélisation surfacique : polygones



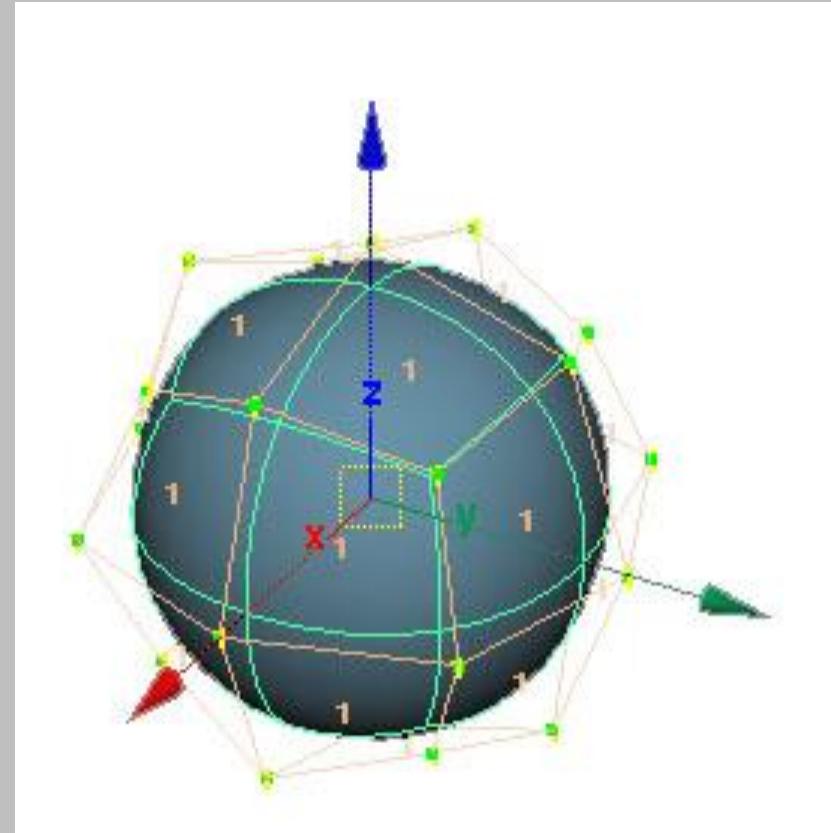
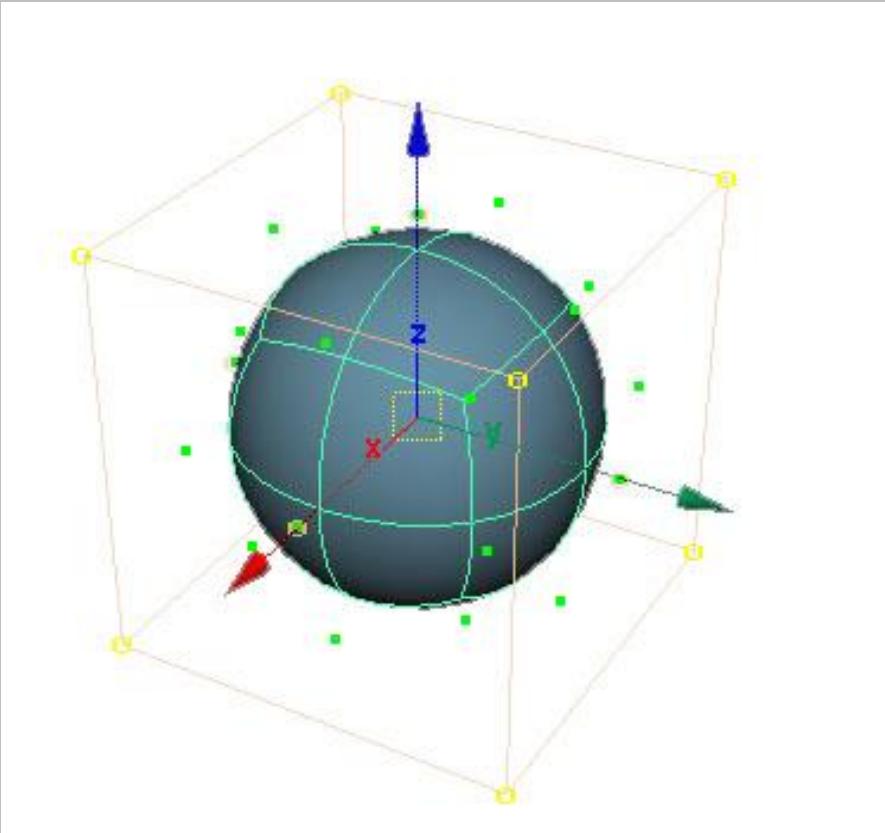
- Modélisation surfacique : Courbes et Carreaux paramétrés



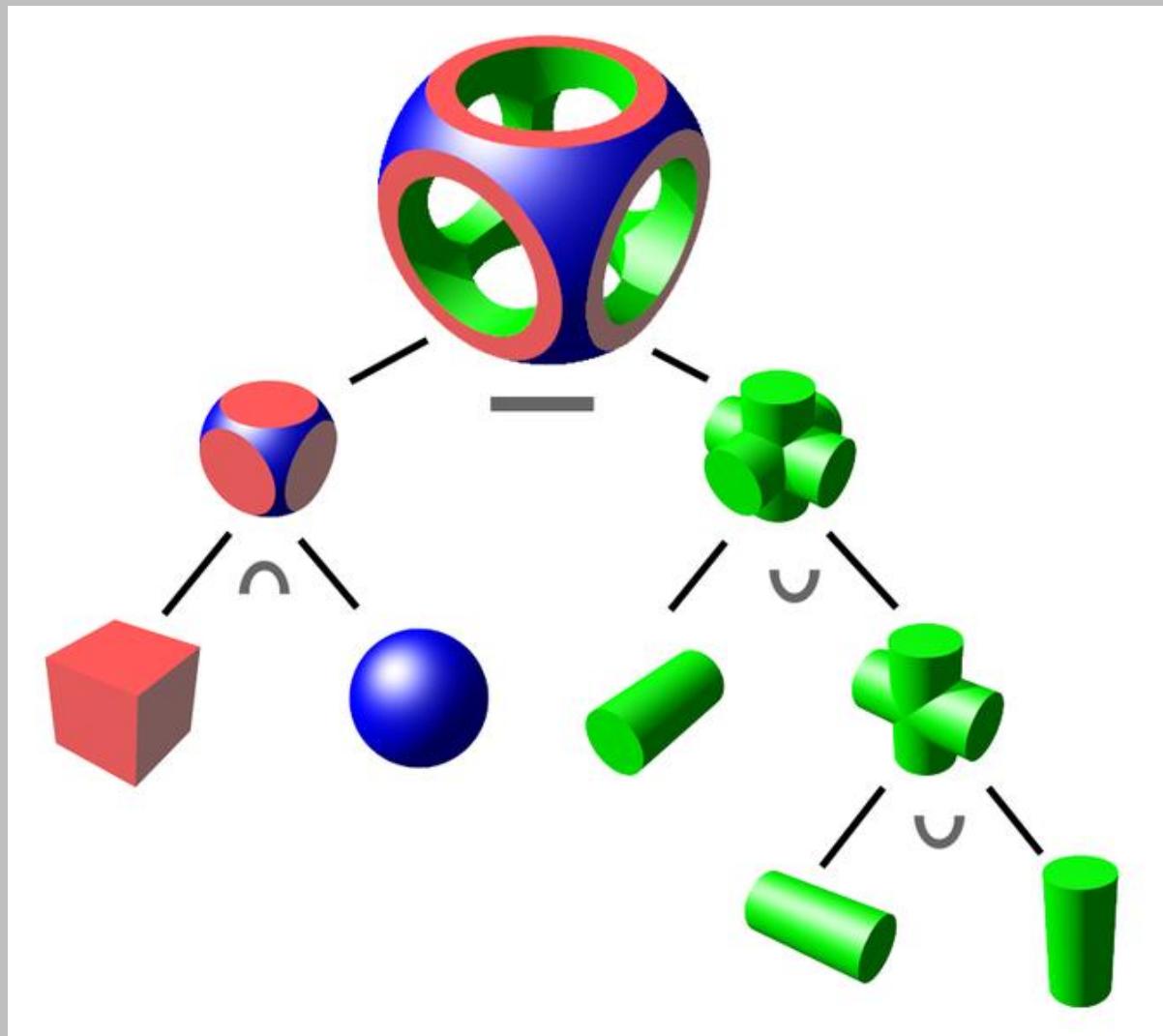
- Modélisation surfacique : Courbes et Carreaux paramétrés



- Surfaces de subdivision



- CSG



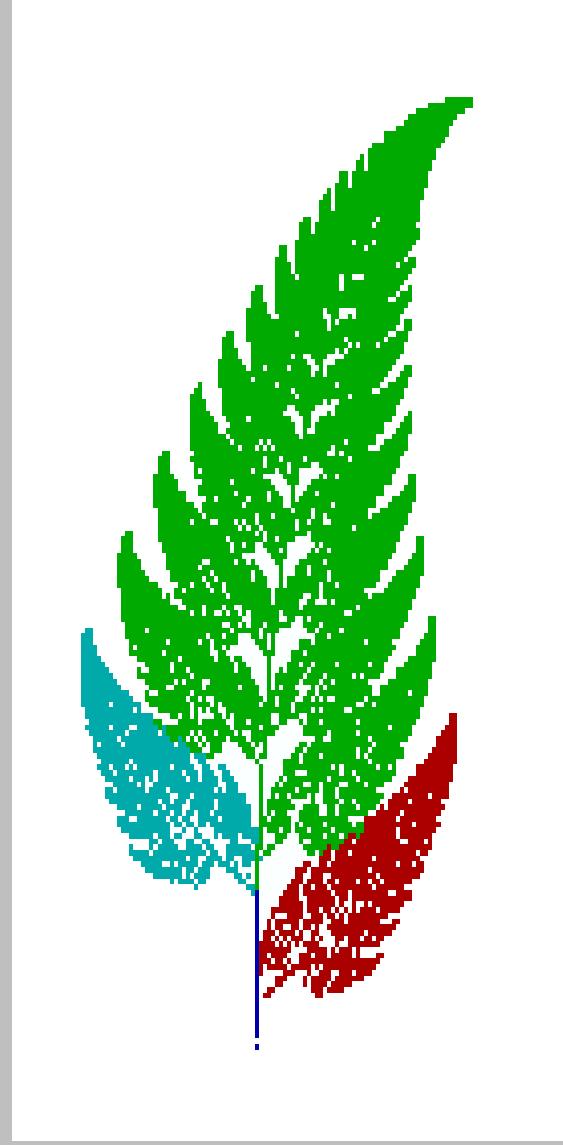
- Modélisation volumique



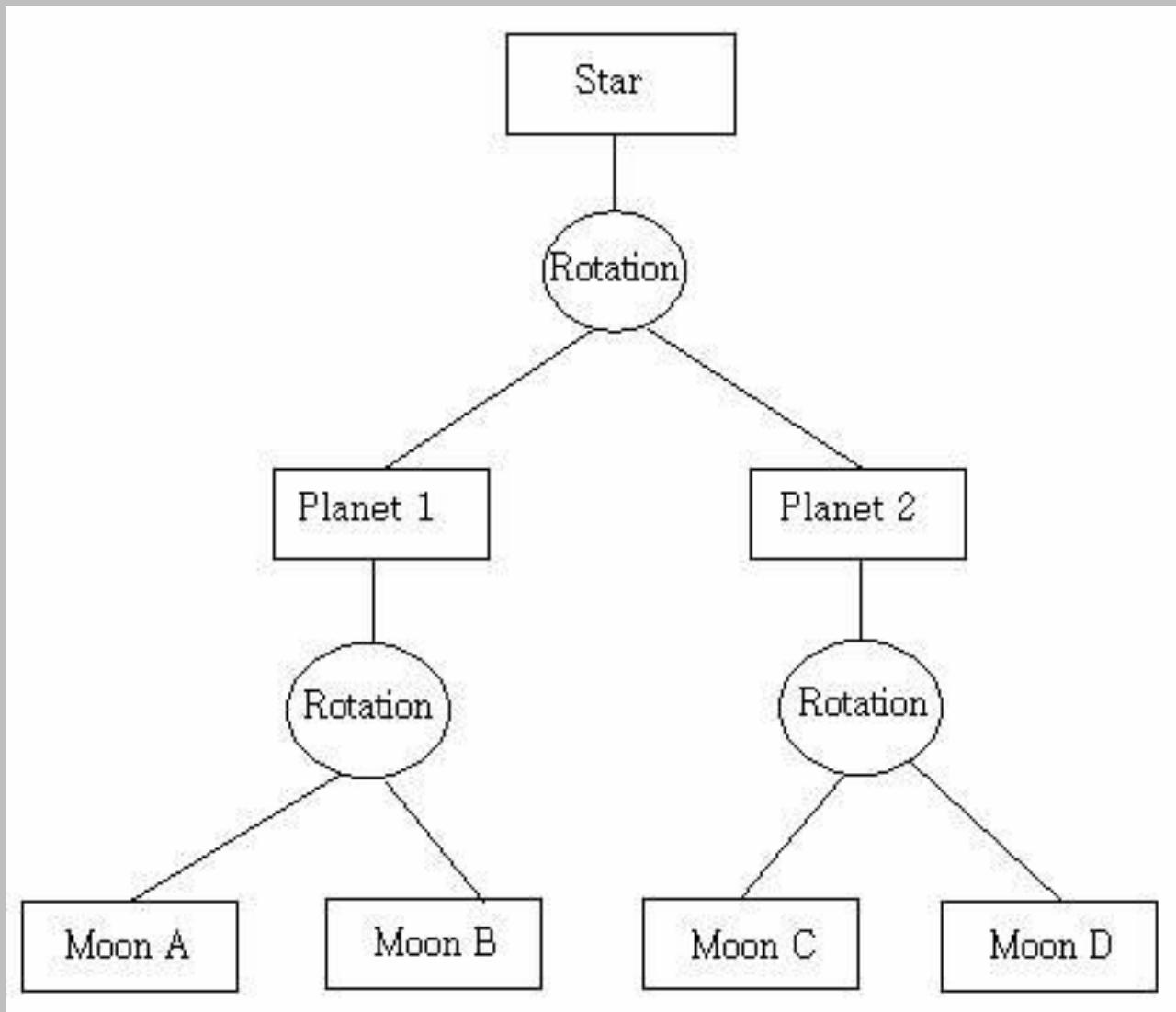
- Modélisation volumique



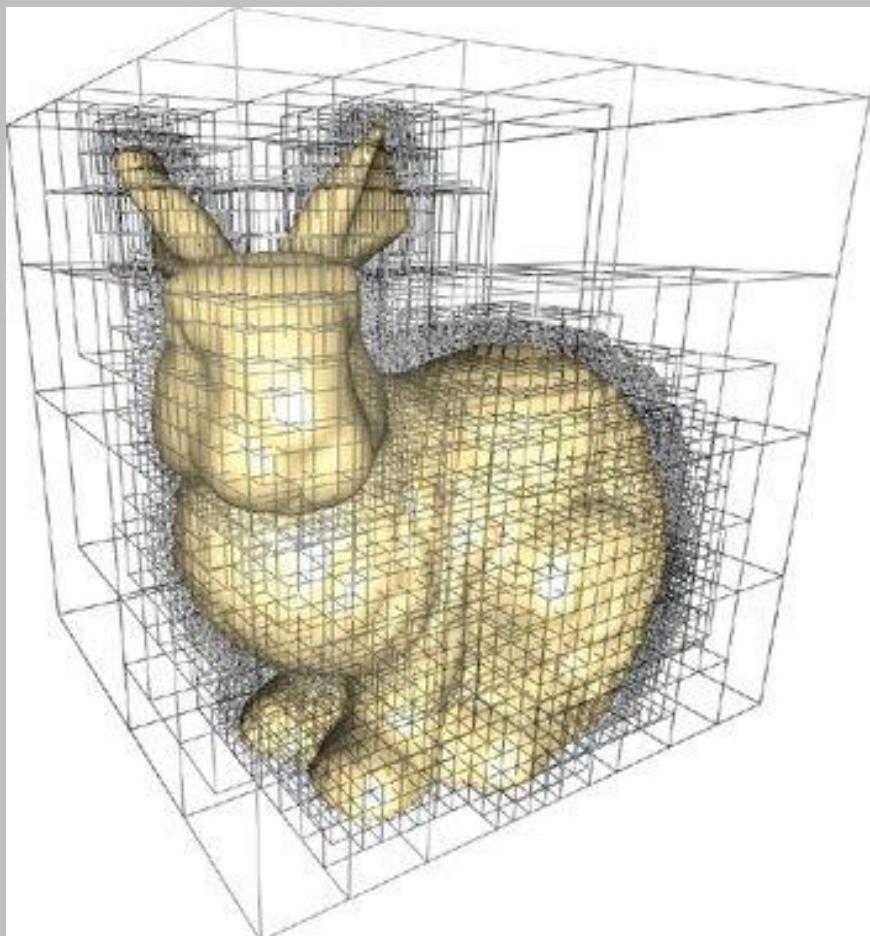
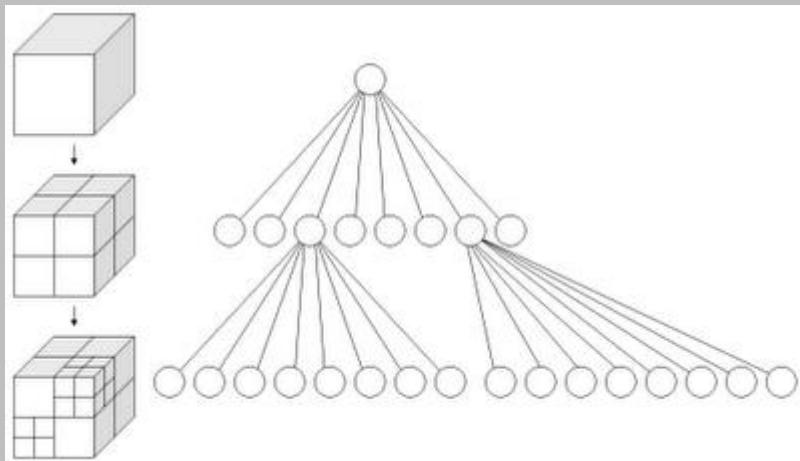
- Fractales



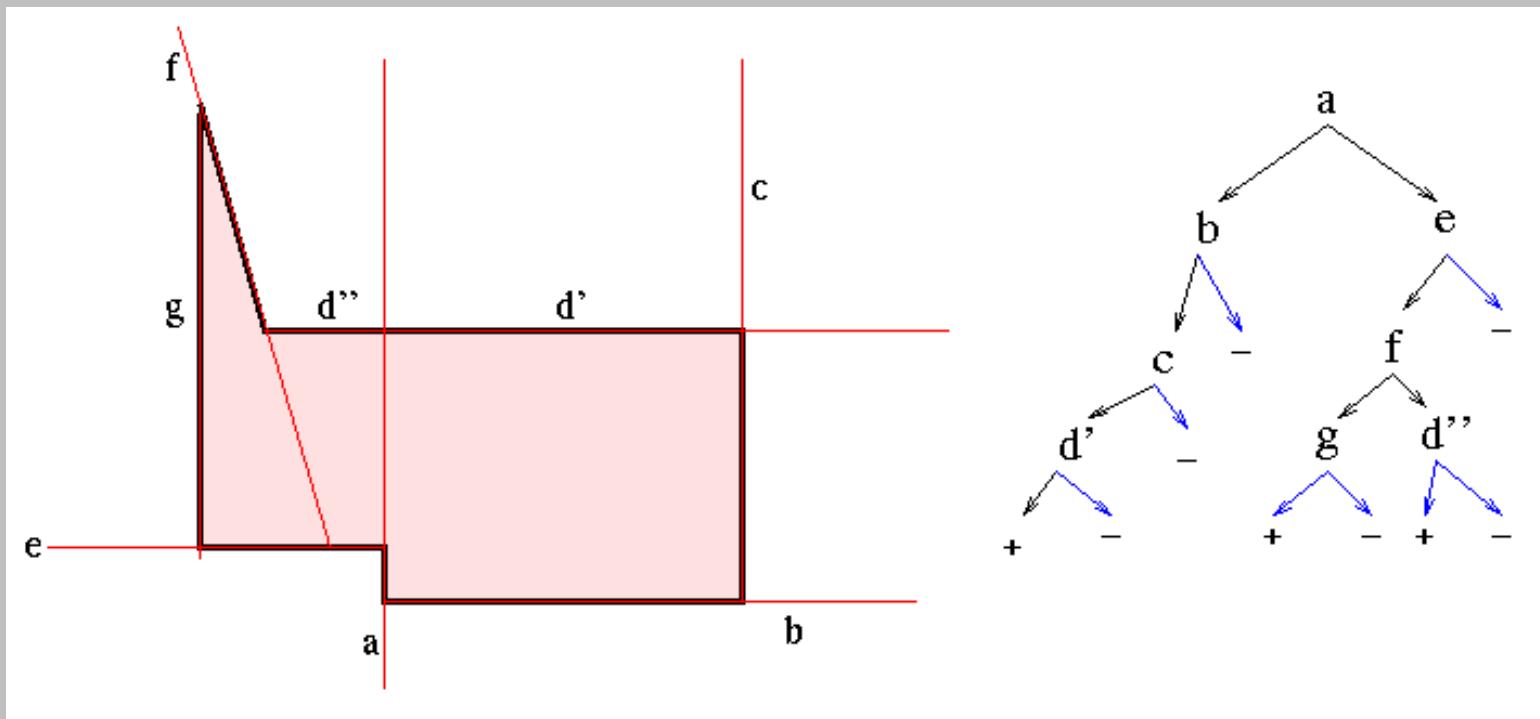
- Graphe de scène



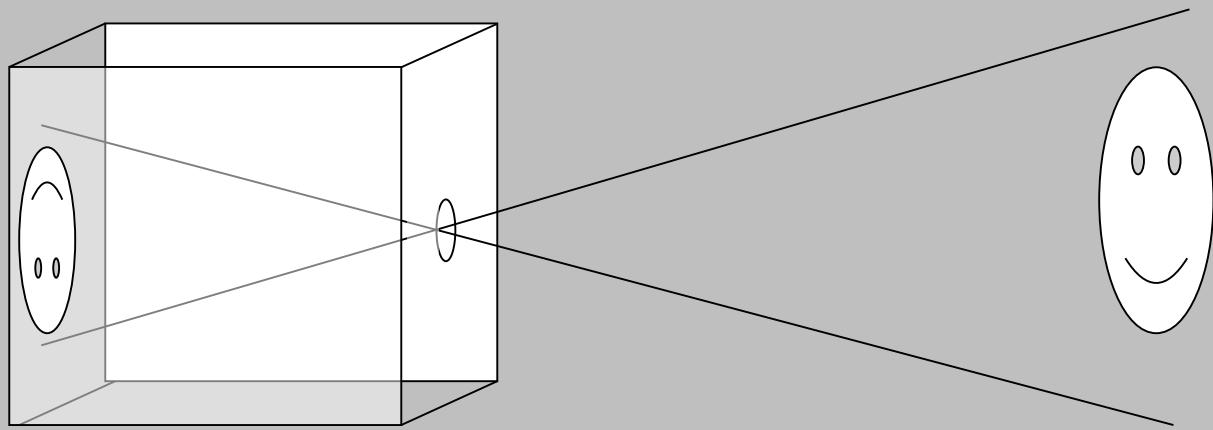
- Octrees

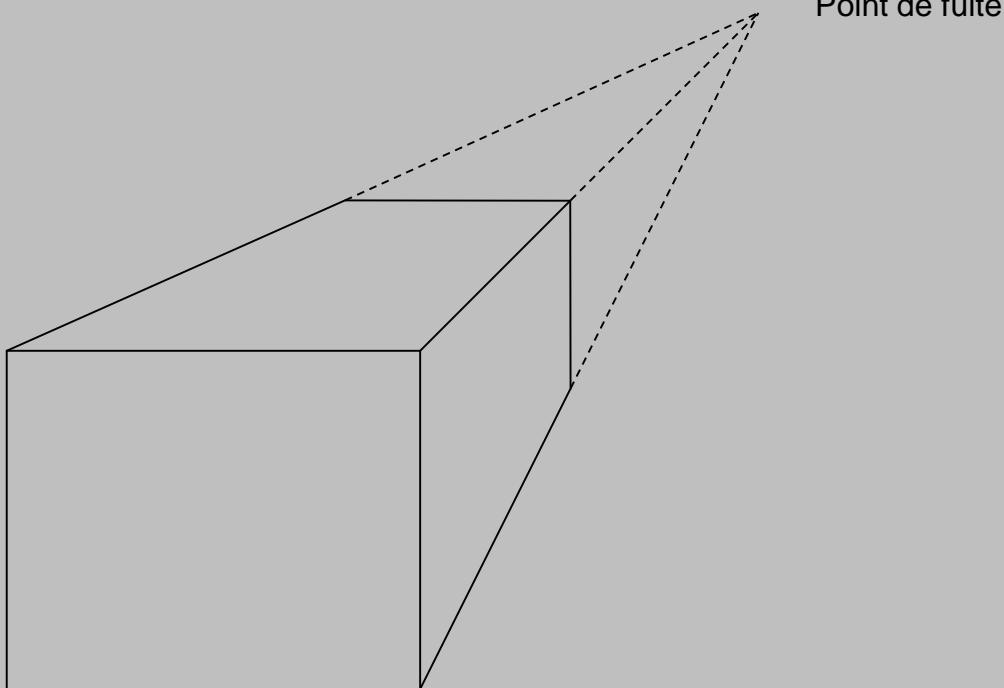


- BSP

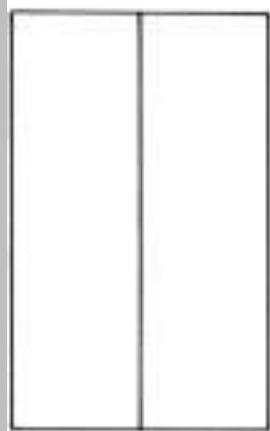


# Prise de vue

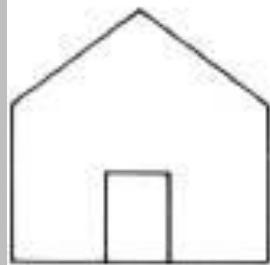




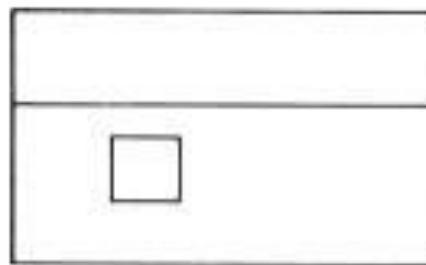
Point de fuite



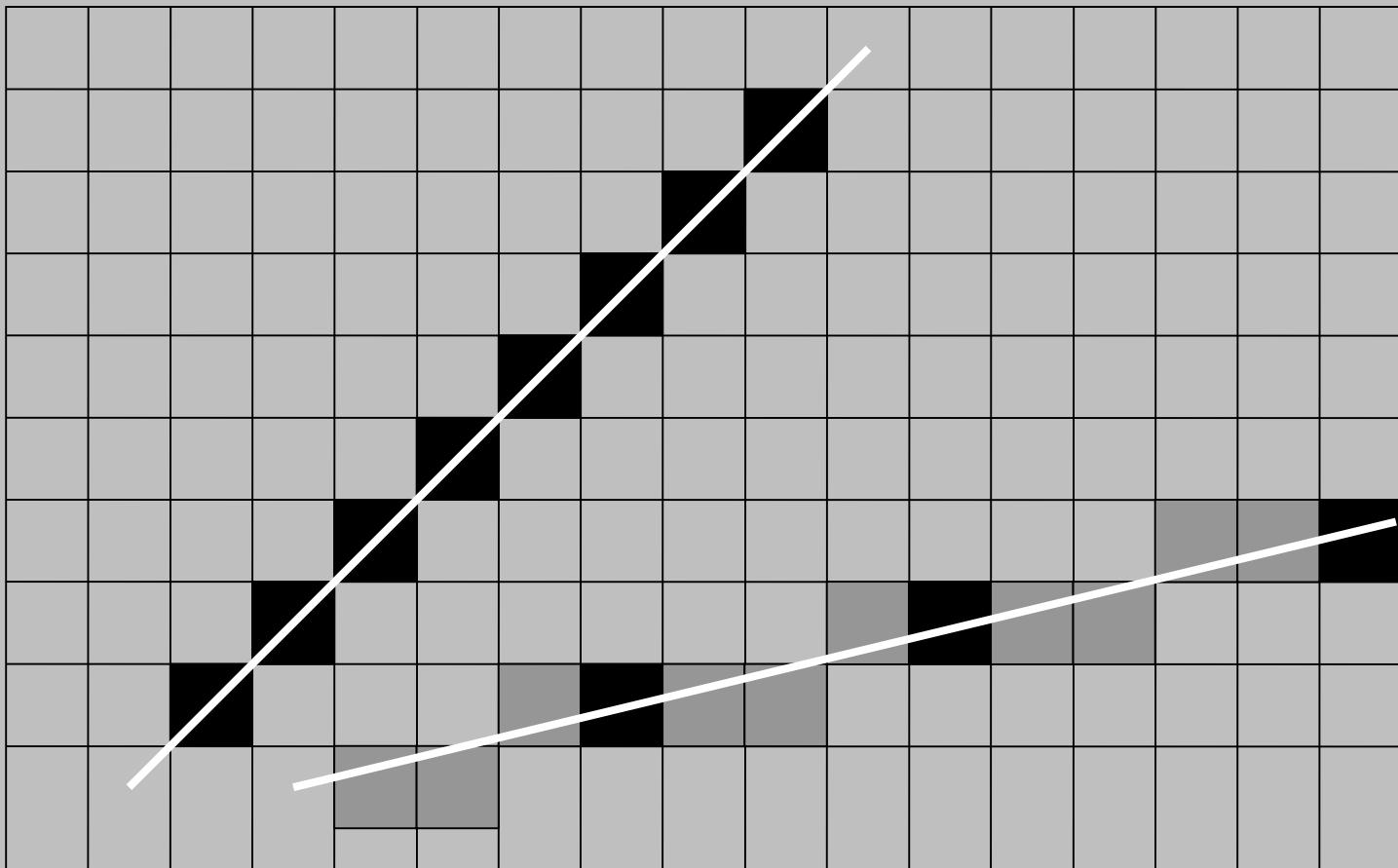
TOP

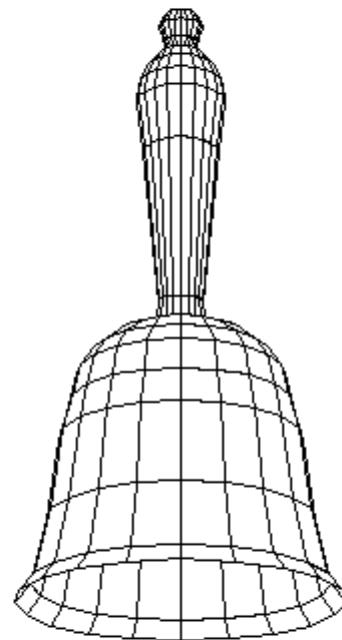


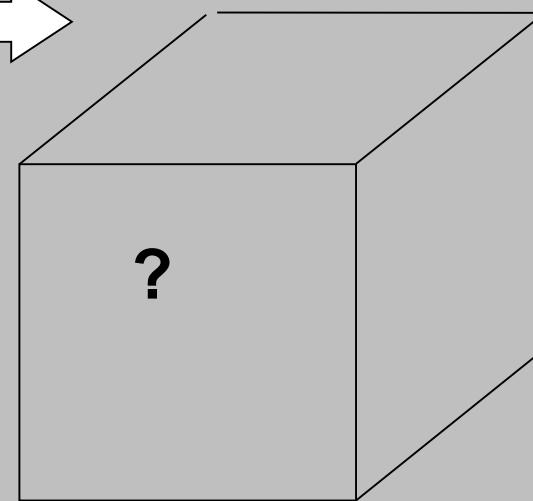
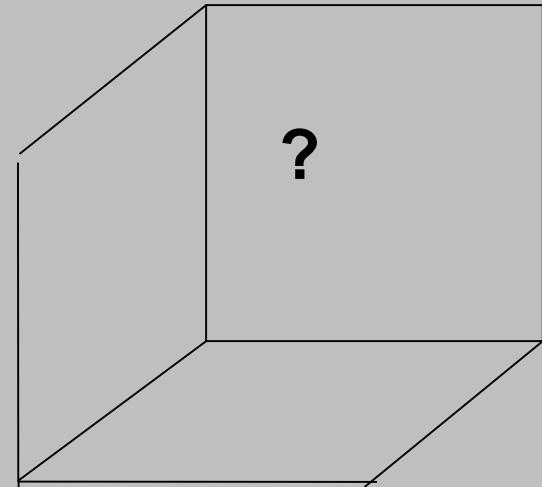
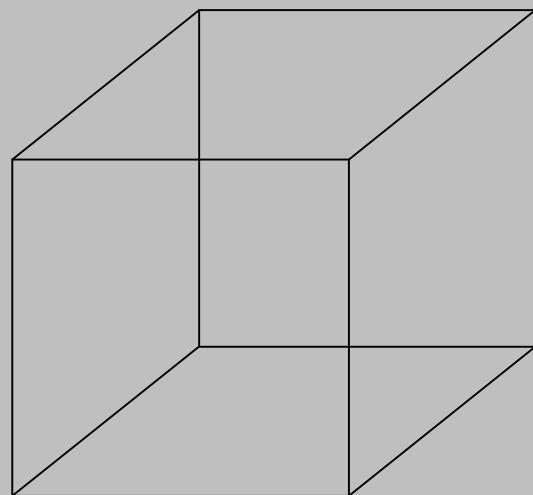
FRONT

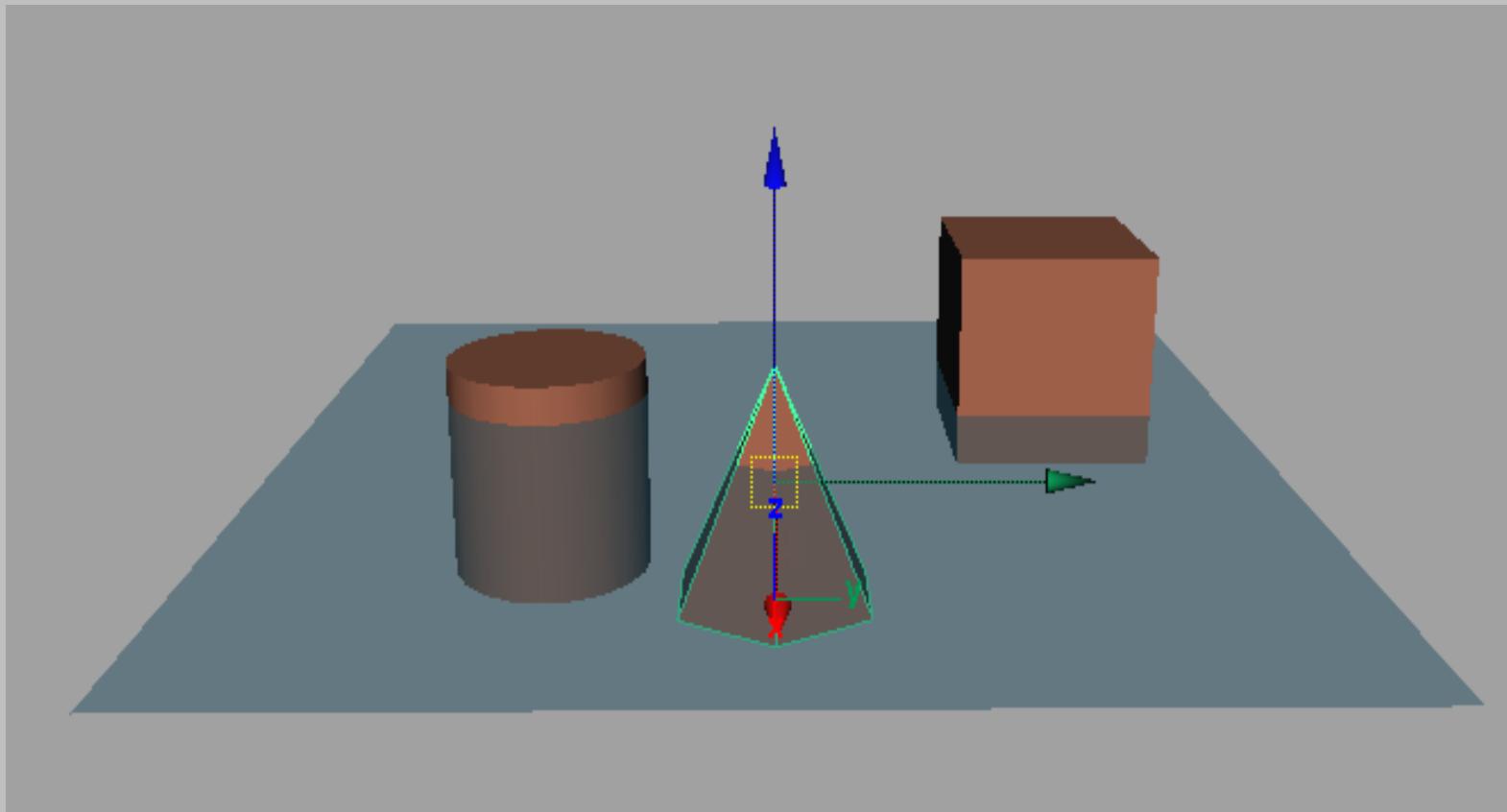


SIDE

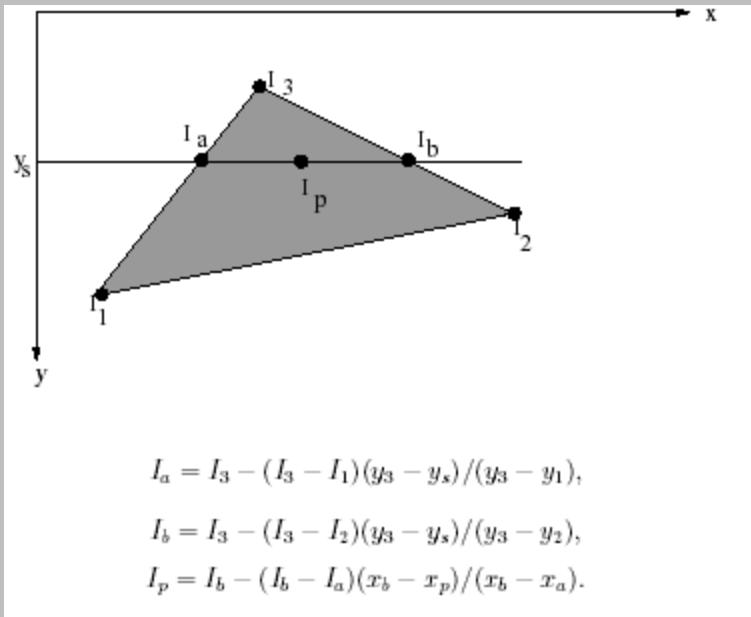
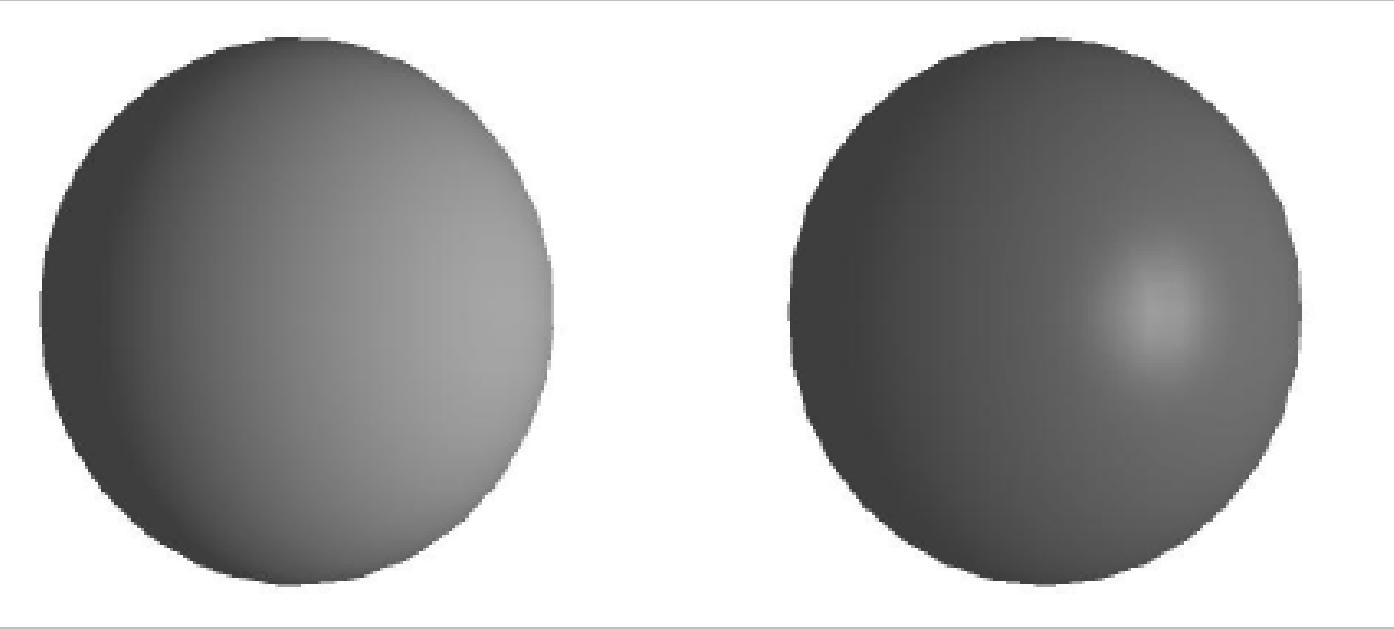


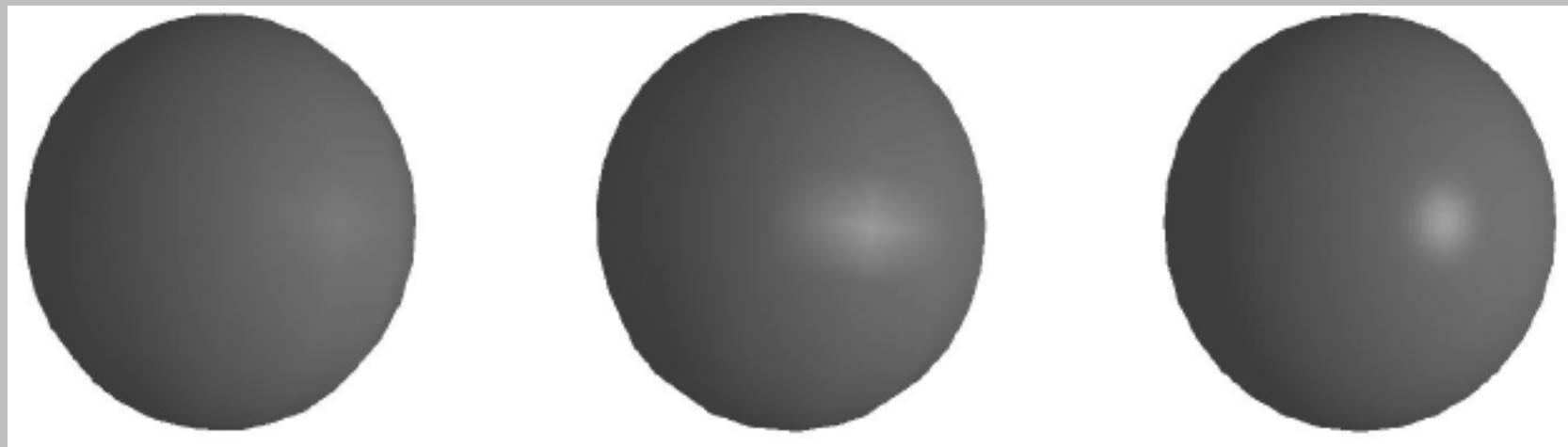
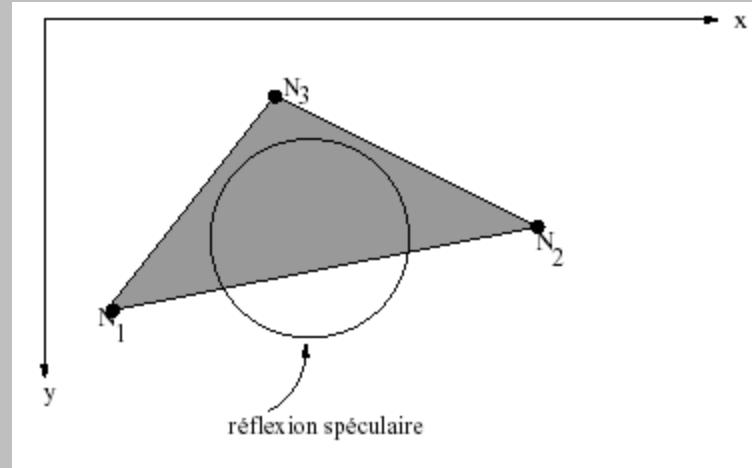
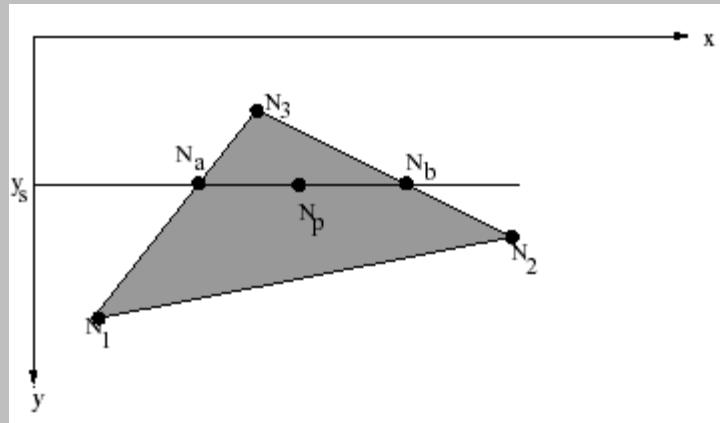


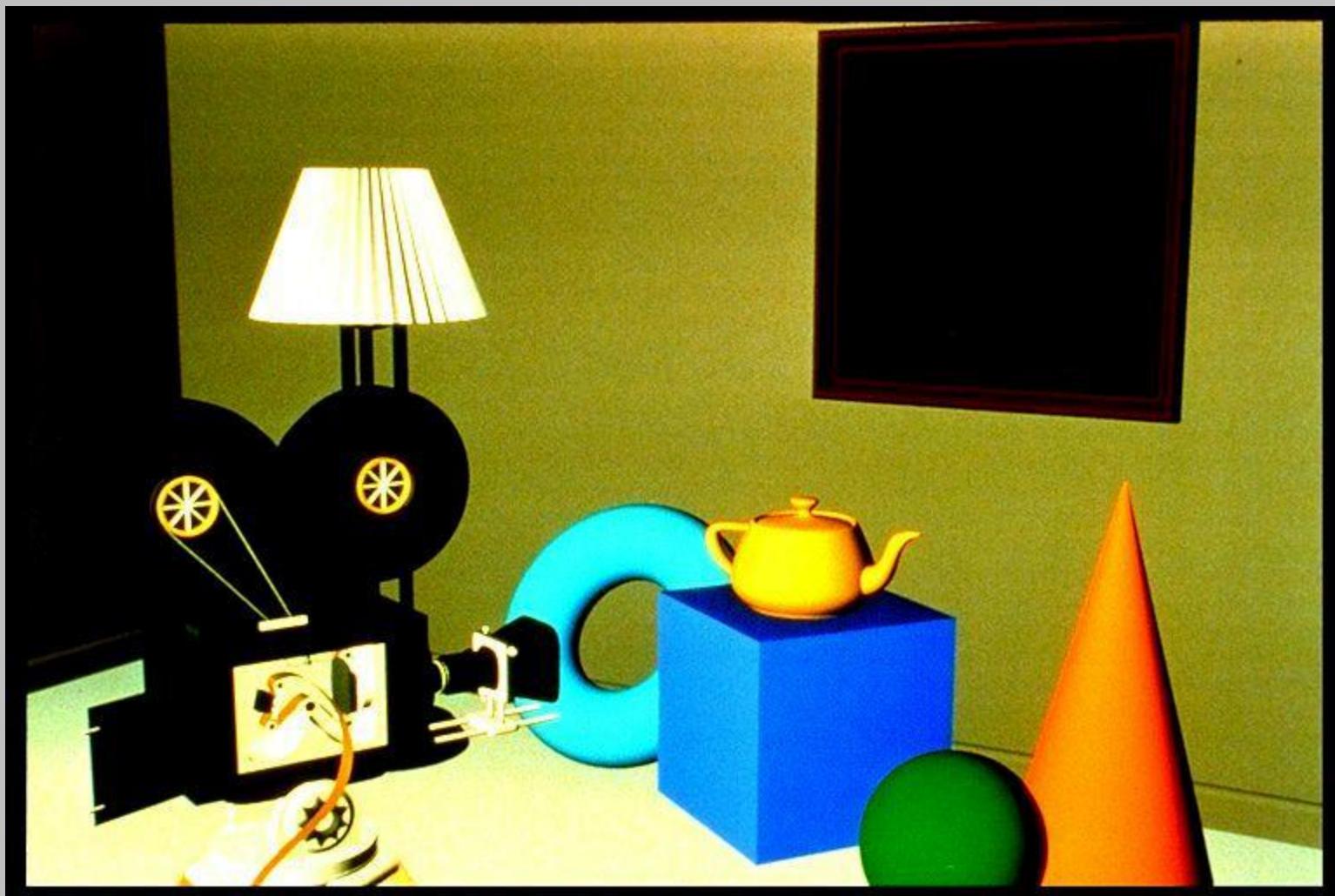






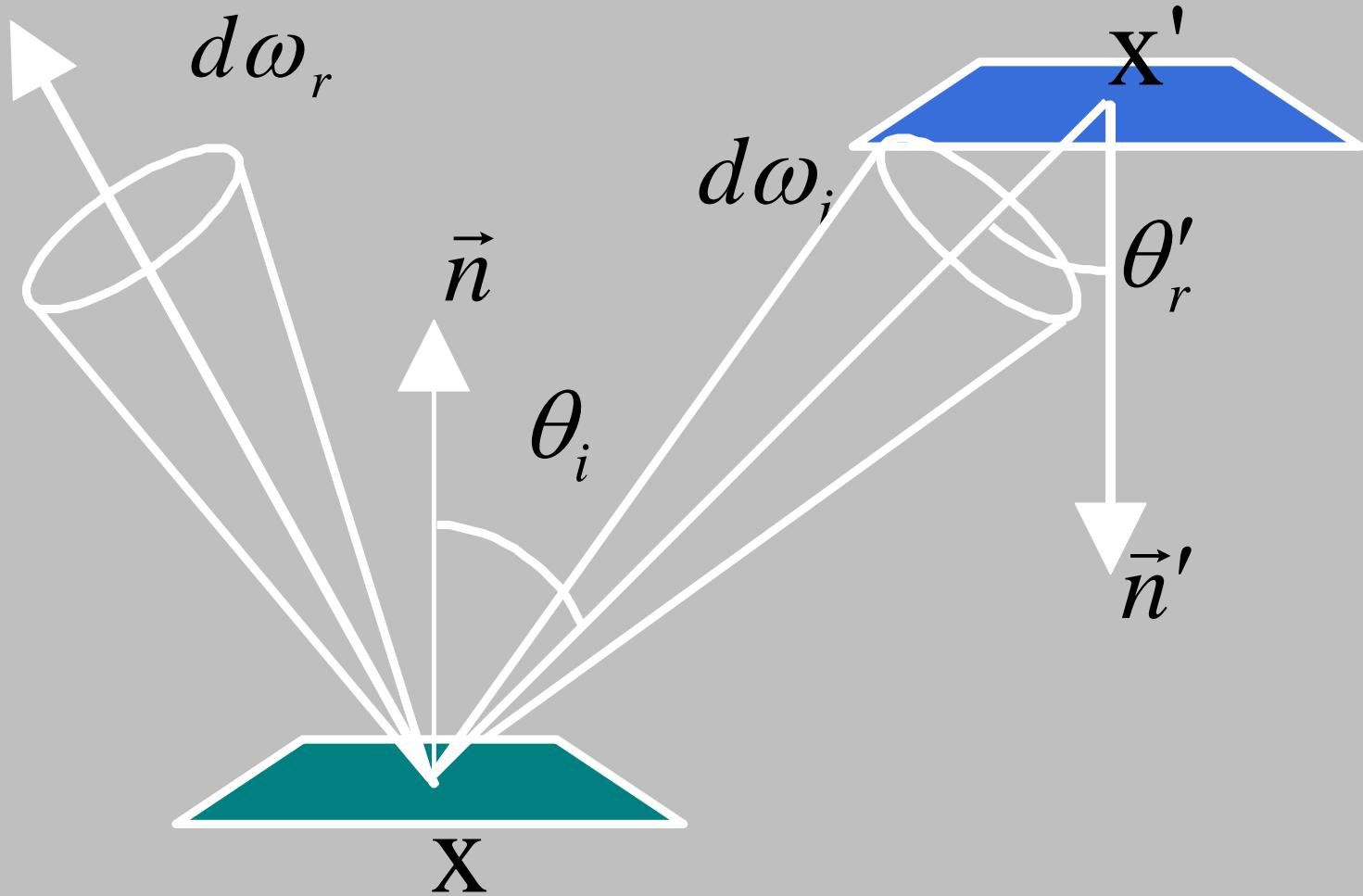








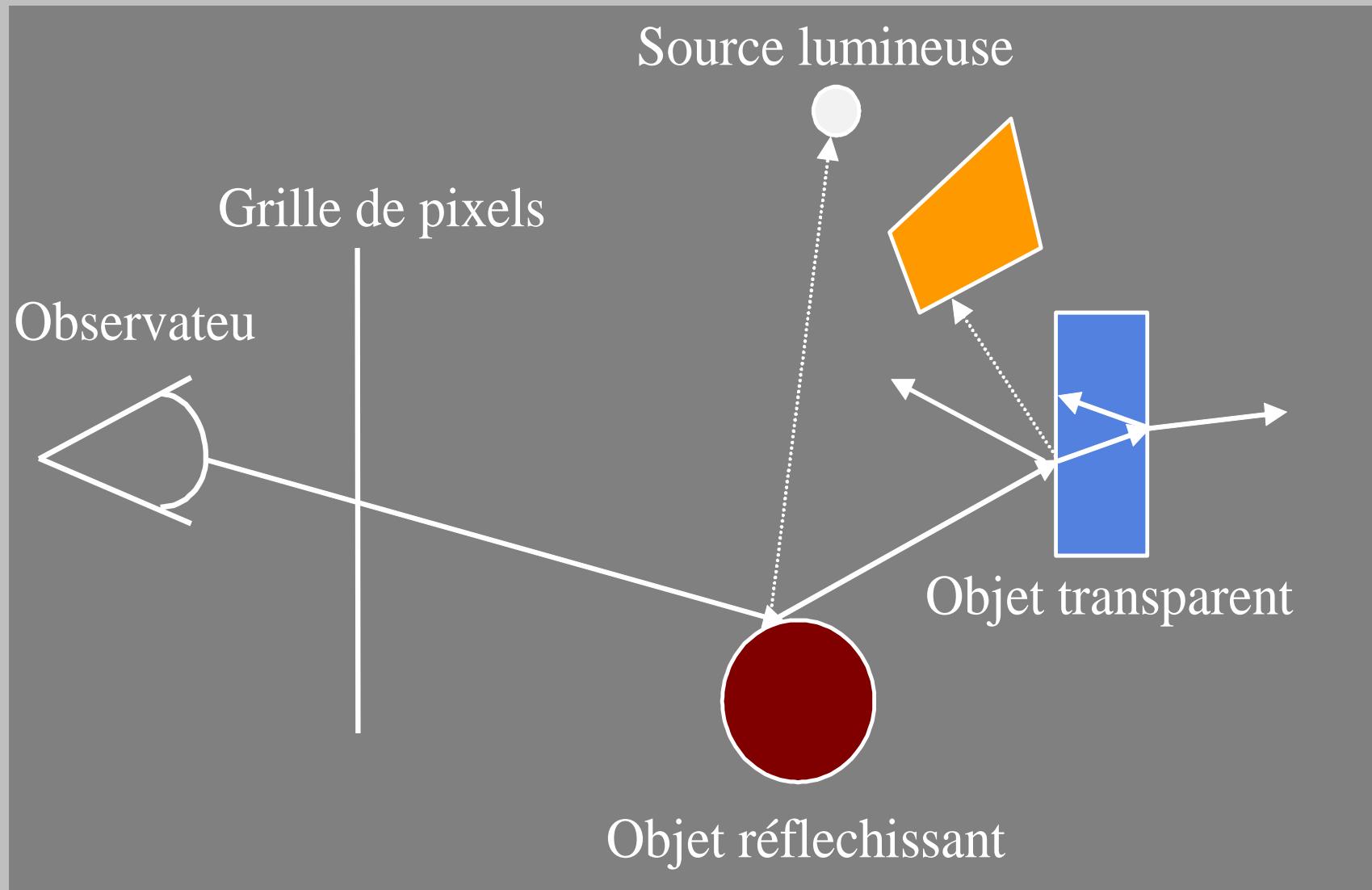
# Éclairage

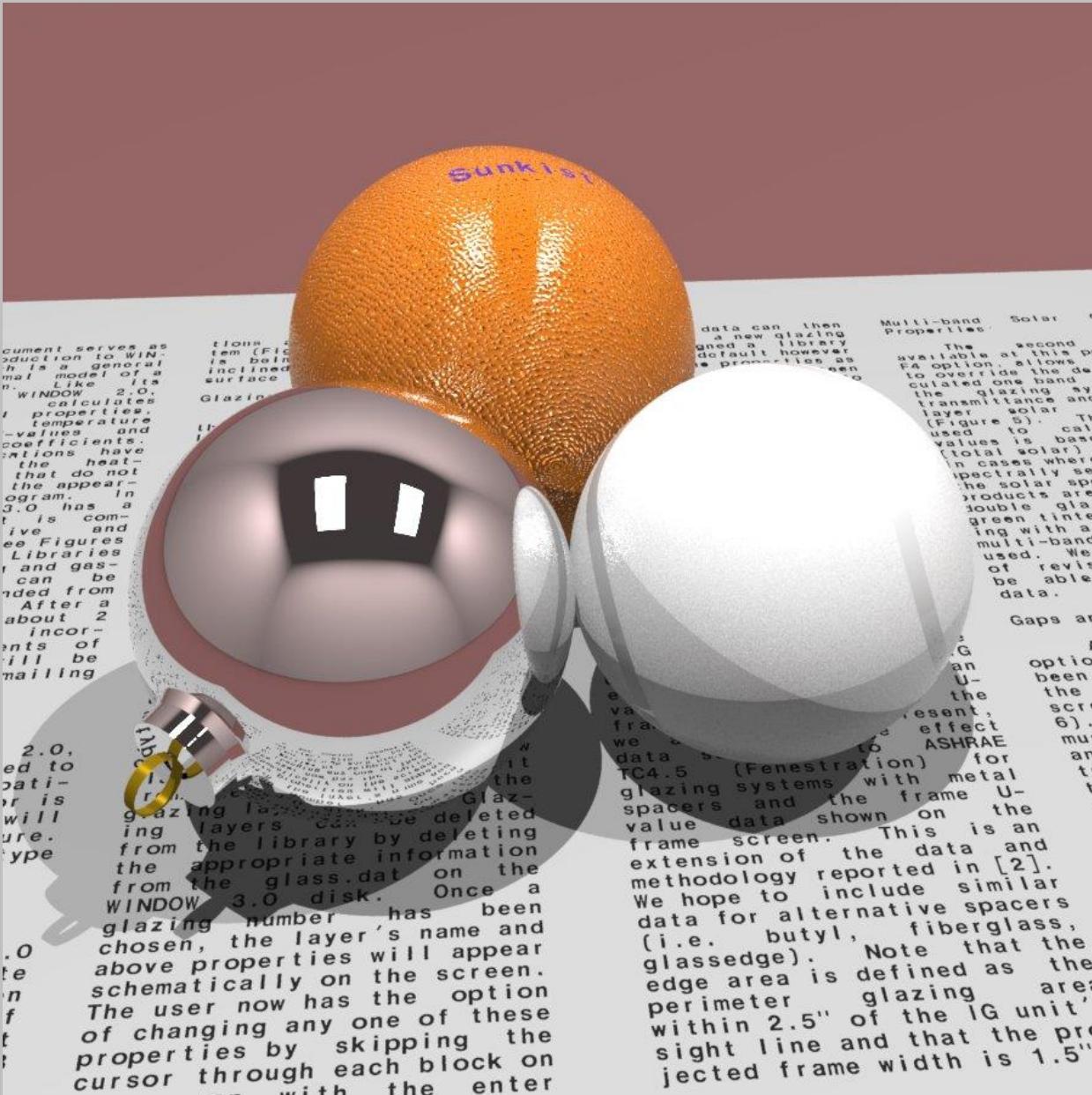


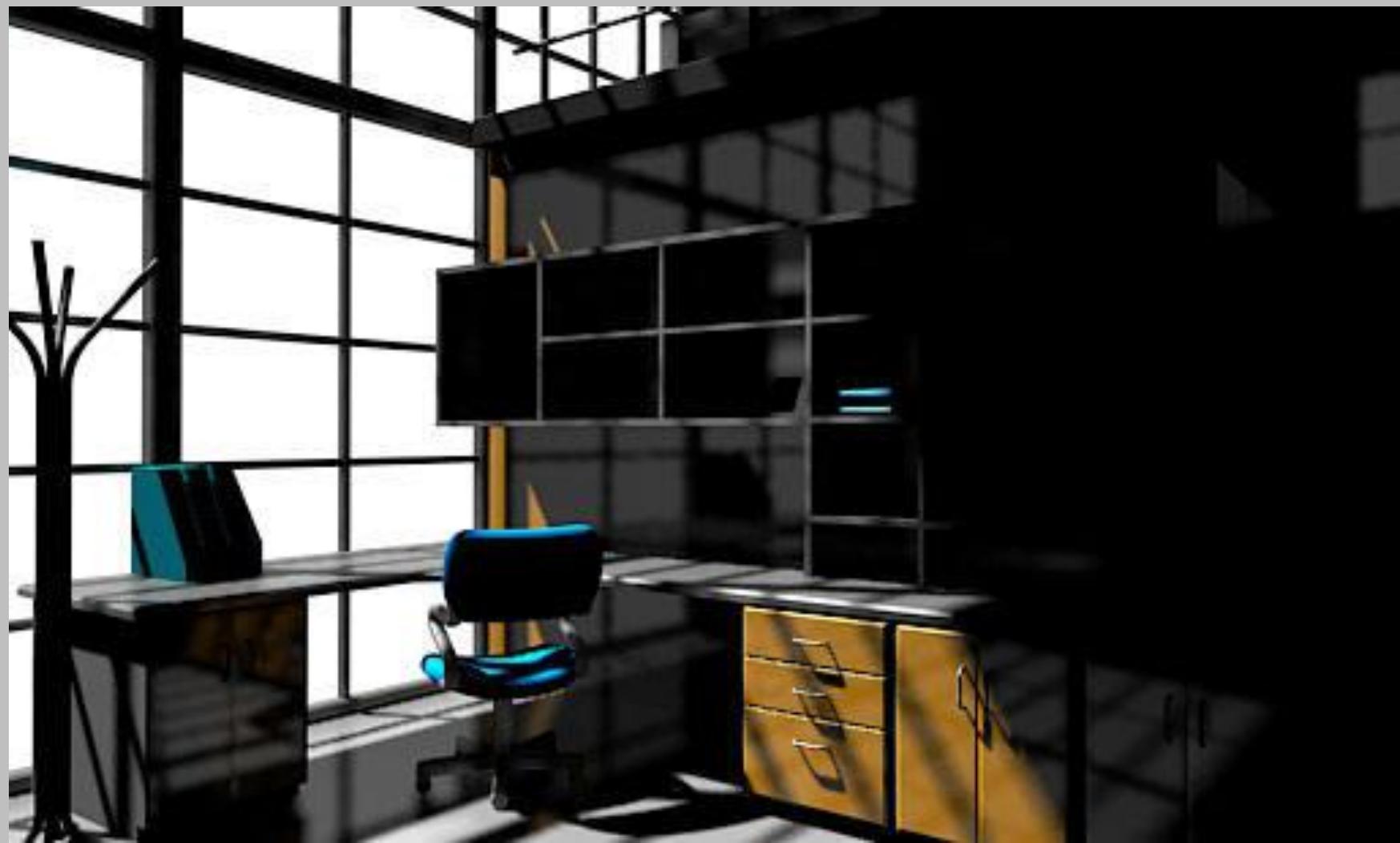
- Equation du rendu

$$\begin{aligned} L_r(x, \vec{\omega}_r) &= \\ L_e(x, \vec{\omega}_r) &+ \\ \int_S \rho_{bd}(x, \vec{\omega}_I, \vec{\omega}_r) \cdot L_r(x', \vec{\omega}'_r) \cdot G(x, x') dx dx' \end{aligned}$$

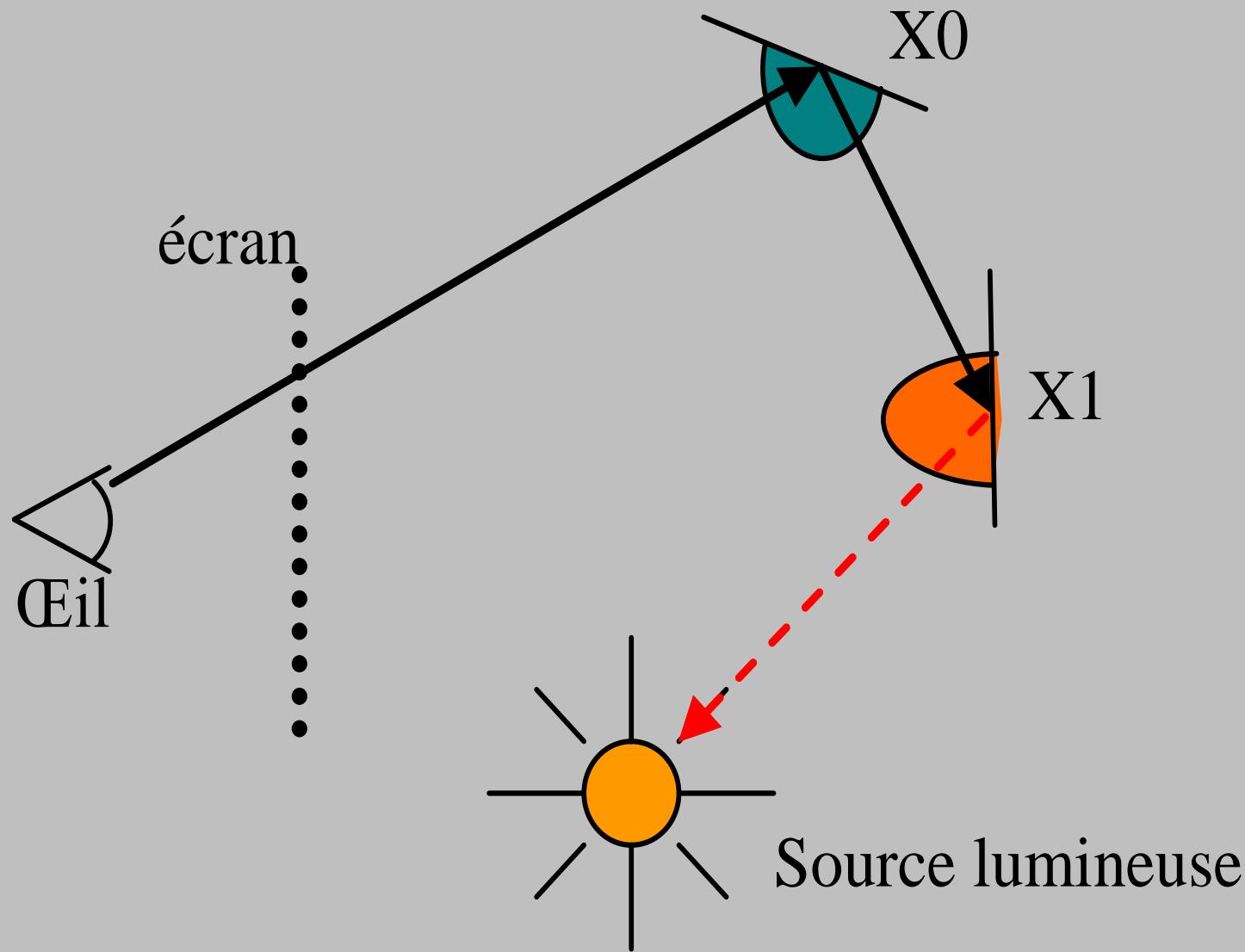
- Lancer de rayon

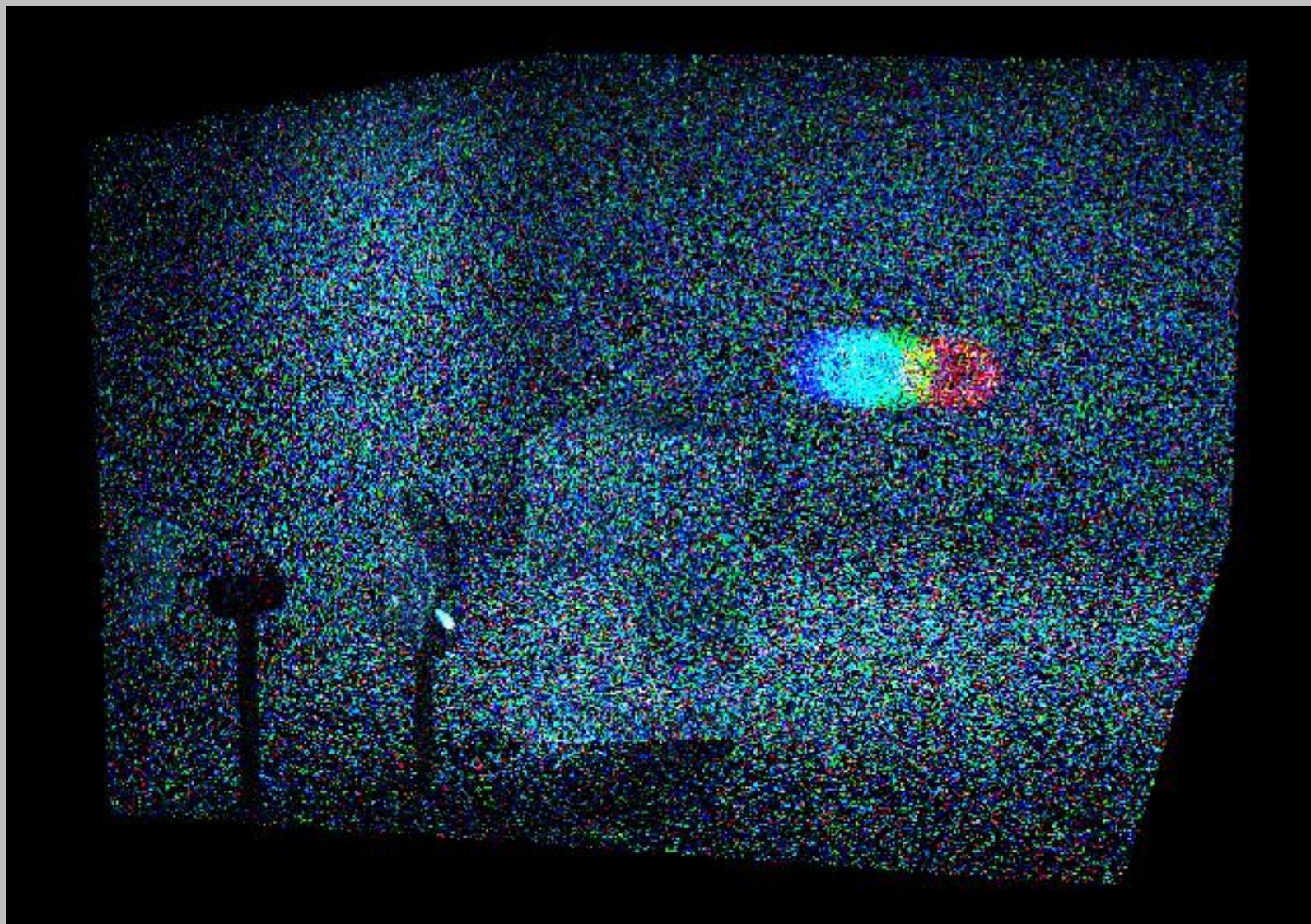


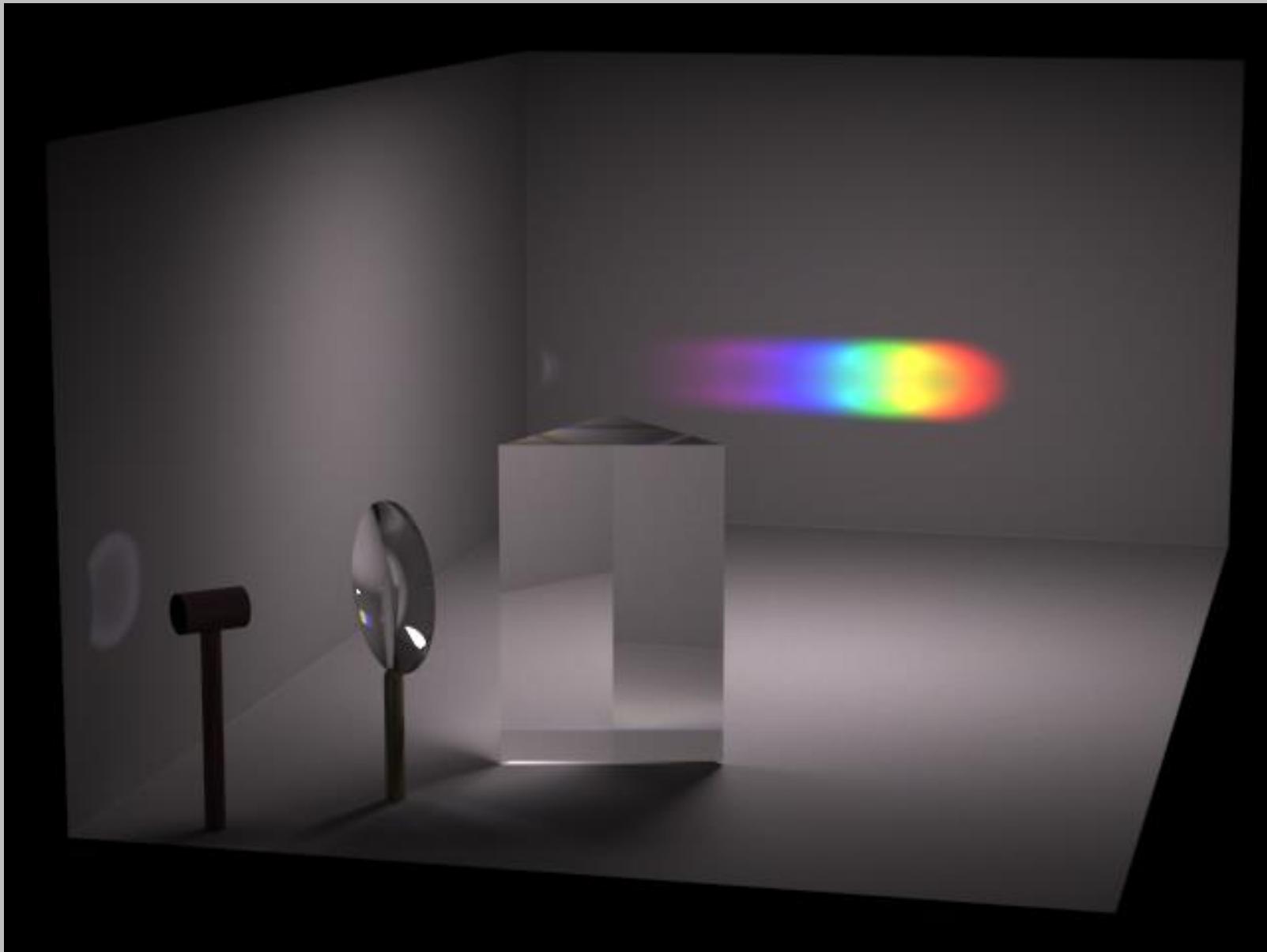




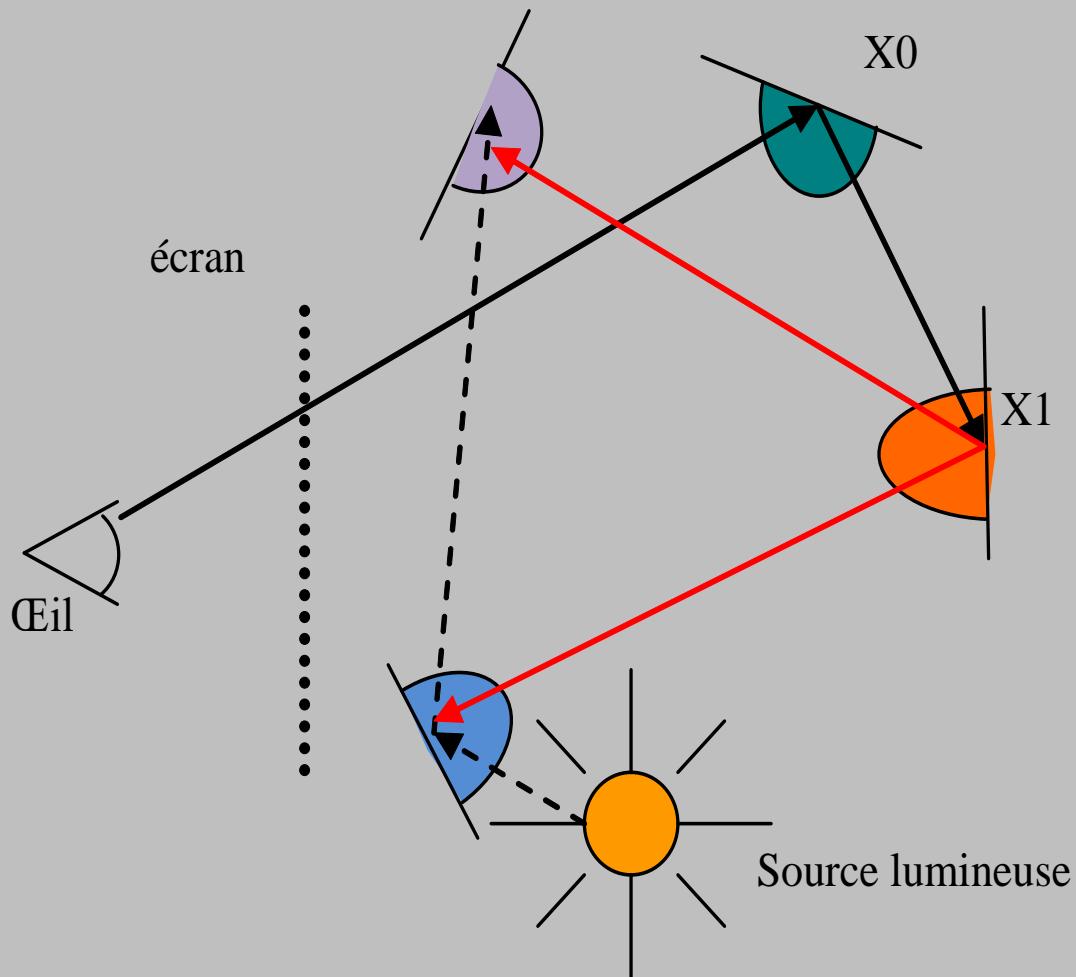
- Path tracing







- Bidirectional path tracing



- Photon Mapping









# Radiosité

- Radiosité

$$L_r(x, \vec{\omega}_r) =$$

$$L_e(x, \vec{\omega}_r) +$$

$$\rho(x) \int_S L(x', \vec{\omega}'_r) G(x, x') dx' x'$$

- Radiosité

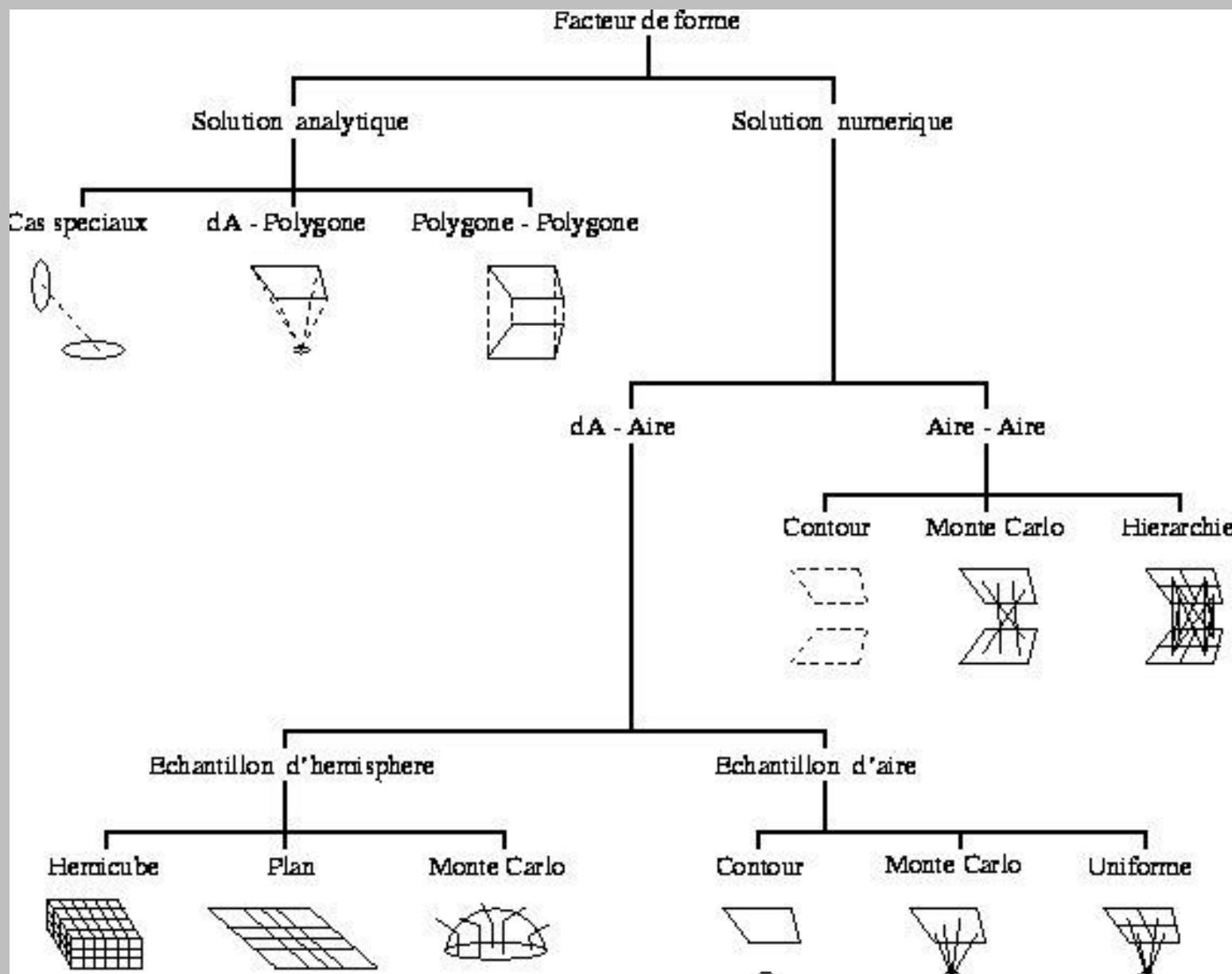
$$B_j = E_j + \rho_j \sum_{i \neq j} B_i F_{ij}$$

- Radiosité

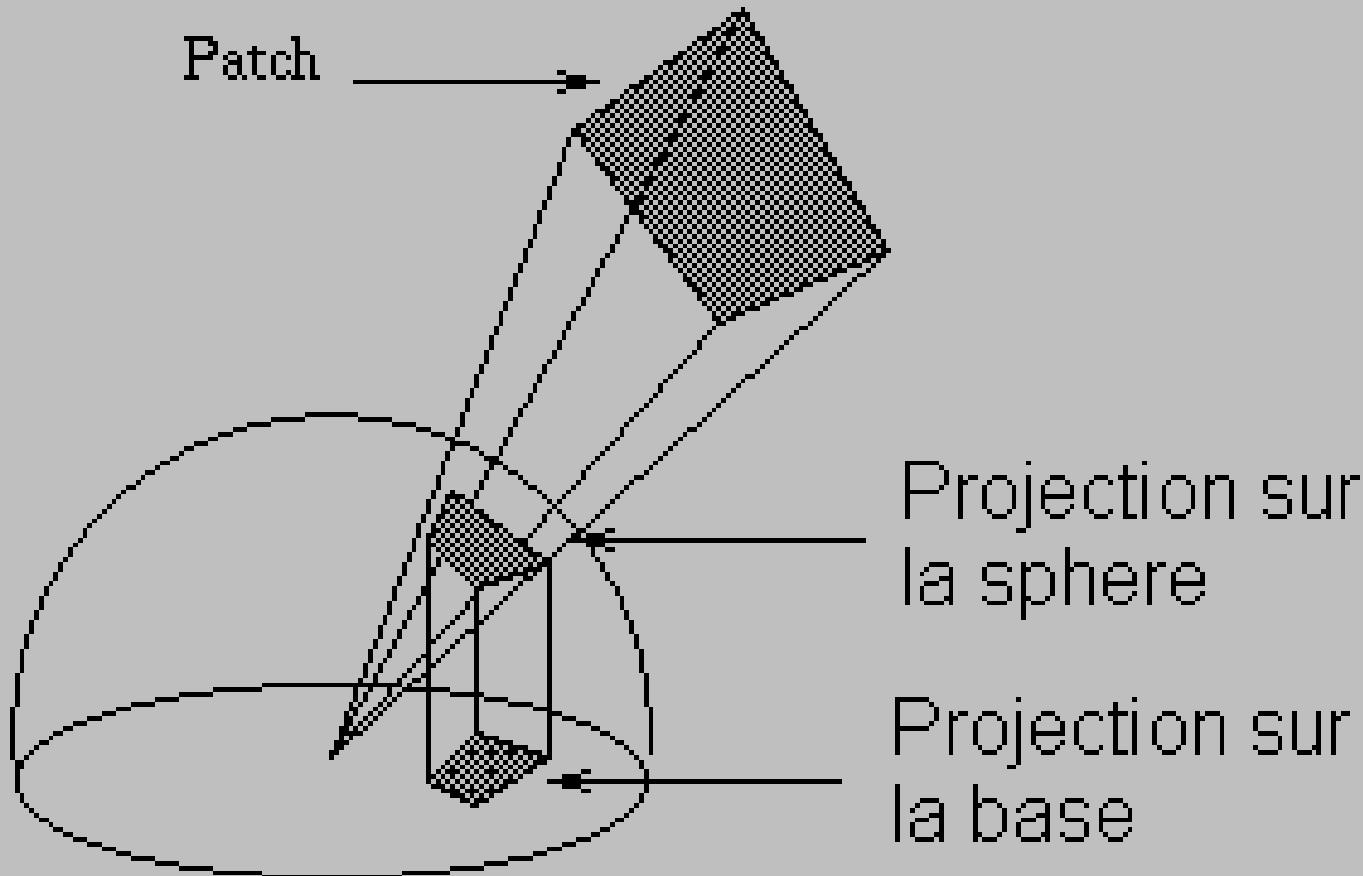
$$[M] \times [B] = [E]$$

$$\begin{bmatrix} 1 & -\rho_1 F_{12} & \cdots & -\rho_1 F_{1n} \\ -\rho_2 F_{21} & 1 & \cdots & -\rho_2 F_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ -\rho_n F_{n1} & -\rho_1 F_{n2} & \cdots & 1 \end{bmatrix} \times \begin{bmatrix} B_1 \\ B_2 \\ \vdots \\ B_n \end{bmatrix} = \begin{bmatrix} E_1 \\ E_2 \\ \vdots \\ E_n \end{bmatrix}$$

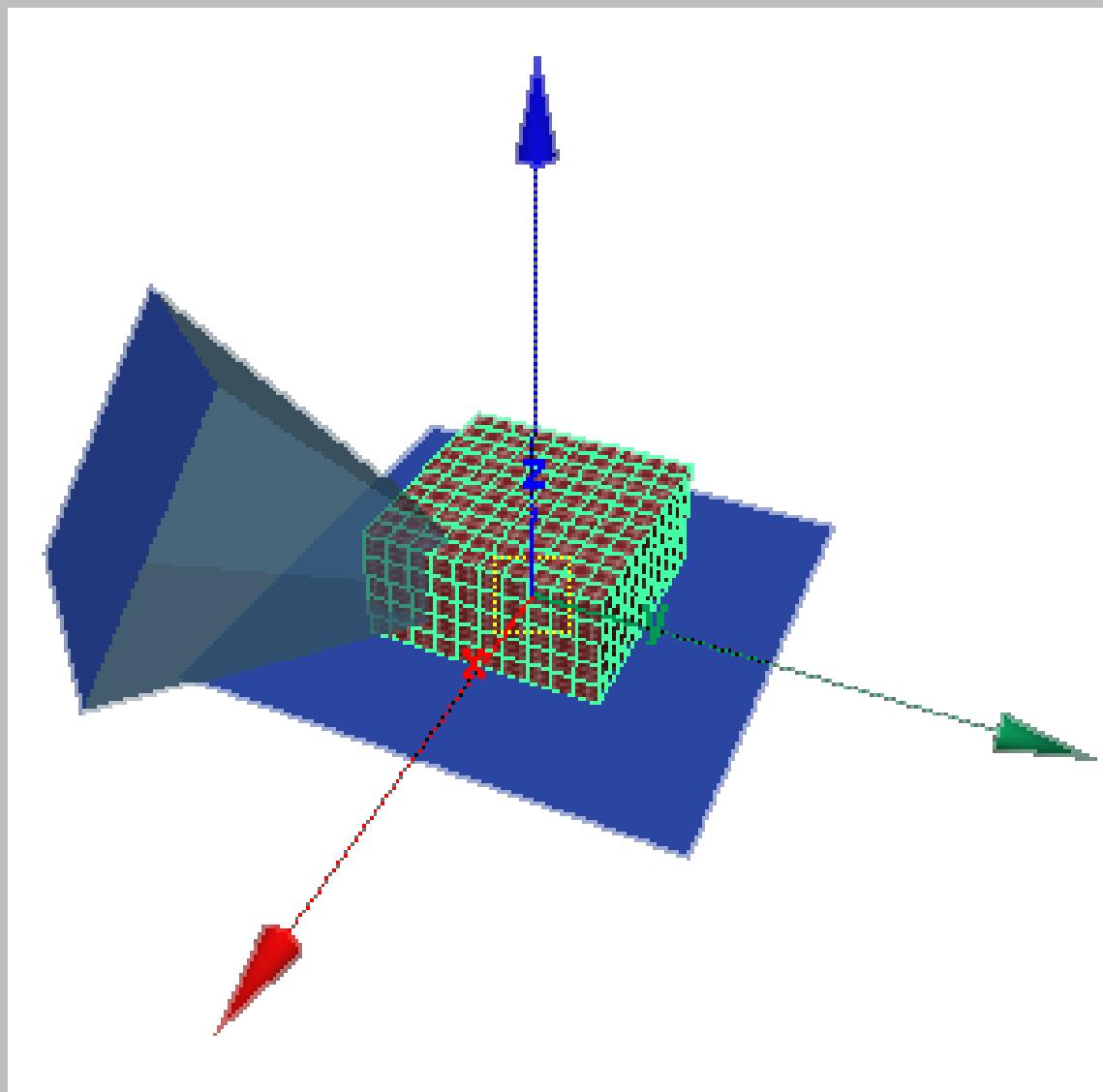
# • Radiosité



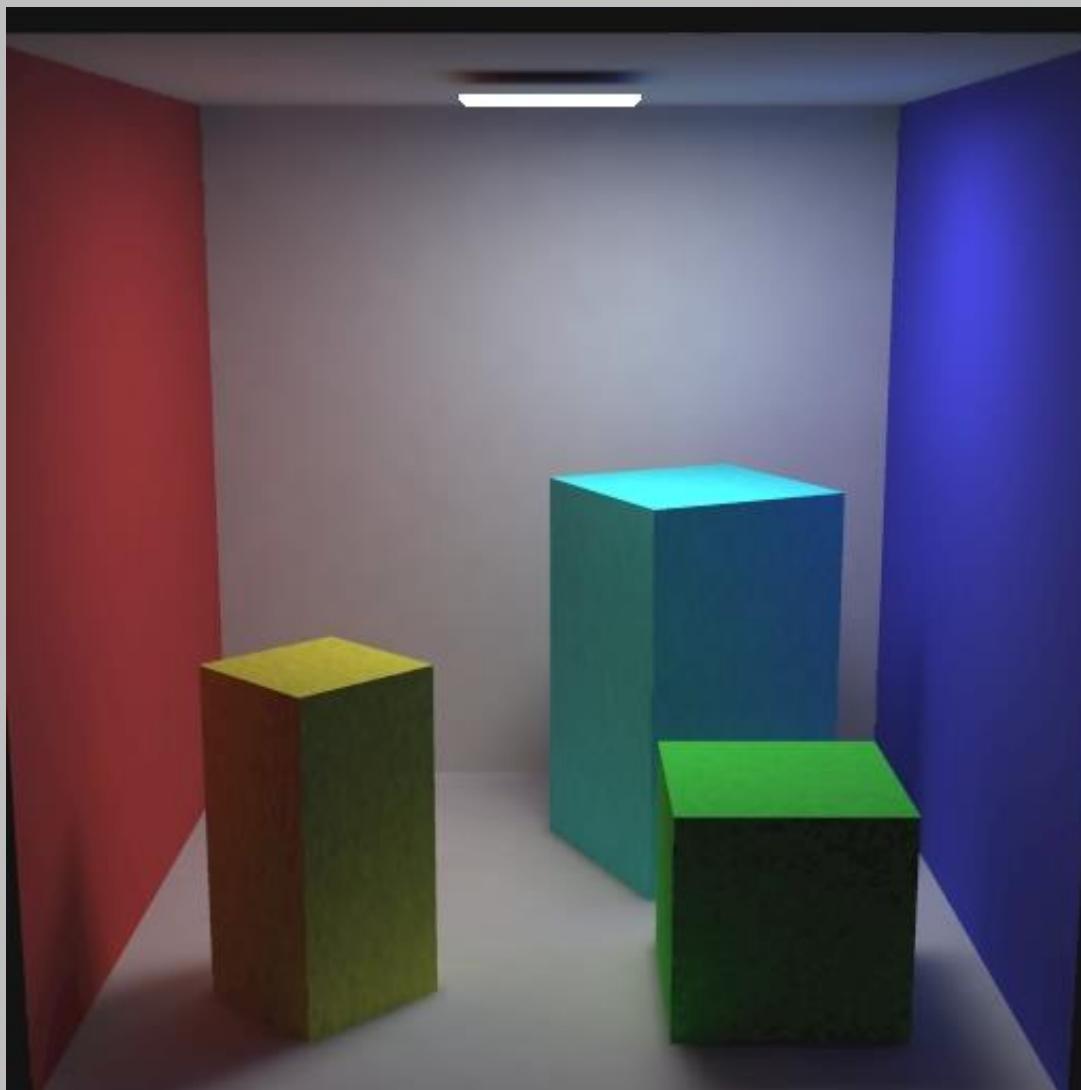
- Radiosité



- Radiosité

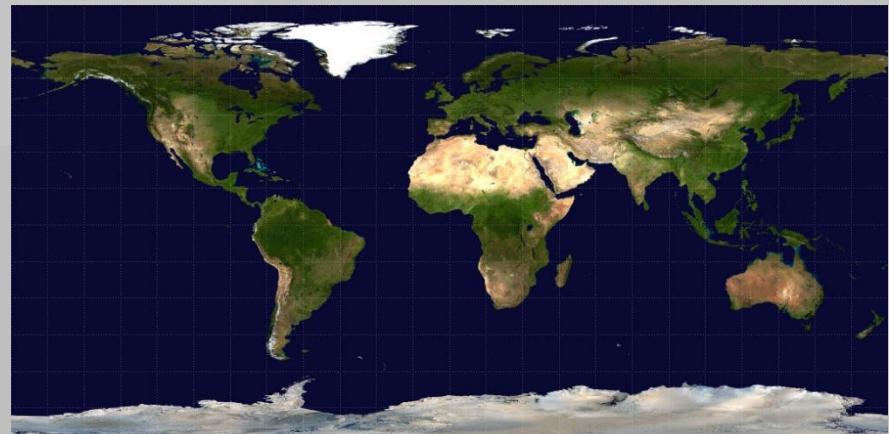


- Radiosité

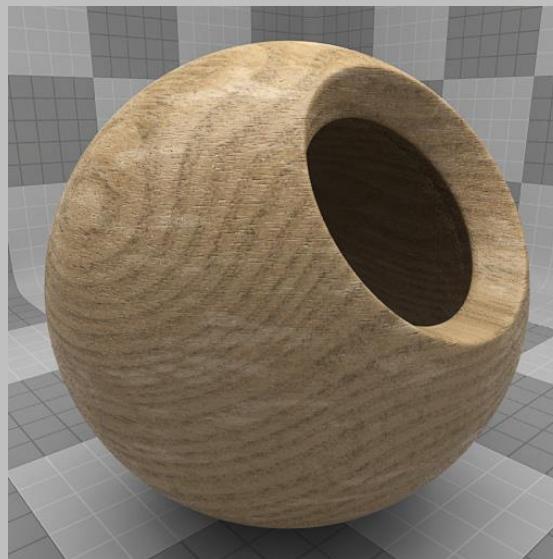
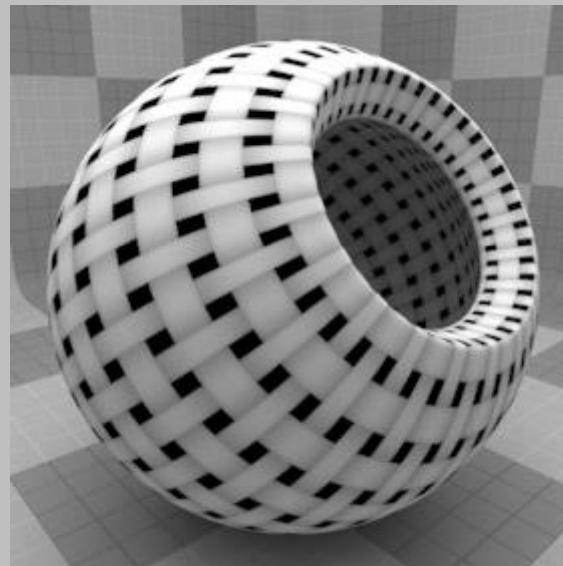
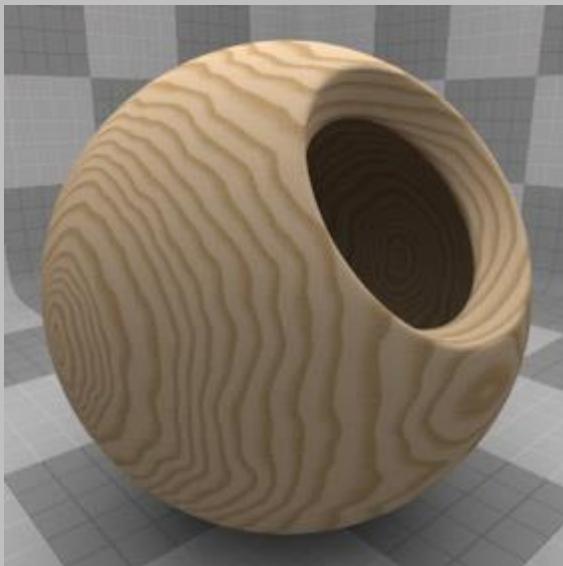


# Textures

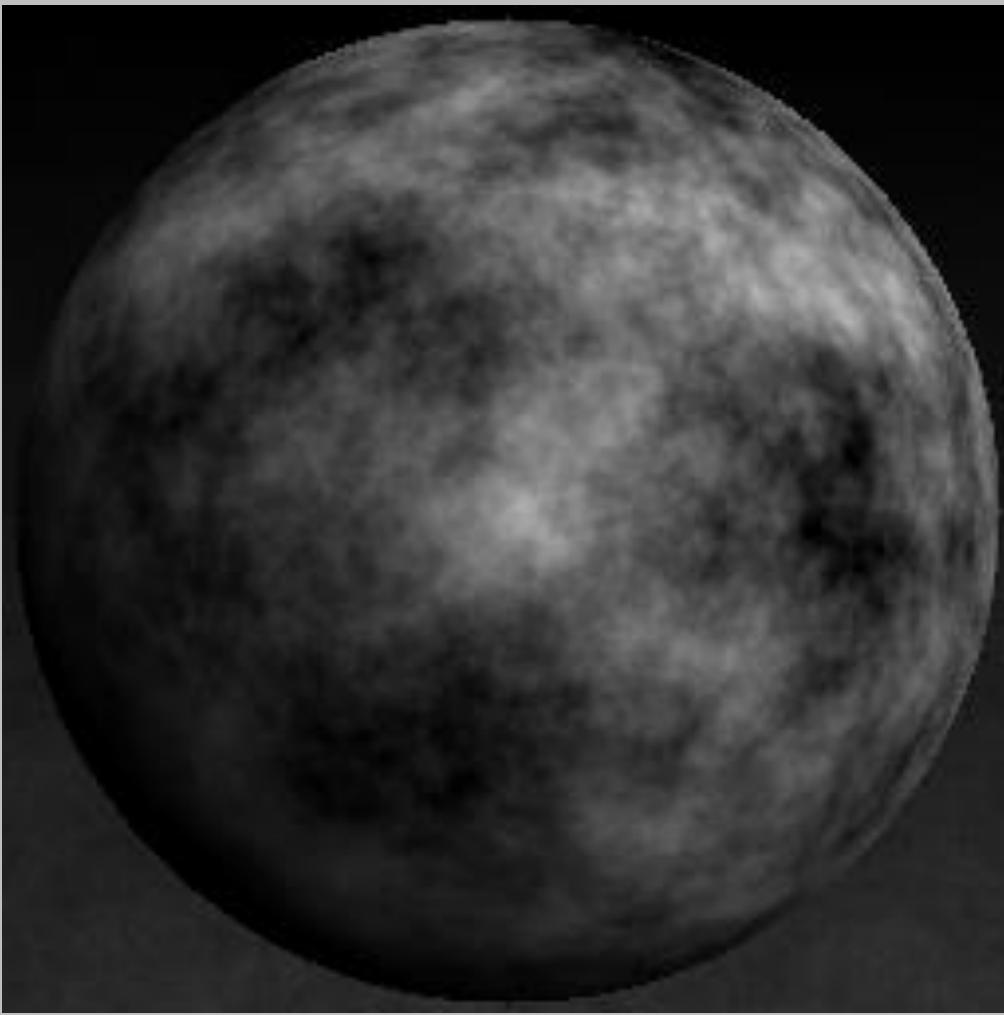
- Texture bitmap (kd)



- Texture procédural (kd)



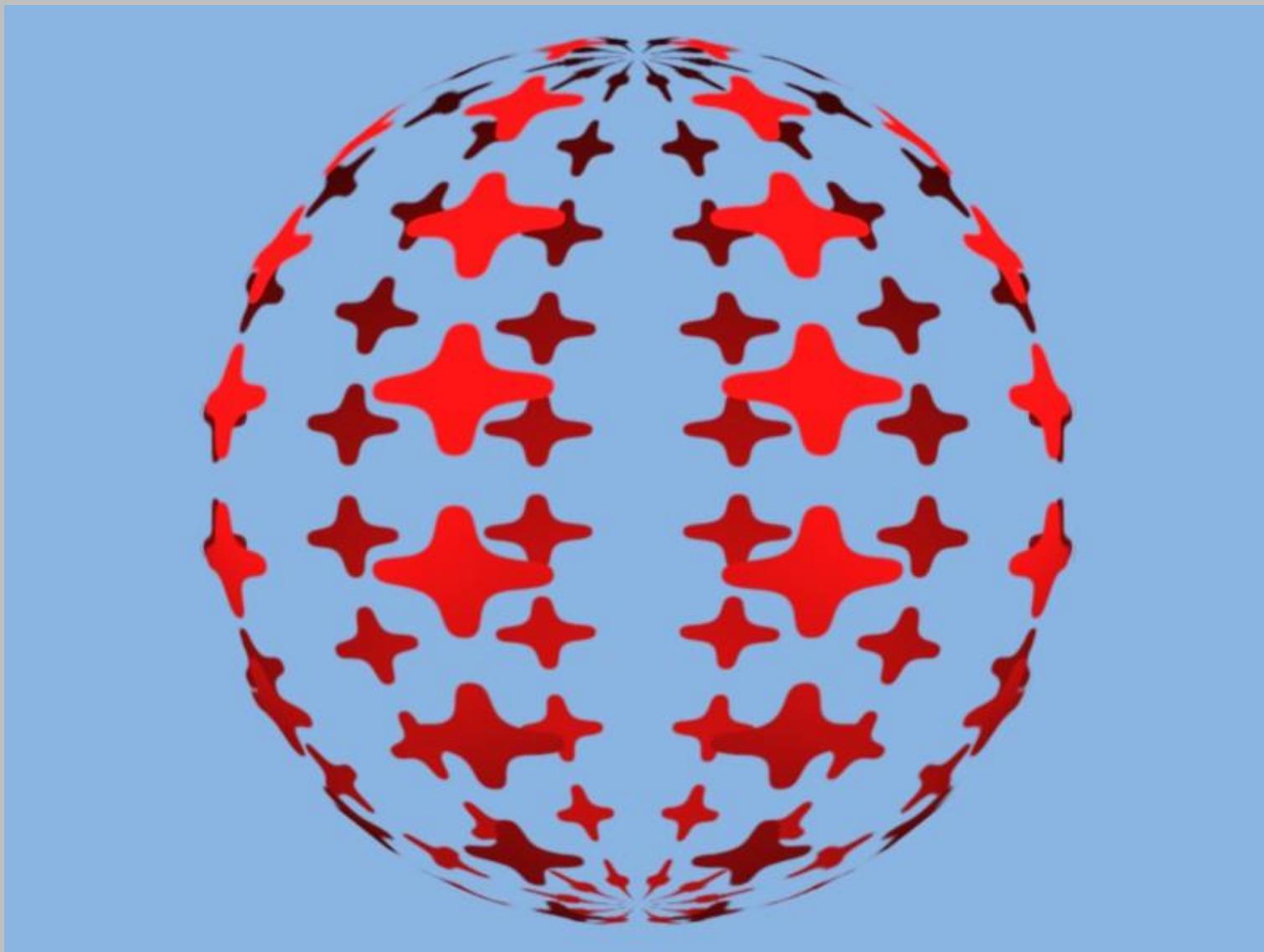
- Texture noise ( $K_d$ )



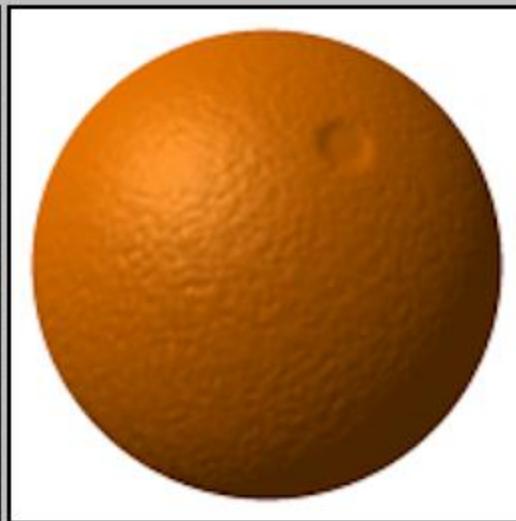
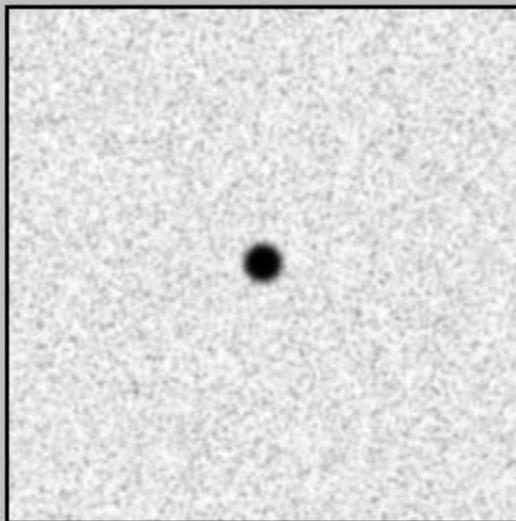
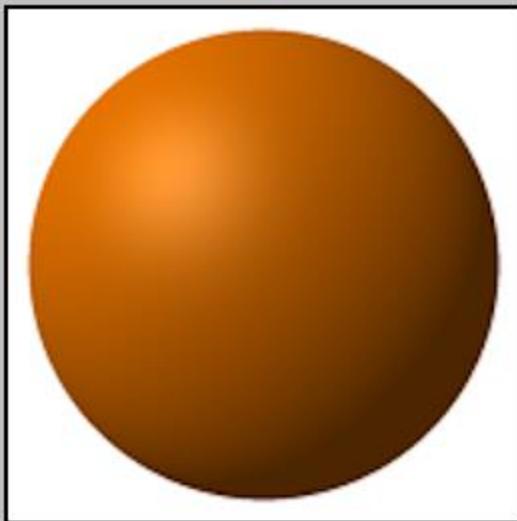
- Texture (ks)



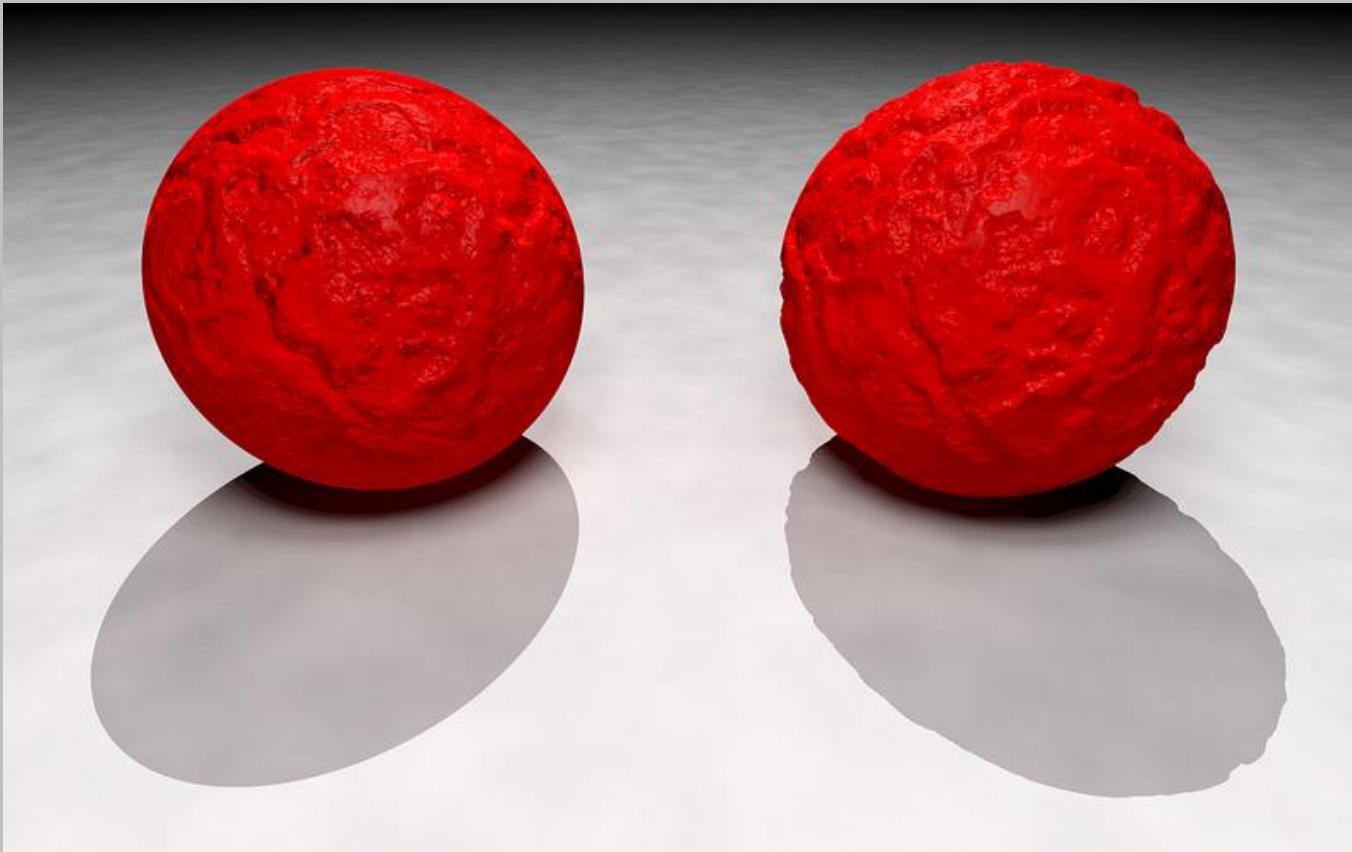
- Texture (alpha)



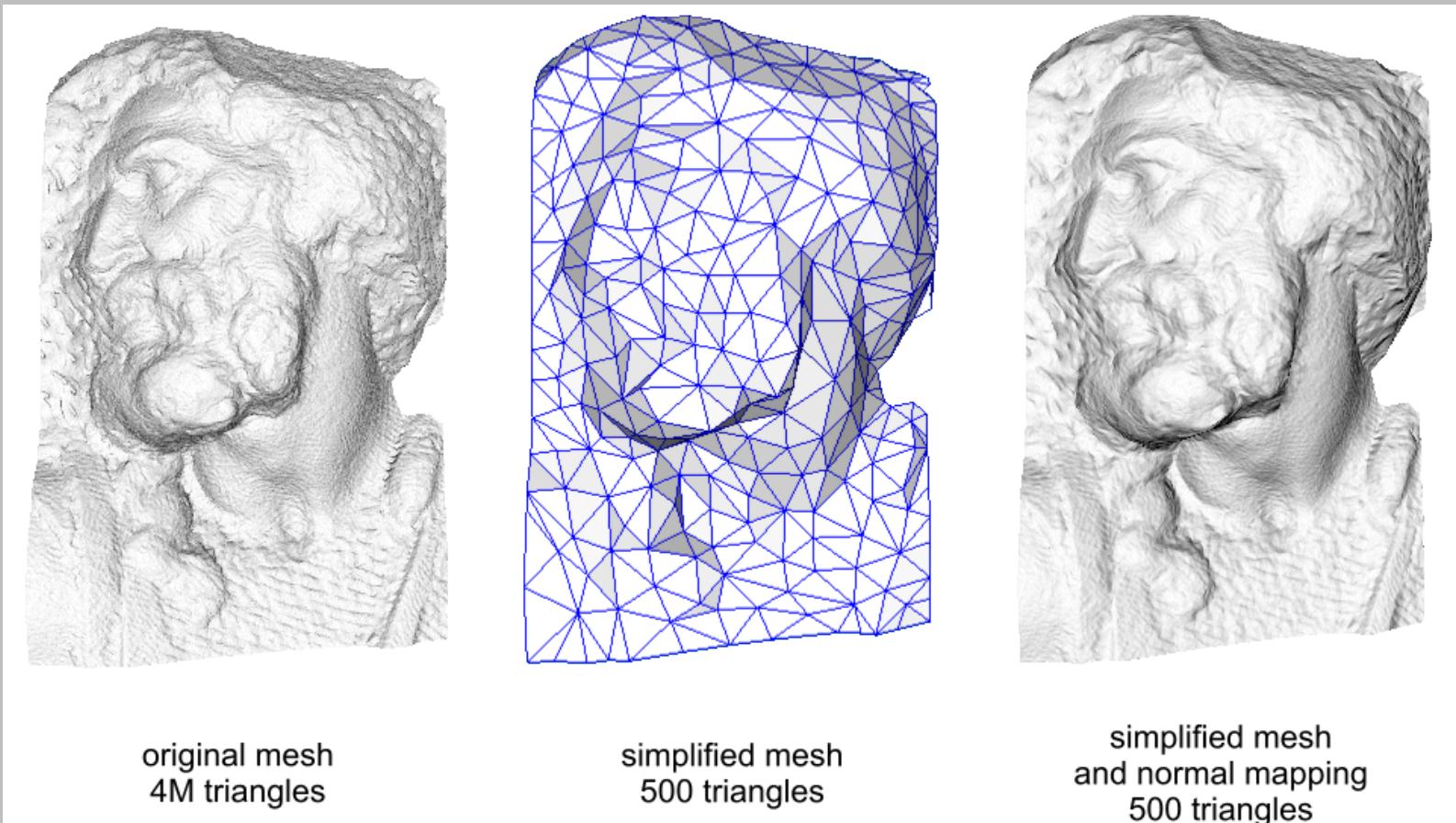
- Bump mapping



- Bump mapping vs Sub Polygon Displacement



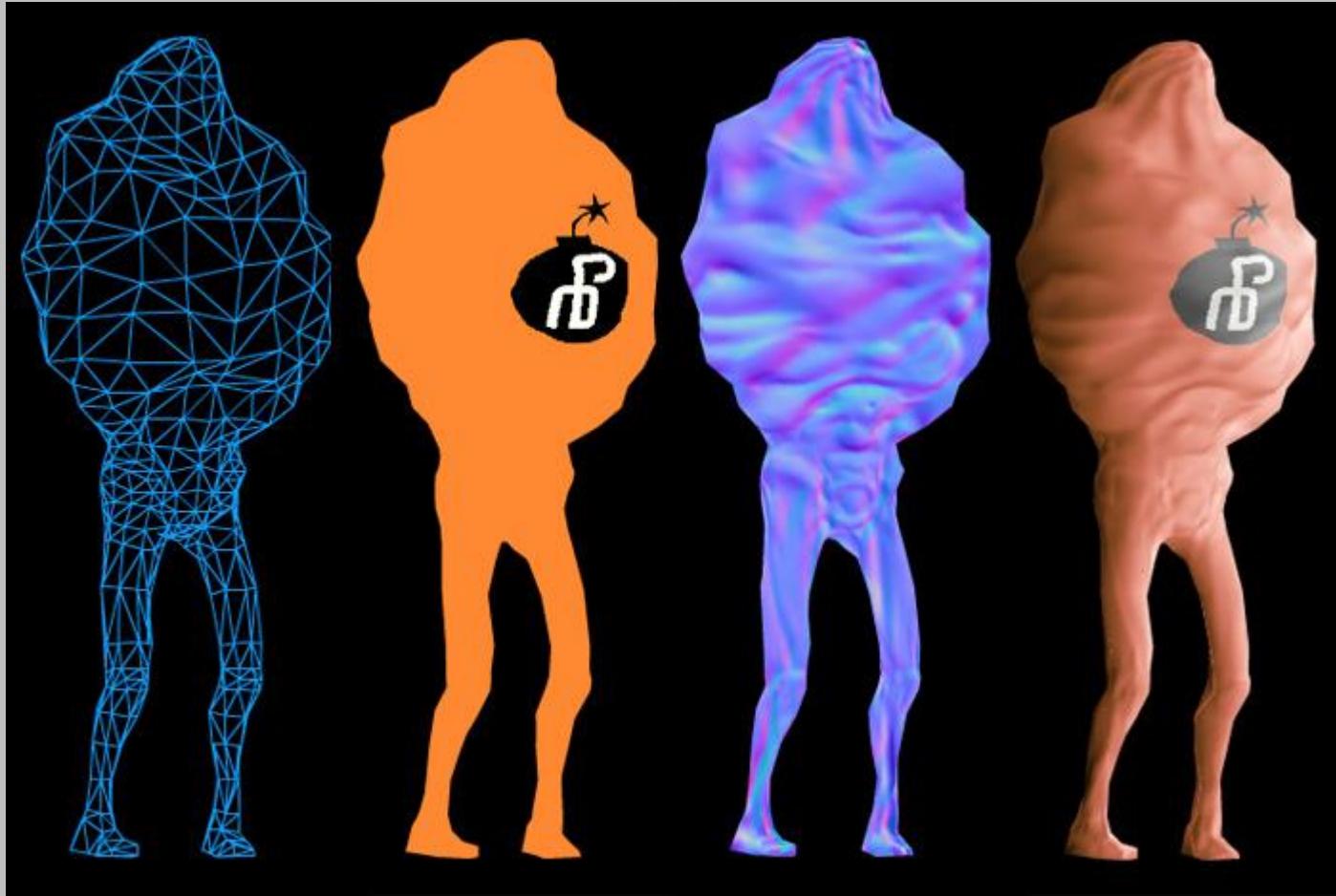
- Normal Mapping



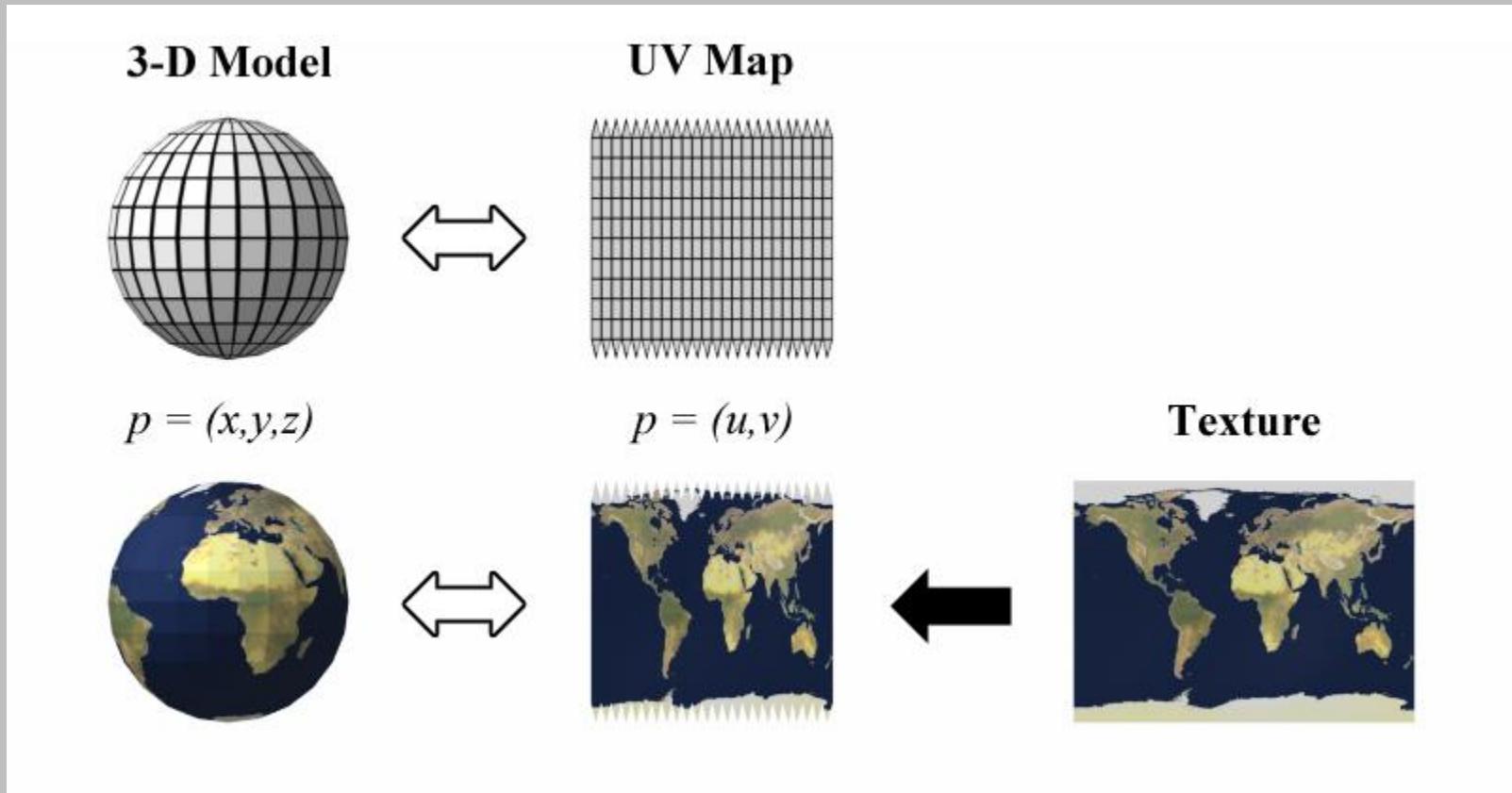
- Normal Mapping



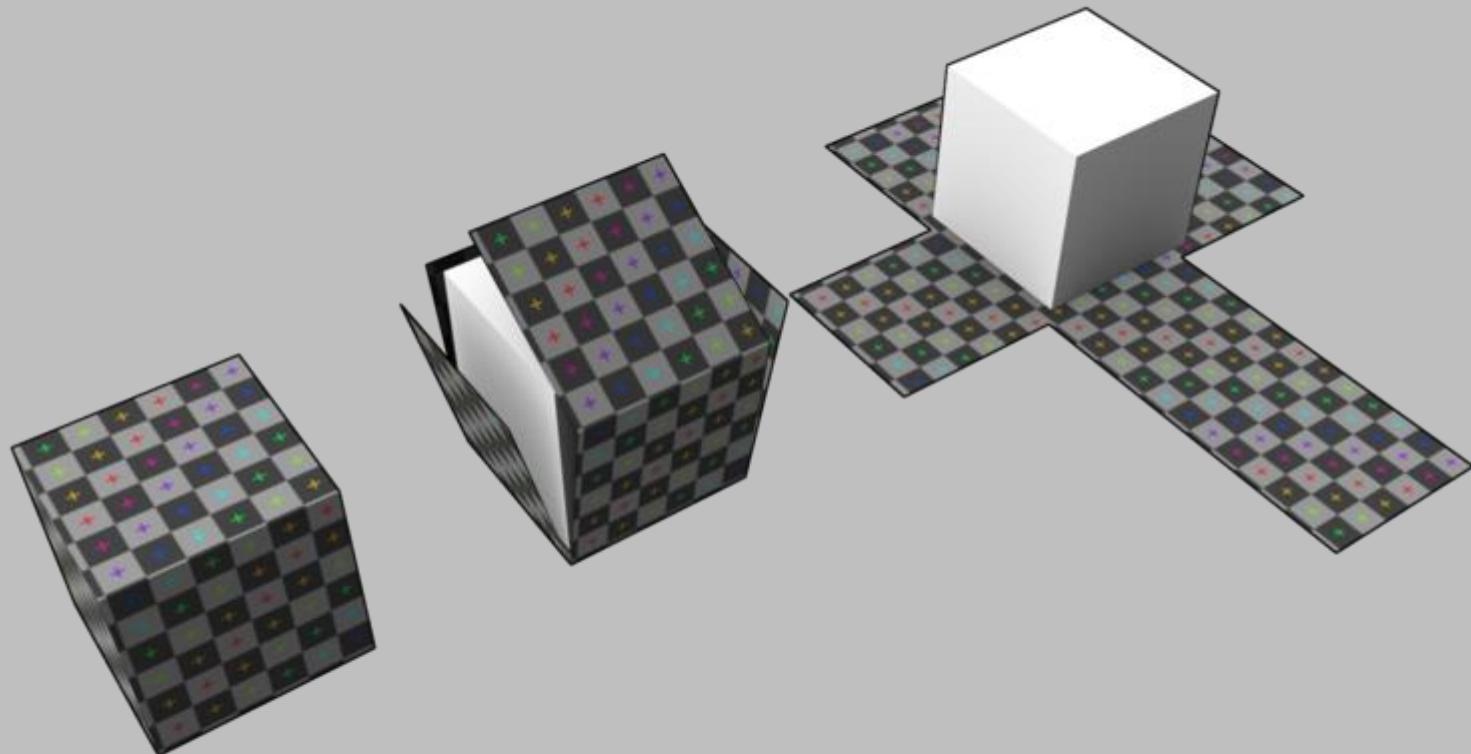
- Normal Mapping



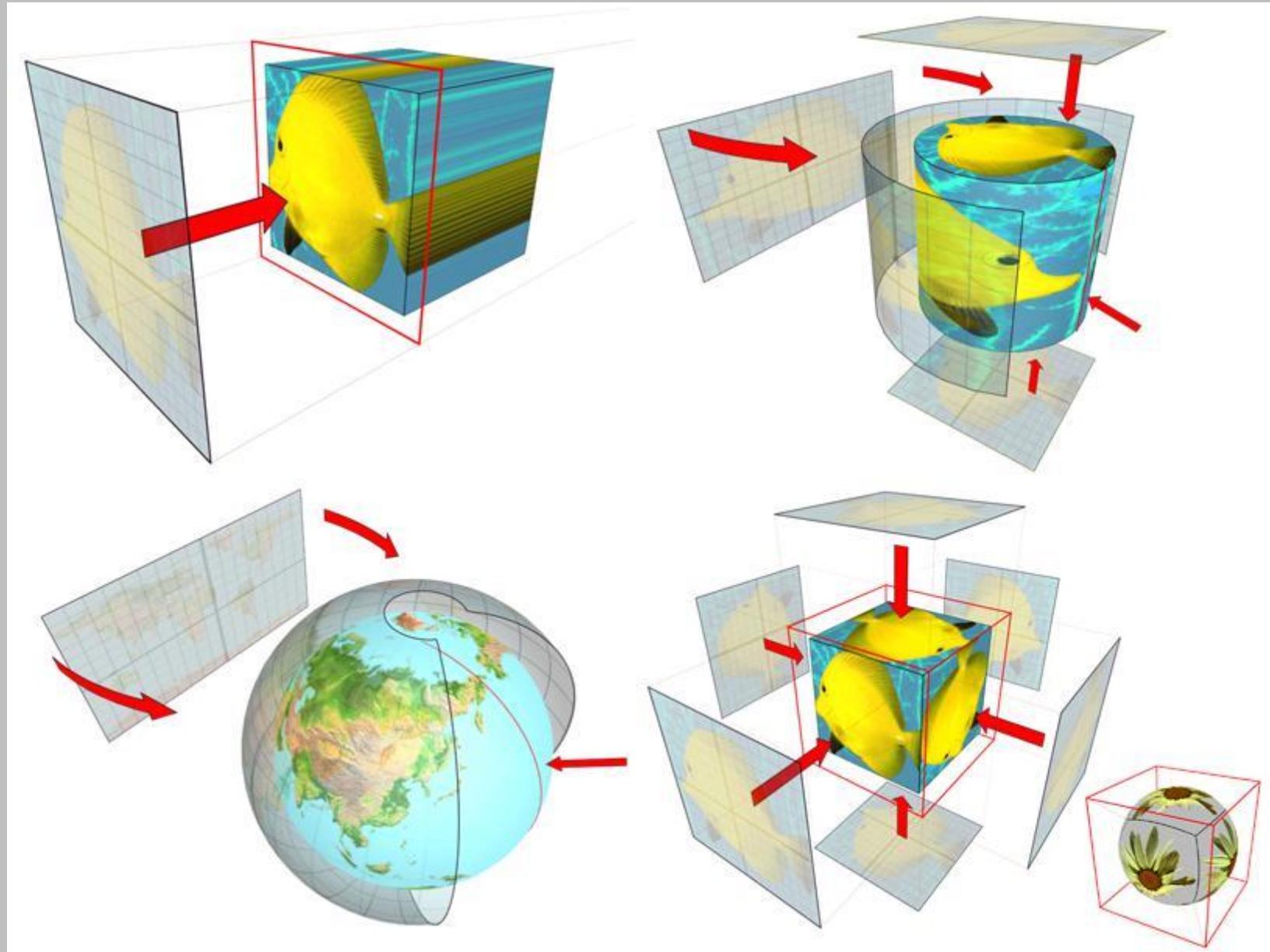
- UV Mapping



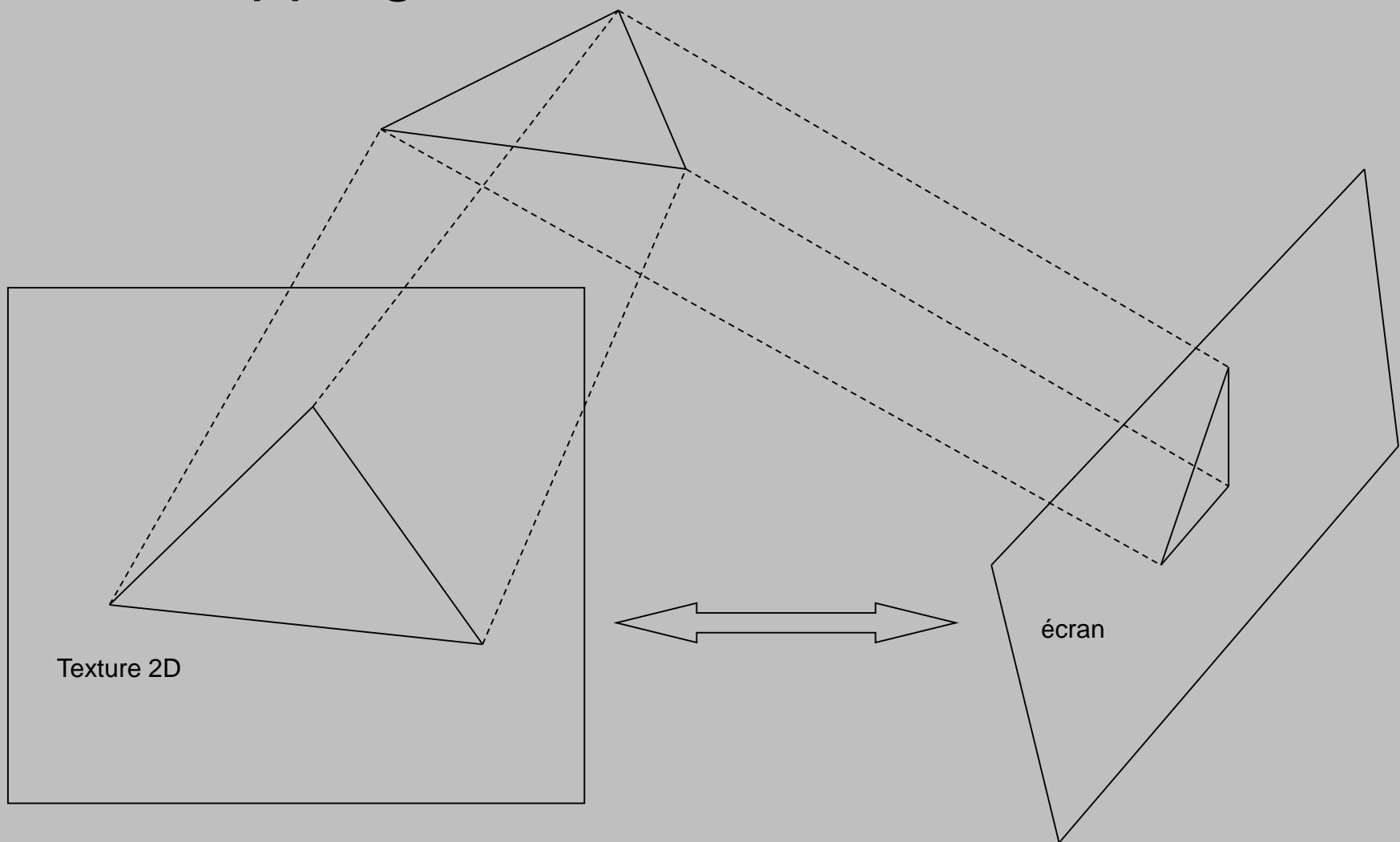
- UV Mapping



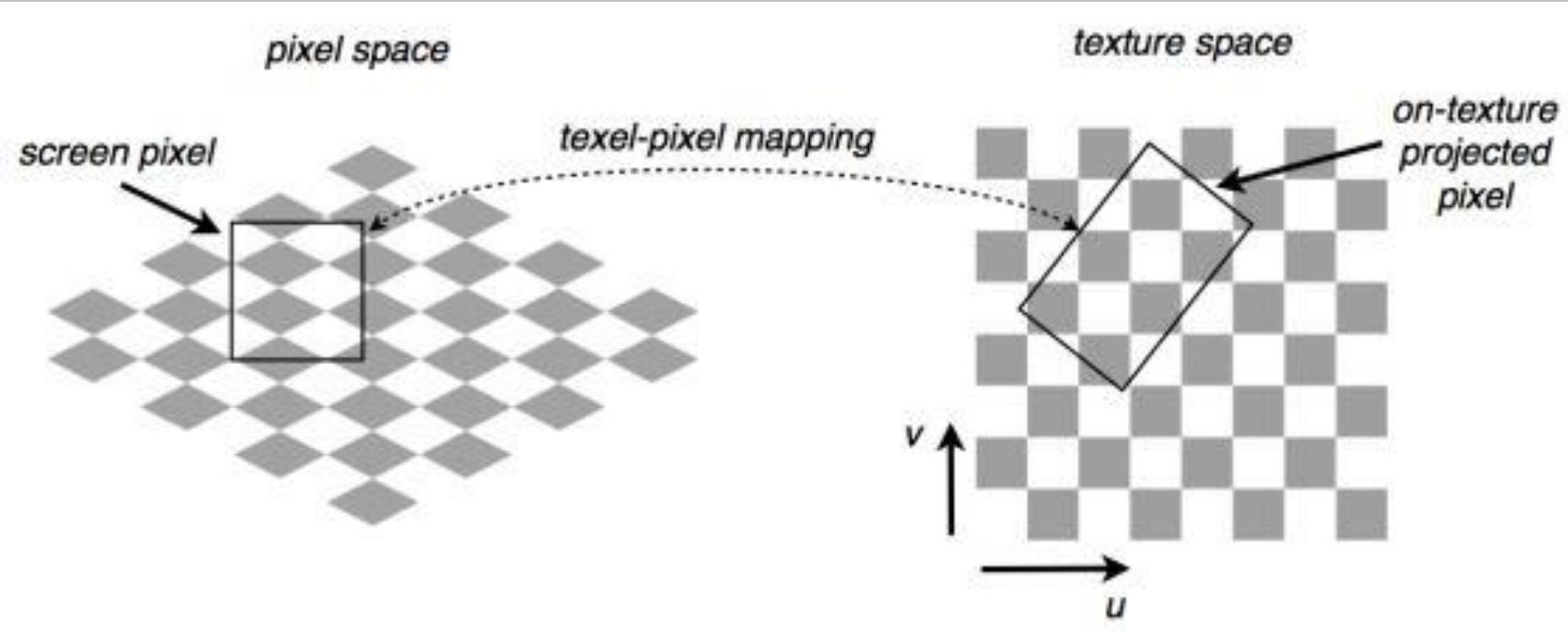
- UV Mapping



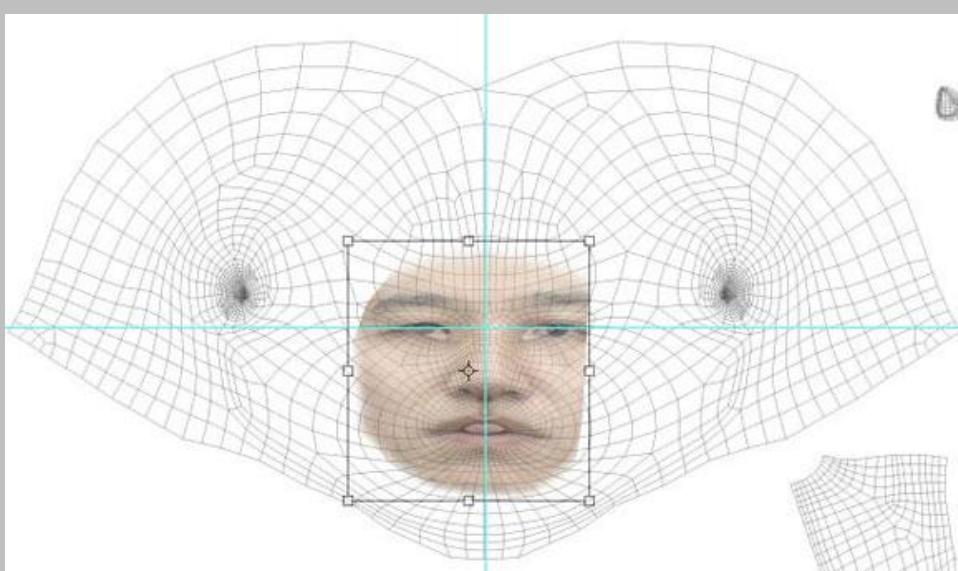
- UV Mapping



- UV Mapping

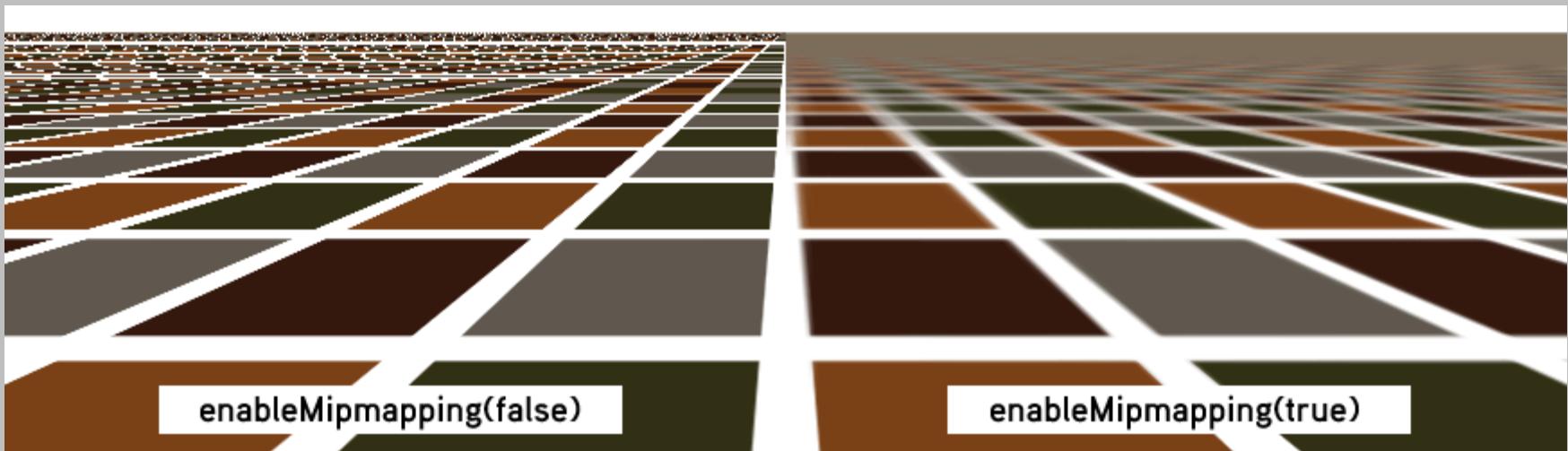
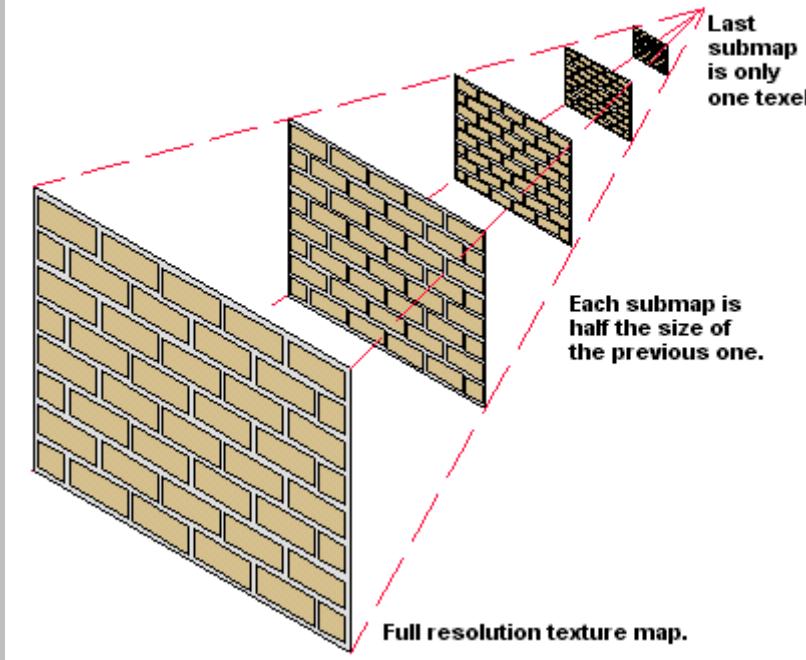


- UV Mapping



- Mipmap

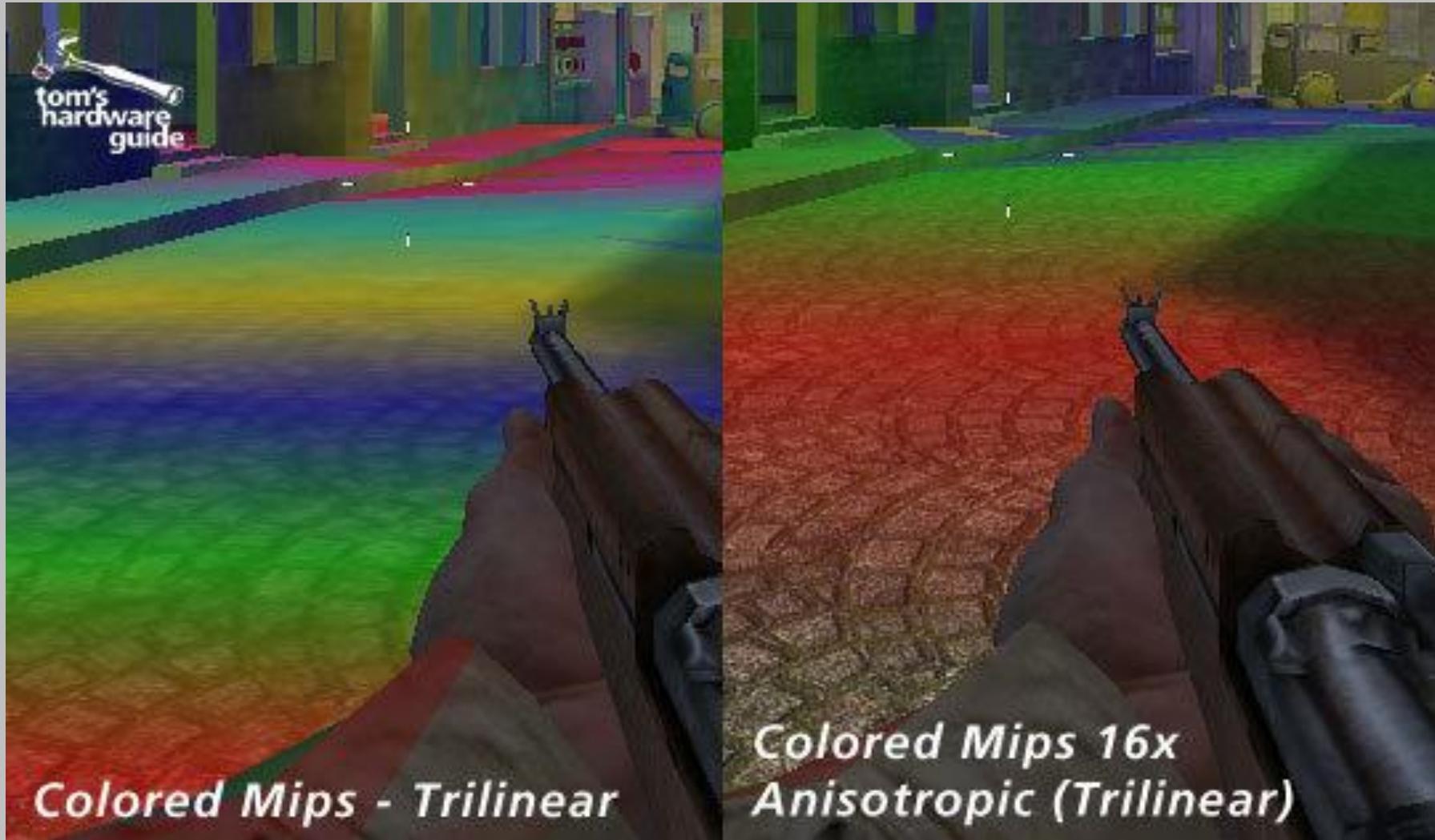
MIP maps provide more depth realism to objects, because texture maps for varying levels of depth have been prepared.



- Filtrage anisotrope



- Filtrage anisotrope

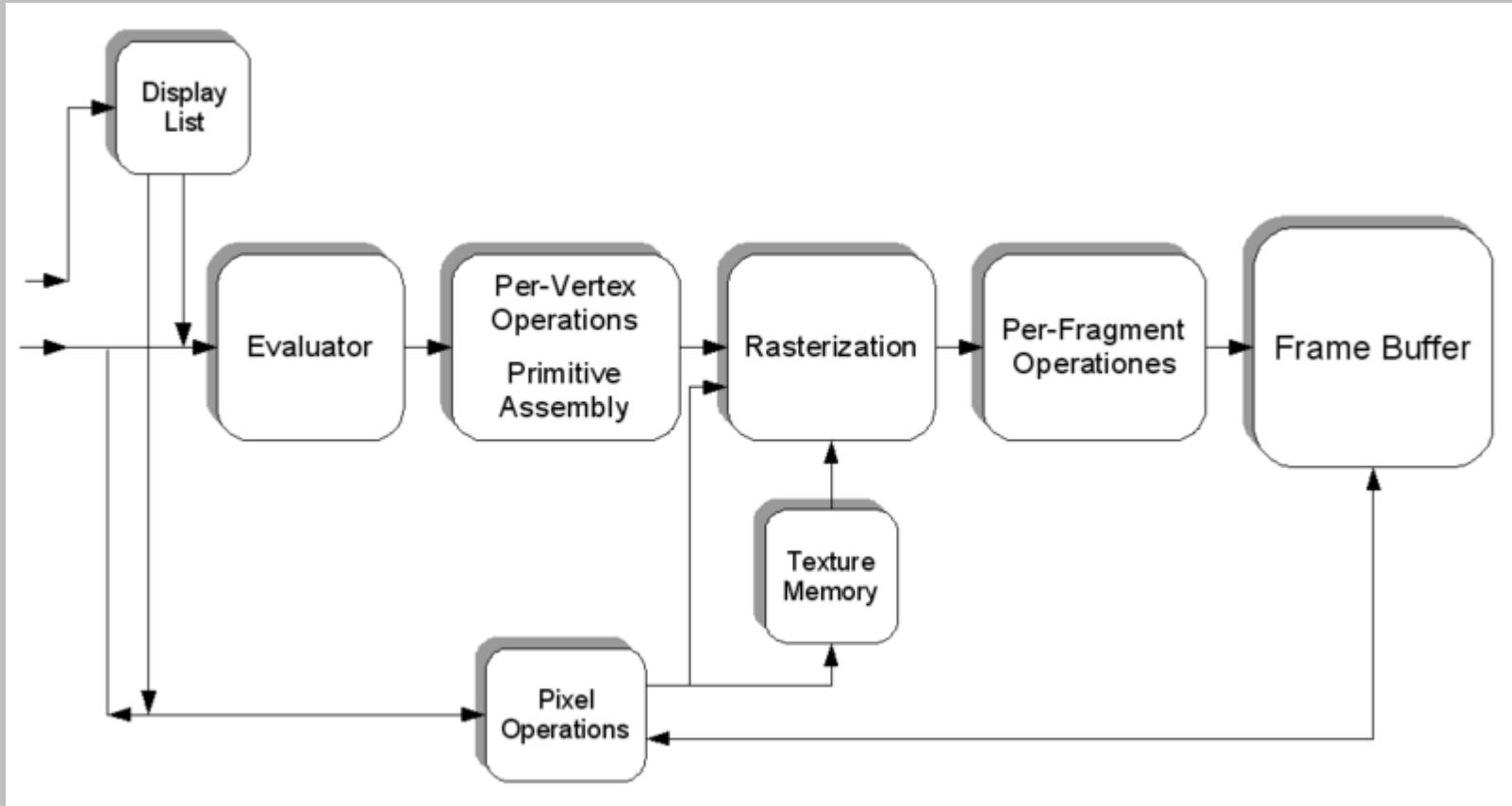


- Affine texture mapping

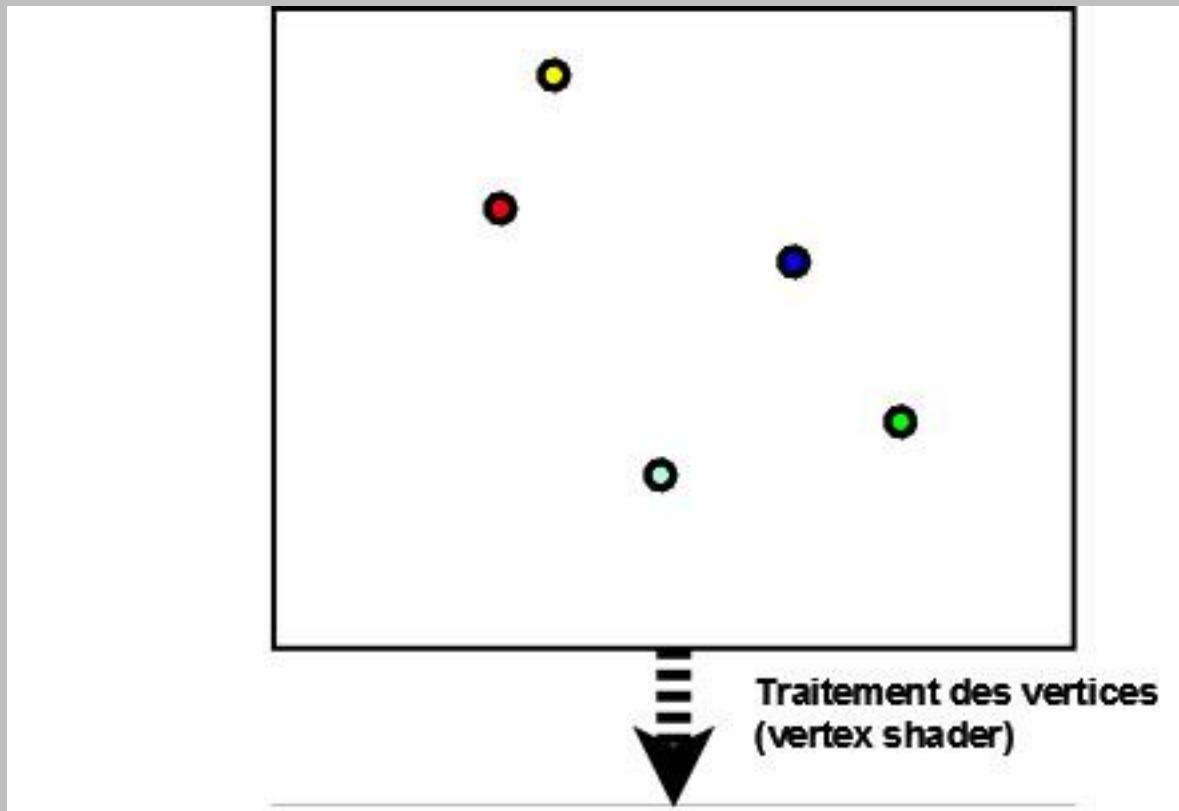


# OpenGL

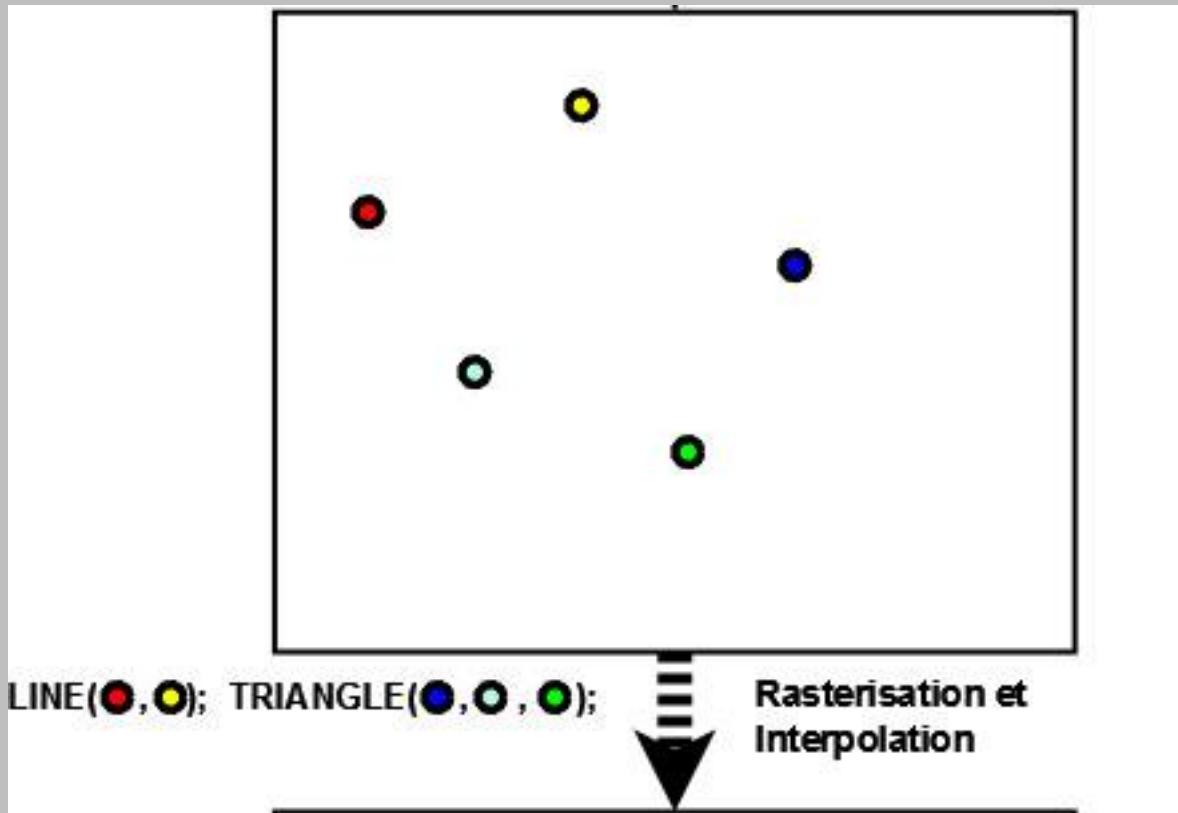
- Pipeline graphique



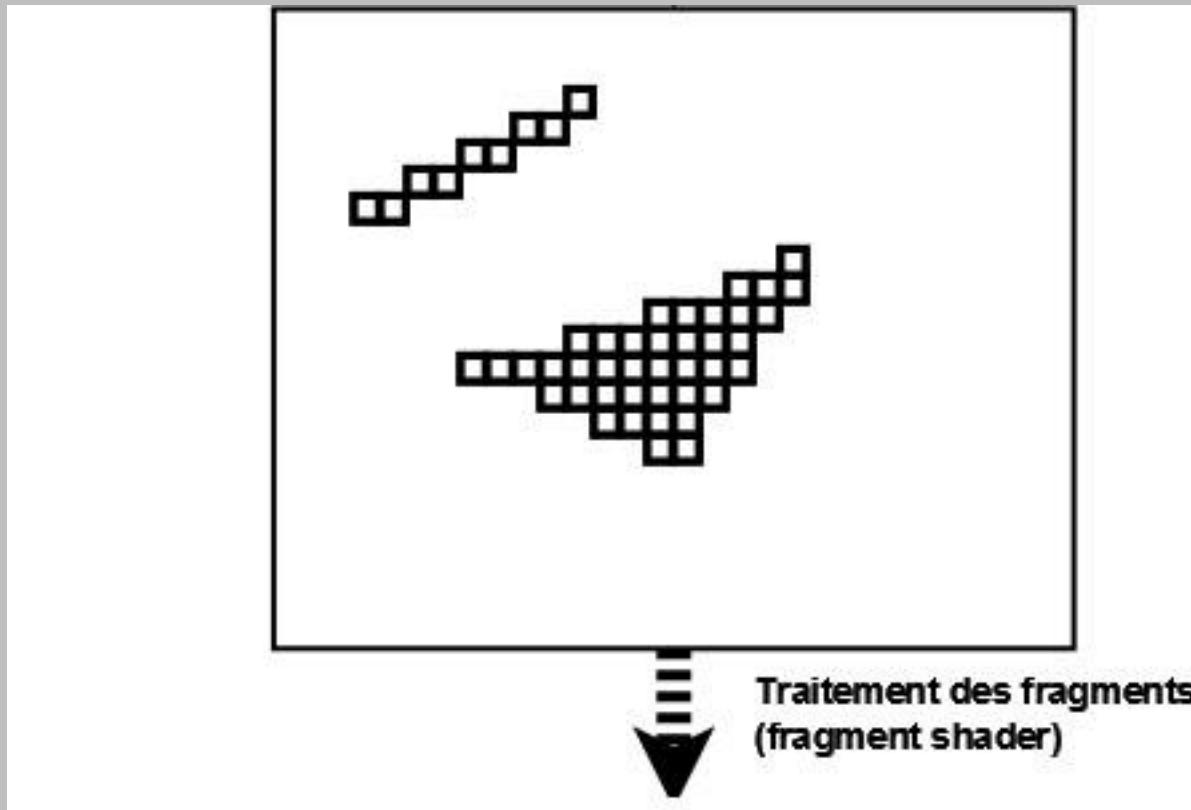
- Pipeline graphique



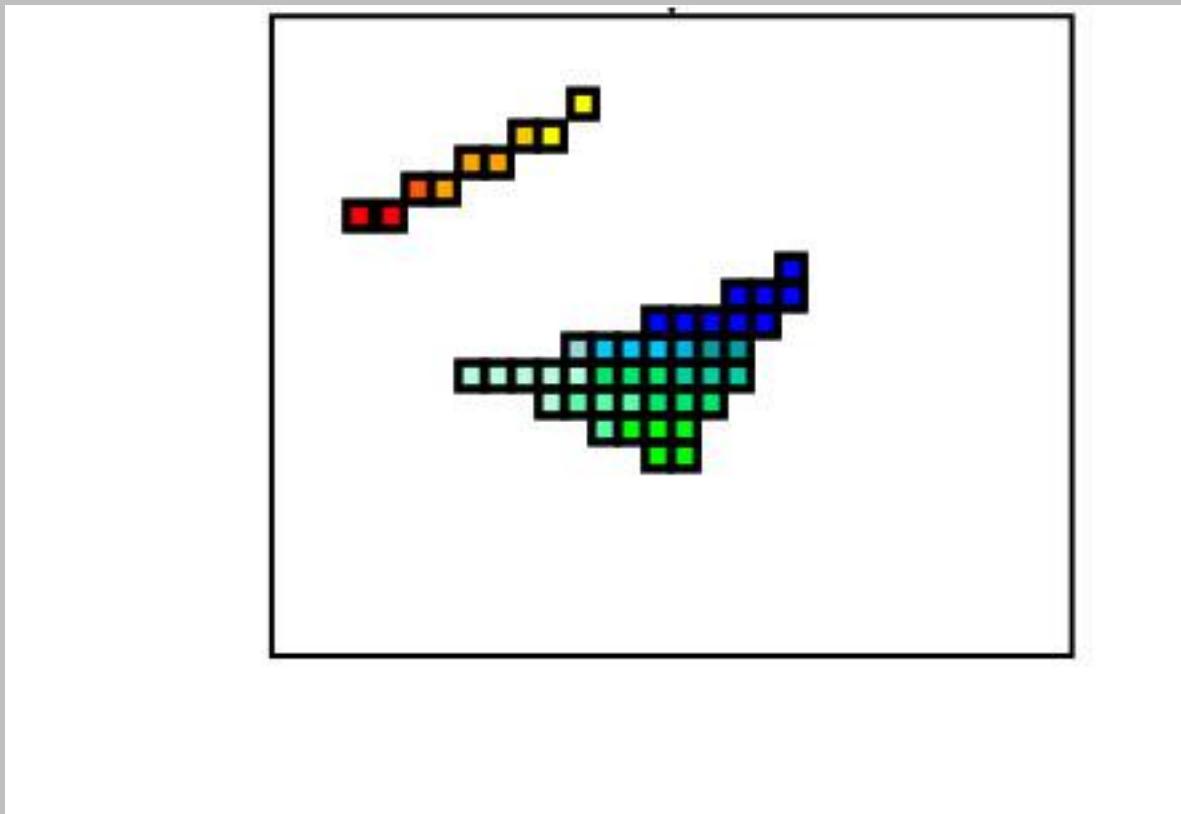
- Pipeline graphique



- Pipeline graphique



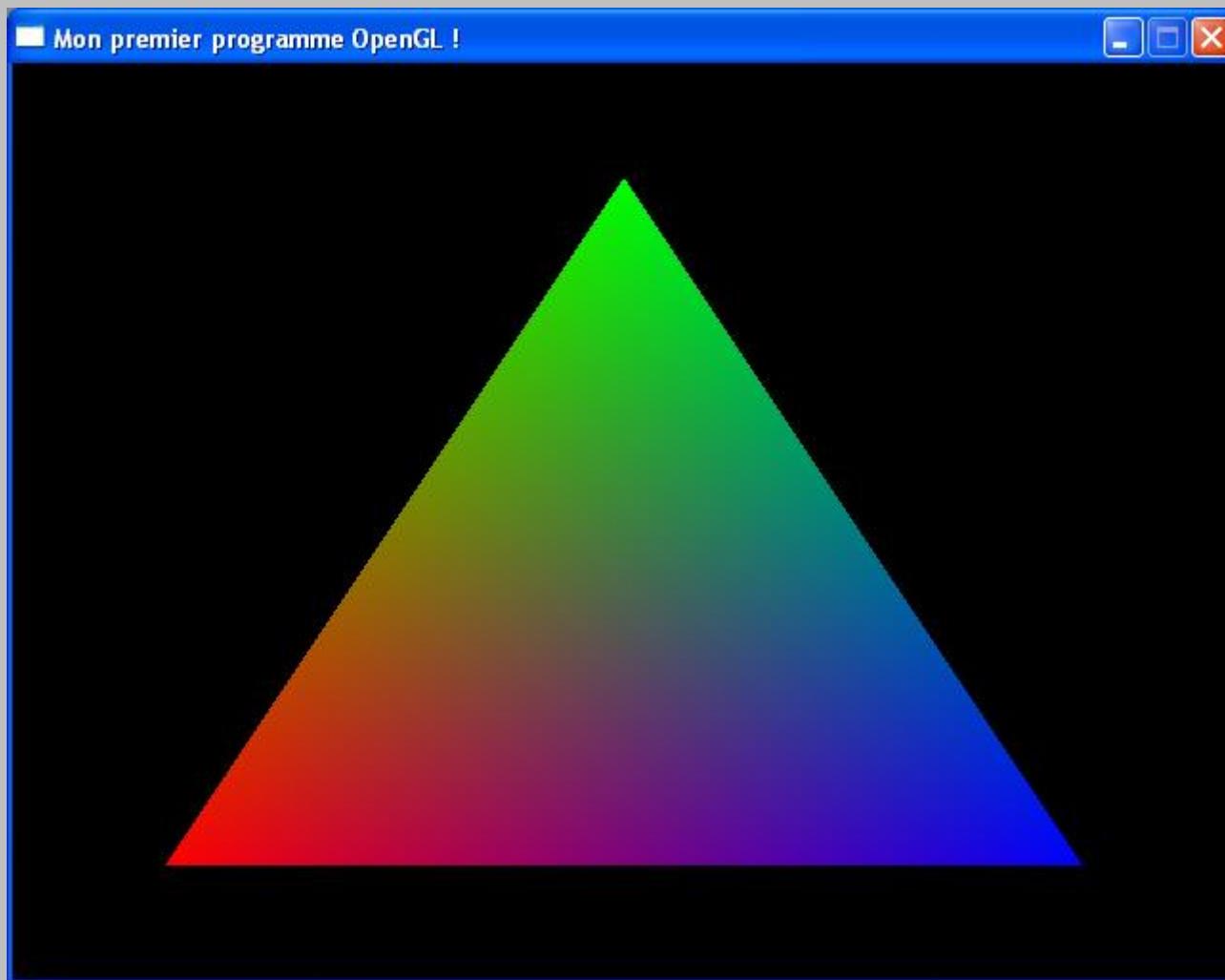
- Pipeline graphique



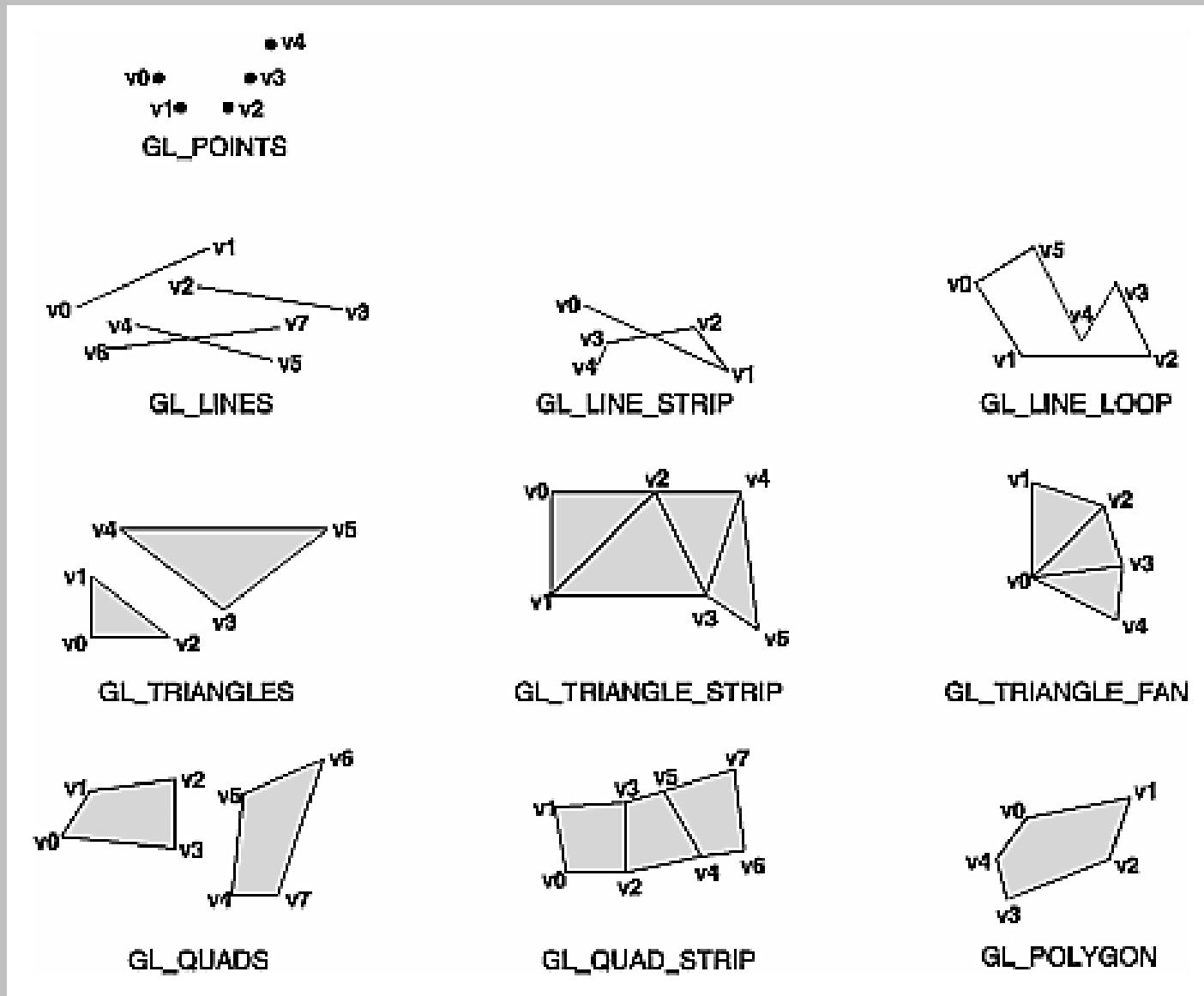
- Exemple

```
glClear(GL_COLOR_BUFFER_BIT);
    glBegin(GL_TRIANGLES);
        glColor3ub(255,0,0);    glVertex2d(-0.75,-0.75);
        glColor3ub(0,255,0);    glVertex2d(0,0.75);
        glColor3ub(0,0,255);    glVertex2d(0.75,-0.75);
    glEnd();
```

- Exemple



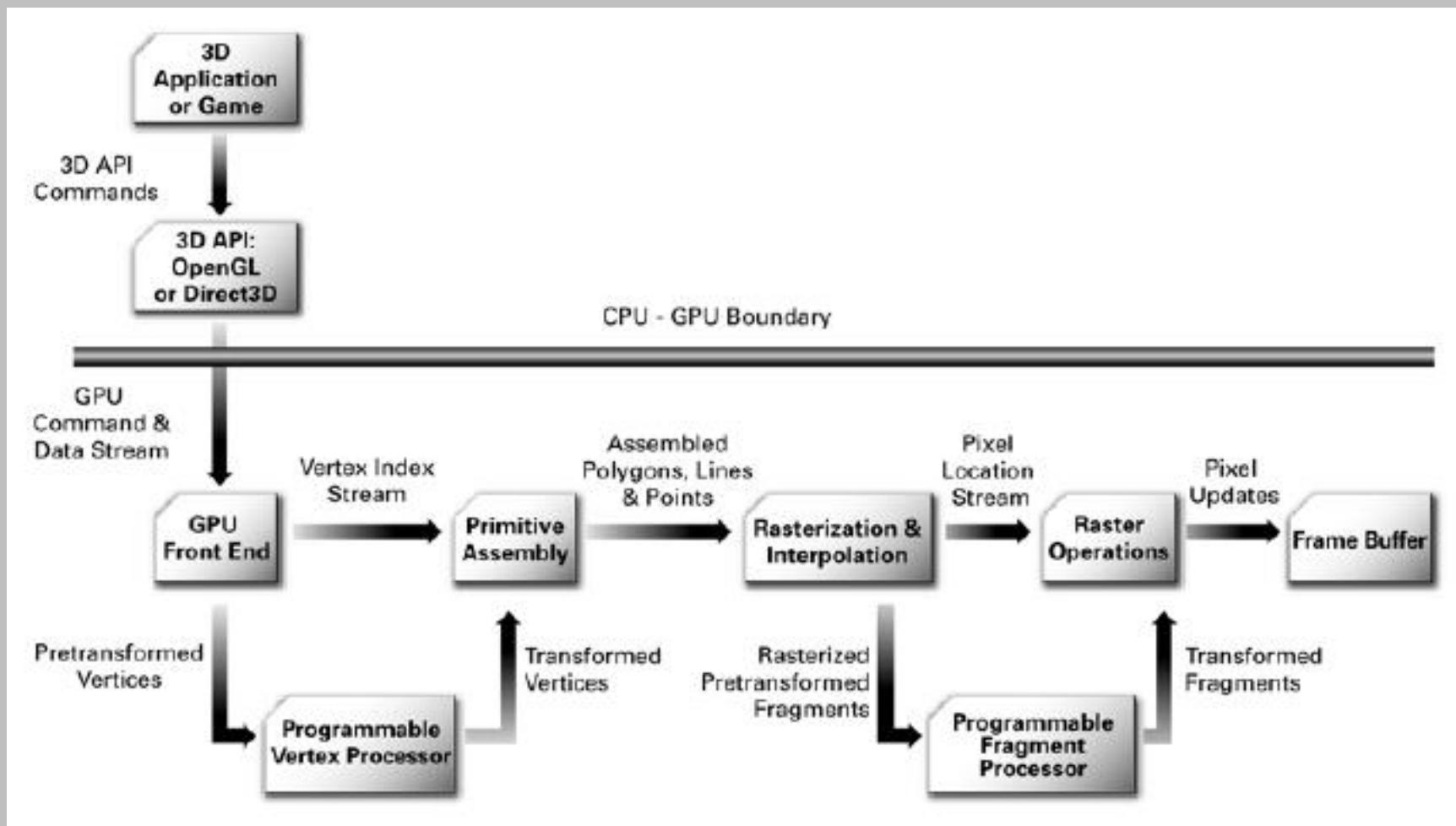
# • Types de primitives



- Matrices & transformations

```
glMatrixMode(GL_PROJECTION);
gluLookAt(3,2,3,0,0,0,0,1,0);
glMatrixMode( GL_MODELVIEW );
glLoadIdentity( );
glPushMatrix() ;
    glTranslate3f(x,y,z) ;
    glRotate3f(ax,ay,az) ;
    glBegin(...)  
    ...  
    glEnd() ;
glPopMatrix() ;
```

# • Shaders



- Fragment shader

```
void main()
{
    gl_FragColor = vec4(1.0, 0.6, 0.0, 1.0);
}
```



- Fragment shader

```
void main()
{
    gl_FragColor = gl_Color;
    gl_FragColor[1] = 1.0 - gl_Color[1];
}
```



- Vertex shader

```
void main()
{
    vec4 coords = gl_Vertex;
    coords.z = coords.z * 0.25;
    gl_Position = gl_ModelViewProjectionMatrix * coords;
}
```



- Vertex shader (diffus)

```
varying vec3 normale;  
varying vec3 lumiere;  
void main()  
{  
    gl_Position = gl_ModelViewProjectionMatrix * gl_Vertex;  
    normale = normalize(gl_NormalMatrix * gl_Normal);  
    vec4 pospoint = gl_ModelViewMatrix * gl_Vertex;  
    vec4 poslum = gl_LightSource[0].position;  
    lumiere = vec3(poslum - pospoint);  
}
```

- Fragment shader (diffus)

```
varying vec3 normale;
varying vec3 lumiere;
void main()
{
    gl_FragColor=vec3(0,0,0);
    const vec4 Kd = vec4(0.8, 0.4, 0.0, 1.0);
    float NL = dot(normalize(normale), normalize(lumiere));
    if (NL > 0) {
        gl_FragColor = Kd * NL;
    }
}
```

FPS: 31



Compilation: Ok.





Activision R&D

Property of Activision Publishing

Not actual gameplay

**FIN**